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UNVEILING THE UNSEEN WITH THE DARK ENERGY SURVEY: GRAVITATIONAL WAVES AND DARK MATTER

Thesis submitted for the Degree of Doctor of Philosophy

by

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To my mum, dad and brother, who have always inspired me, supported me and loved me.
I, Antonella Palmese, confirm that the work presented in this thesis is my own. Where information has been derived from other sources, I confirm that this has been indicated in the thesis. In particular I note these contributions:

- The work presented in Chapter 2 has been published with the DES Science Verification data release at https://des.ncsa.illinois.edu/releases/sval1, ANNz2 has been written by Iftach Sadeh, Ofer Lahav and Filipe Abdalla, the BMA code has been written by James Annis and myself. I have worked closely with Iftach Sadeh on testing ANNz2 and providing DES Science Verification photo-z’s catalogues.

- The work presented in Chapter 3 has been published in Palmese et al. (2017). GALFIT runs have been performed by Federica Tarsitano and William Hartley, pixel color magnitude diagrams have been produced by Chris Conselice. The DES gravitational wave follow up program involves the effort of a whole team composed by a dozen people. The host matching work has been performed with the help of DES Supernovae experts. The whole pipeline is shortly described in Herner et al. (2017), and has been used in the analysis of GW170814, which will soon be published in Doctor et al. (2018). My contribution to the DECam GW follow up work partially described in this chapter has granted me co-authorship in LIGO Scientific Collaboration et al. (2017), Abbott et al. (2017a), Soares-Santos et al. (2017), Scolnic et al. (2017) and Cowperthwaite et al. (2017).

- The work presented in Chapter 4 has been published in Palmese et al. (2016).

- The work presented in Chapter 5 will shortly be published in Palmese et al. (2018) and Welch et al. (2018). Palmese et al. (2018) is currently undergoing the DES review process required for submission. The membership probability assignment work has been led by Brian Welch, with major contribution by James Annis, Huan Lin, Marcelle Soares-Santos and myself. The weak lensing mass calibration section
is part of work that has been published in Pereira et al. (2018), who lead the work with contributions by the same team.

- The work presented in Chapter 6 will also shortly be published in Palmese et al. (2018). In the last section I present work on Intra–cluster light, which has been lead by Yuanyuan Zhang and to which I gave major contributions. This work is undergoing the DES review process and will shortly be published in Zhang, Yanny, Palmese et al. (2018).
In this thesis I show how large galaxy surveys, in particular the study of the properties of galaxies, can shed light on gravitational wave sources and dark matter. This is achieved using the latest data from the Dark Energy Survey, an on-going 5000 deg$^2$ optical survey. Galaxy properties such as photometric redshifts and stellar masses are derived through spectral energy distribution fitting methods. The results are used to study host galaxies of gravitational wave events and how light traces dark matter in galaxy clusters. Gravitational wave (GW) science, and particularly the electromagnetic follow up of these events, is transforming what had never been seen into a new astronomical field able to unveil the nature of cataclysmic events. Identifying the galaxies that host these events, and estimating their redshift, stellar mass, and star–formation rate, is crucial for cosmological analysis with gravitational waves, for follow up studies and to understand the formation of the binary systems that are thought to produce observable gravitational wave signals. This thesis describes how the host matching is implemented within the DES–GW pipeline and how observations of NGC 4993, the galaxy host of the event GW170817, provide important information about possible formation scenarios for binary neutron stars. In particular, we find that NGC 4993 presents shell structures and we relate their formation to the binary formation. The same galaxy properties are used to derive an observable mass proxy for galaxy clusters. I show that this mass observable correlates well with the total mass of clusters, which is mainly composed of dark matter. It can therefore be used for cosmological studies with galaxy clusters. The measurement of stellar–to–halo mass relations in clusters provides insights on the connection between the star content and the total matter content in clusters, and how this evolves over cosmic time.
The analysis presented on host galaxy of the gravitational wave event GW170817 brought evidence that formation mechanisms of the sources of such events differ from what was previously expected. This will have an impact on the theoretical models needed to explain these events. The methodology developed for electromagnetic follow ups and host galaxy analyses will be applied to future observations, and the science results from these studies will affect our current understanding of fields that span from cosmology to particle physics.

The extensive computational effort required for transient searches with photometric surveys and for photometric redshift (or galaxy properties) estimation, has been an important point of connection with the UCL Center for Doctoral Training (CDT) in Data Intensive Science. I have presented my work at various CDT events, and I hope that in the near future we will strengthen the collaboration between the DIS centre and DES analyses. More generally, developing and testing machine learning codes and methods to handle large datasets affects research inside and outside the world of academia.
I acknowledge William Hartley, for the support provided over the past two years, as mentor in galaxy evolution studies and research life. I am so thankful to my supervisor Ofer Lahav, for what he taught me over the years, while also leaving space for my own research interests, and for always understanding my problems. I acknowledge the DES Fermilab team and the URA visiting scholar award for allowing me to do research at Fermilab, broaden my research horizons and opening precious opportunities for my future. In particular, I am grateful to Marcelle Soares–Santos and James Annis for being the best hosts possible during my stay at Fermilab and for introducing me to the world of gravitational waves. I also thank the whole DES collaboration for providing an extremely stimulating environment for science, but also a relaxed and even often fun atmosphere. Each single DES collaboration meeting has been an extremely stressful moment in which I also clearly remembered how much passion I have for this work. I am extremely grateful to my family, my mum, dad and brother, for the support and help always provided, especially in the darkest moments. I acknowledge all my colleagues and fellow or former PhD students at UCL, Luisa Lucie-Smith, Felix Priestley, Guido Roberts-Borsani, Boris Leist- edt, Davide Gualdi, Ingo Waldmann, Nicola Baccichet, Marco Rocchetto, Daniela Saadeh, David Buckley, Paul Moseley, Stephanie Jouvel, David Johnson for making my everyday research life at UCL brighter. I acknowledge UCL for providing such a stimulating, bright and open-minded environment to work in. I acknowledge the UCL Women’s Volleyball team and the UCL Elite athlete programme, which gave me the honour to represent my university and compete at high level. I acknowledge my long-time friends Elisabetta Mutidieri, Francesca Ussia, Chiara Grillo, Debora Grillo, Isabella Cuoghi, Lewis Saccocci, Federica Ferretti for being always close even when we have been far away. I acknowledge
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“So remember, look at the stars and not at your feet.”

Stephen Hawking
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Chapter 1

Introduction

“The mind loves the unknown. It loves images whose meaning is unknown, since the meaning of the mind itself is unknown.”

René Magritte

In this introductory chapter, I present the main topics necessary to understand the contents and motivation of this thesis. I start from an introduction to cosmology in Section 1.1. Sections 1.2 and 1.3 introduce the main areas treated in my work, galaxy clusters and gravitational waves, with focus on topics which are relevant within the Dark Energy Survey (DES). DES and other galaxy surveys are described in Section 1.4.

1.1 Cosmology

The most accepted cosmological model nowadays is called the Friedmann-Robertson-Walker (FRW) Model, also known as the Standard Cosmological Model (SCM). In this model the geometry of the Universe is described by the Robertson-Walker (RW) metric, that can be derived assuming the Cosmological Principle, which says that “the Universe is homogeneous and isotropic on large scales”. This principle is observationally verified over the fraction of Universe that we can see, the Observable Universe, that corresponds more or less to the present Hubble Volume (a few Gpc$^3$). The transition towards homogeneity is indeed clear from the galaxy surveys on scales greater than a megaparsec, and in the
Cosmic Microwave Background (CMB) anisotropies (which are roughly only one part over $10^5$). Although the observational evidence does not imply either that the entire Universe has these features, or that the region of the Universe we live in will last in this state forever, we can affirm that it will conserve these properties at least for the time needed to cross it at the light velocity, the Hubble time, estimated around 10 Gyr. So, in order to understand the Observable Universe, we first begin by describing its overall background evolution as if it were isotropic and homogeneous, neglecting the inhomogeneities that we observe today on small scales.

Unless otherwise stated, quantities are expressed in units such that for the light velocity $c = 1$ in this Section. Further information about the Standard Cosmological Model might be found in Dodelson’s monograph (Dodelson 2003) or in Kolb & Turner (1991).

1.1.1 Robertson-Walker Metric

The isotropy and homogeneity assumptions imply that all the spatial coordinates evolve in time in the same way, and that in a metric $g_{\mu\nu}$ terms like $g_{0j}$ ($j = 1, 2, 3$) are zero. It can be then proven that the RW metric can be written in a general way as:

$$ds^2 = dt^2 + h_{ij}dx^i dx^j = dt^2 - a^2(t)dl^2,$$

(1.1)

where $a(t)$ is the scale factor that describes the Universe dynamics on large scales, $t$ is the proper time measured by an observer standing in the comoving reference frame (that means, in polar coordinates, $r, \theta, \phi = \text{constants}$), $h_{ij}$ is the metric tensor restricted to spatial coordinates (such that if $g_{\mu\nu}$ is the metric tensor, $h_{ij} = -g_{ij}, i, j = 1, 2, 3$), $dl^2$ is the spatial line element of a three-dimensional space with constant positive, negative or zero curvature. It can be proven that in spherical coordinates, $(r, \theta, \phi)$, the line element is described by:

$$ds^2 = dt^2 - a^2(t)\left\{\frac{dr^2}{1 - kr^2} + r^2d\theta^2 + r^2 \sin^2 \theta d\phi^2\right\},$$

(1.2)

where $k = 0, 1, -1$ for respectively zero, positive or negative curvature.
1.1.2 Redshift and Astrophysical distances

The motion of a free test-particle is described by the geodesic equation, which can be simplified in the RW metric to:

$$\frac{\dot{u}}{u} = -\frac{\dot{a}}{a},$$

(1.3)

where $u$ is the spatial velocity of the particle. This differential equation admits the solution $u \propto a^{-1}$, which has a fundamental consequence: if $m_0$ is the rest mass of the particle, its momentum $p = m_0u$ scales as $a^{-1}$, therefore it changes if the Universe expands or contracts. We can therefore apply this same reasoning for a particle following $ds = 0$, that is a particle with zero mass. So, for a photon of energy $\varepsilon$, if its wavelength is $\lambda$:

$$\varepsilon = p = \frac{2\pi}{\lambda} \propto a^{-1}.$$  

(1.4)

Hence if a photon is emitted from a source at time $t_{em}$ with wavelength $\lambda_{em}$, it will be observed at time $t_{oss}$ with a greater wavelength $\lambda_{oss}$ if the Universe is expanding (redshift), or with a smaller wavelength if it is contracting (blueshift); in fact:

$$1 + z \equiv \frac{\lambda_{oss}}{\lambda_{em}} = \frac{a(t_{oss})}{a(t_{em})},$$

(1.5)

where the redshift $z$ was introduced. In the same way, any proper length $l$ varies with the expansion or contraction of the space, and as a consequence the only physical, measurable length becomes $a(t)l$. This fact led astrophysicists to a redefinition of distances.

The fundamental distance measure, the one from which all other distances can be computed, is that in the comoving reference frame. An important comoving distance is that between a distant photon emitter and us:

$$\chi(a) = \int_{t(a)}^{t_0} \frac{dt'}{a(t')}.$$  

(1.6)

On the other hand, the proper distance, the length of the spatial geodesic between two points, is:

$$d_p = a(t)\chi,$$

(1.7)

$^1t_0$ refers to the present time.
where $\chi$ is the radial comoving distance.

Moreover, the luminosity distance $d_L$ is defined as:

$$
d^2_L \equiv \frac{L}{4\pi \mathcal{F}},
$$

where $\mathcal{F}$ is the energy measured per unit time and area, and $L$ is the luminosity (energy per unit time). Supposing that the emitted radiation propagates isotropically in space, from the definition it is clear that $d_L$ would be the distance to the source if there were no expansion of the space. On the other hand, in case of expansion, light emitted from a position at $\chi$ in the comoving reference frame arrives at our position, which we choose to be at $\chi = 0$, crossing an area of $4\pi a_0^2 \chi^2 = 4\pi \chi^2$. Moreover, its photons will lose a factor $(1 + z)^2$ of their energy, of which $(1 + z)$ comes from the greater distance travelled, and the other $(1 + z)$ from the growing of the proper wavelength. Consequently from energy conservation:

$$
\mathcal{F} = \frac{L}{4\pi \chi^2 (1 + z)^2} \implies d_L = \chi (1 + z) = \frac{\chi}{a}.
$$

A classic way to measure distances in astronomy is through the angle $\vartheta$ subtended by an object of physical length $l$. The angular diameter distance is then defined as:

$$
d_A \equiv \frac{l}{\vartheta} = d_L/(1 + z)^2,
$$

which we have also expressed in terms of the luminosity distance, and has an explicit expression that depends on the curvature of the Universe.

### 1.1.3 Hubble Law

The Hubble Law describes, to a first approximation, the relative recession of galaxies, and it can be analytically derived by considering galaxies as travelling along geodesics in a RW metric. Expanding $a(t)$ in a Taylor series around the present time (which means obtaining the Hubble Law for a time around ours, or rather for Universe regions close enough to us):

$$
a(t) = \frac{1}{a_0} = 1 + H_0(t - t_0) - \frac{1}{2} a_0 H_0^2 (t - t_0)^2 + ..., \tag{1.11}
$$

It is usual to take $a_0 = 1$. 

\footnote{It is usual to take $a_0 = 1$.}
where the subscript 0 indicates the quantities evaluated at present time. Defining the Hubble Parameter \( H(t) = \frac{a'(t)}{a(t)} \), the Hubble Parameter at present time, called the Hubble constant, is:

\[
H_0 \equiv \frac{a_0'}{a_0}, \quad (1.12)
\]

and the deceleration parameter

\[
q_0 \equiv -\frac{a_0''}{a_0^2} = -\frac{\ddot{a}}{aH_0^2}. \quad (1.13)
\]

Another useful definition is the Hubble length \( L_H \equiv H(t)^{-1} \), that approximatively represents the distance that a photon can travel in a Hubble time \( H^{-1} \), and it is the scale that has to be compared to the characteristic length of any physical process in order to understand whether such a process might cause cosmologically relevant effects or not. One can similarly compare the characteristic time \( \tau \) of a reaction to \( H^{-1} \), i.e. a process needs to be faster than expansion in order to be able to maintain the equilibrium. Comparing \( H \) with the reaction rate \( \Gamma \) is often preferred.

At small distances, eq. (1.9) becomes the Hubble Law:\[4\]

\[
H_0 d_L = z + \frac{1}{2}(1-q_0)z^2 + ... \quad (1.14)
\]

It is worth stressing that the luminosity distance is not necessary in order to obtain the Hubble Law, but for the close distances that we are considering in this approximation, the proper distance \( d = a(t)\chi \) works as well. Eq. (1.14) is however useful when Standard Candles are observed, because \( d_L \) is the observable in such case.

Note that the approximations used imply that for galaxies not satisfying \( z \ll 1 \), the relationship between \( d_L \) and \( z \) differs from the Hubble law, in a way that depends on the cosmological model: we need a solution \( a(t) \) from Einstein’s equations in order to obtain an exact expression of \( r \). Einstein’s equations are treated in the next section.

---

\[3\]Note that units with \( c = 1 \) are used.

\[4\]Interpreting the redshift \( z \) as a Doppler effect, obtaining the Hubble Law in the classical form \( v = H_0 d \) is straightforward.
1.1.4 Dynamics of the Universe

In order to obtain an expression for $a(t)$, let us write the Einstein equations:

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = G_{\mu\nu}$$  \hspace{1cm} (1.15)

$$= 8\pi GT_{\mu\nu} + \Lambda g_{\mu\nu}.$$  \hspace{1cm} (1.16)

where $G_{\mu\nu}$ is the Einstein tensor, $T_{\mu\nu}$ is the stress-energy tensor, $\Lambda$ is the cosmological constant.

For a perfect fluid in a space that satisfies the cosmological principle, $T_{\mu\nu}$ has a particular form, since homogeneity, isotropy and the absence of viscosity impose zero off-diagonal components and equal diagonal elements for the space components. If $\rho$ is the energy density of the fluid and $P$ its pressure:

$$T_{\mu\nu} = \text{diag}(\rho, -P, -P, -P).$$  \hspace{1cm} (1.17)

The Friedmann equation is the $\mu = \nu = 0$ equation of Einstein’s equations, that in a RW metric becomes:

$$\frac{\dot{a}^2}{a^2} + \frac{k}{a^2} = \frac{8\pi G}{3} \rho,$$  \hspace{1cm} (1.18)

while the acceleration equation can be written as:

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho + 3P).$$  \hspace{1cm} (1.19)

If today there is expansion ($\dot{a} \geq 0$), and if $\rho + 3P > 0$ has always held, as expected by the Standard Cosmological Model, this equation tells us that $\dot{a}$ has always been negative, implying that there must have been a certain time in the past when $a = 0$. That time, when the Universe was concentrated in a singularity, is often chosen as the “zero-time”.

According to the SCM, the Universe has not always evolved in the same way. In fact, from the energy conservation ($T^{0\nu} = 0$) the first law of Thermodynamics can be derived:

$$d(\rho a^3) = -Pd(a^3).$$  \hspace{1cm} (1.20)

Substituting the equation of state $P = w\rho$, it becomes $\rho \propto a^{-3(1+w)}$, with $w$ being
1.1. Cosmology

redshift–dependent in general. In the particular cases in which the universe is dominated by:

- Radiation: \( w = \frac{1}{3} \Rightarrow \rho \propto a^{-4} \);
- Matter: \( w = 0 \Rightarrow \rho \propto a^{-3} \);
- Cosmological Constant: \( w = -1 \Rightarrow \rho \propto \text{constant} \).

In the first moments of its life, the Universe had \( a \ll 1 \), so it was radiation dominated; later the equivalence was reached at a certain \( a_{\text{eq}} \) such that radiation and matter densities were equal, and eventually it was dominated by matter. It is useful to write the Friedmann equation introducing some new parameters:

\[
\frac{k}{H^2a^2} = \Omega - 1, \tag{1.21}
\]

where \( \Omega \equiv \frac{\rho}{\rho_c} \) is the density parameter, and \( \rho_c \equiv \frac{3H^2}{8\pi G} \) is the critical density, and represents the density at which the Universe would be flat. Important consequences might be deduced:

- \( k = +1 \Rightarrow \Omega > 1 \) and the Universe is closed;
- \( k = 0 \Rightarrow \Omega = 1 \) and the Universe is flat;
- \( k = -1 \Rightarrow \Omega < 1 \) and the Universe is open.

Note that in this version of the Friedmann equation, \( H, a \) and \( \Omega \) vary with time.

From eq. (1.18) and eq. (1.19) one can derive the equation for the deceleration parameter in this cosmological model:

\[
q_0 = \frac{\Omega_0}{2} (1 + 3w). \tag{1.22}
\]

Therefore the acceleration depends on how much matter is contained in the Universe, and is always negative for matter dominated (MD) and radiation dominated (RD) Universes.

We now want to understand how \( a \) evolves with time. For a fluid with \( P = w\rho \), we know that \( \rho \propto a^{-3(1+w)} \), so from the Friedmann equation in a flat space:

\[
a \propto t^{2/3(1+w)}, \tag{1.23}
\]
as a consequence:

- \( \text{MD} \Rightarrow a \propto t^{2/3}; \)
- \( \text{RD} \Rightarrow a \propto t^{1/2}; \)
- \( \Lambda D \) (Cosmological-constant dominated) \( \Rightarrow a \propto \exp(H_*t) \) (where \( H_* \) is the Hubble parameter, constant in this case).

Luminosity and angular distances are larger in a Universe with a cosmological constant than in one without it. In fact, the energy density and the expansion rate are smaller in the earlier epochs of a \( \Lambda \) dominated Universe, and photons had more time to travel from distant objects to us. This is why those objects appear fainter than they would be in a matter dominated Universe.

### 1.1.5 Universe components

The principal components of the Standard Cosmological Model are:

1. Matter: dark matter, baryons (ordinary matter), neutrinos (in non-relativistic regime)
2. Radiation: photons (mainly CMB), neutrinos (in relativistic regime)
3. Dark Energy.

Dark Energy (DE) and Dark Matter (DM) are two phenomenological solutions to effects that cannot be explained with known physics, namely the accelerated expansion of the Universe and the problem of the missing matter. Non standard theories that try to explain these effects using alternative solutions (e.g. modifying Einstein’s equations, Bekenstein 2010, see Caldwell & Kamionkowski 2009 for a review) may not include one or both of these components in their cosmologies.

#### Photons

Today, the largest contribution to the mean number density of photons in the universe comes from the Cosmic Microwave Background. The existence of this relic radiation was for the first time predicted by Gamow (1948), as a direct consequence of the *Hot Big Bang theory*. In fact, if the universe is today expanding and cooling, in the past it must have been very dense and hot. Therefore, there must have been a time when all the ordinary matter in the Universe was in the form of a completely ionized plasma. In such a medium, the
1.1. Cosmology

Photons were interacting continuously with free electrons through Thompson scattering, and their mean free path was much smaller than the current dimension of the Universe. Thus, photons from this epoch cannot be observed today. As the Universe expanded and cooled, protons recombined with electrons first in Helium atoms, and then in neutral Hydrogen. Due to the decrease of free electrons in the medium, photons scattered with the last electron they encountered and then they were free to propagate through the Universe. This decoupling between photons and ordinary matter happens at redshifts $z \simeq 1100$ and defines the so-called last scattering surface, i.e. the ensemble of points where the last scattering of each CMB photon happens. Today these photons are observed to form an almost isotropic photon background, that was first detected by the Nobel Prize winners Arno Penzias and Robert Wilson in 1964.

In the last 20 years several experiments were aimed at studying CMB properties, confirming with impressive precision that the CMB has a black body spectrum. Its temperature today is well measured to be $T_0 = 2.7255 \pm 0.0006$ K (Fixsen 2009). Moreover in 1992 the COBE satellite revealed that the CMB presents small temperature anisotropies at a level of $\Delta T/T \sim 10^{-5}$. These anisotropies are the product of physical processes that mainly happened before decoupling and are originated by the same initial conditions that seeded the inhomogeneities that we observe today in the matter distribution.

It is useful to have all the energy densities of the different components in the same units, hence we divide them by the critical density at the present epoch. It can be shown that the density parameter for the photons is (e.g. Dodelson 2003):

$$\Omega_\gamma(a) = \frac{\rho_\gamma}{\rho_c} = \frac{2.47 \times 10^{-5}}{h^2 a^4},$$

where $h = H_0/100$ is the reduced Hubble constant. Note that eq. (1.24) has no spatial dependence, but the small perturbations around the zero-order distribution function used do have a spatial dependence, and describe the CMB anisotropies.

Matter

Two types of matter are considered by the SCM: baryons, i.e. ordinary matter such as protons, neutrons and (improperly) electrons, and dark matter, which is currently only observable through the gravitational effects it generates. Both baryons and dark matter present large inhomogeneities in their density distributions due to the formation of
gravitationally bound structures, so their densities have to be measured through different methods, instead of computing them from the gas temperature (as for photons). Also the abundance of these two components is usually indicated through their density parameters today $\Omega_b$ and $\Omega_{dm}$:

$$\frac{\rho_b}{\rho_c} = \Omega_b a^{-3}, \quad \frac{\rho_{dm}}{\rho_c} = \Omega_{dm} a^{-3}.$$  \hspace{1cm} (1.25)

**Baryons**

There are different observational methods used to determine the amount of baryons in the universe; some of them are:

- Estimation of the luminous matter in stars, galaxies and clusters of galaxies at different wavelengths (see e.g. Fukugita et al. 1998);

- Observation of the Lyman-$\alpha$ forest, which consists of absorption lines arising in the spectra of far quasars. The depth of the hydrogen absorption lines are an indicator of the amount of gas that quasar light travelled through (Rauch 1998);

- Observation of the temperature anisotropies of the CMB, that are affected by the amount of baryons in the Universe (see e.g. Challinor 2013 for a review);

- Observation of the amount of isotopes of light elements such as Deuterium, Helium and Lithium in extragalactic metal poor regions and comparison with primordial nucleosynthesis predictions (Steigman et al. 2007).

The angular power spectrum of the CMB and the relative abundances of primordial hydrogen, deuterium and helium isotopes are compatible and indicate that $\sim 4.6\%$ (Planck Collaboration et al. 2016b) of the current mass density of the Universe consists of baryons. However, only a small fraction of these baryons can be accounted for in stars and gas inside galaxies, galaxy groups and galaxy clusters, and in spectral-line absorbing gas in the intergalactic medium (IGM). In particular 6% of baryons is found in stars in galaxies, 1.7% in the cold gas in galaxies and 4% is the gas in clusters of galaxies and groups (Fukugita & Peebles 2004). Lyman-$\alpha$ observations (Shull et al. 2012) find that the Lyman-alpha absorbing material can account for a large fraction of the baryon content, but $\sim 30\%$ of it is missing. This issue is known as the *Missing baryons problem*. It is argued that the remaining baryons are in the form of shock-heated gas in a cosmic web between clusters of
1.1. Cosmology

galaxies. This so-called Warm Hot Intergalactic Medium (WHIM) has a temperature in the $10^5 - 10^7$ K range, but it is hard to detect with current observations because of its low density (Cen & Ostriker 2006). Tanimura et al. (2017) have recently claimed that they provide the first detection of this filamentary gas. However, further studies are necessary and this issue remains a matter of present research.

Dark Matter

Dark matter accounts for $\sim 25\%$ of the total density ($\Omega_c h^2 = 0.1186 \pm 0.0020$; Planck Collaboration et al. 2016b). However, the nature of dark matter is today unknown. Zwicky (1933) first found that the velocity dispersion of galaxies in the Coma cluster of galaxies was too large to be supported by only luminous matter. In the 1970s, Vera Rubin and collaborators (e.g. Rubin & Ford 1970) measured the extended rotation curves of spiral galaxies and found that they were flat. The observed rotational speed of objects in the outer regions of galaxies is much larger than the one expected by simply equating the centrifugal to the gravitational force due to observable matter. This is attributed to the presence of a large halo of dark matter much more extended than the distribution of luminous matter. This and other classic evidences for non-luminous matter has now been supplemented with a number of recent probes such as:

- Weak and strong lensing. We shall see these how this probe can infer the presence of dark matter throughout this work.

- The Bullet Cluster. In this cluster, a collision between two galaxy clusters appears to have caused a separation of dark matter and baryonic matter (Markevitch et al. 2002). X-ray observations show that a lot of the baryonic matter in the system is concentrated in the centre. Electromagnetic interactions between passing gas particles caused them to slow down and settle near the point of impact. However, weak gravitational lensing observations of the same system show that much of the mass resides outside of the central region of baryonic gas. Because dark matter does not interact through electromagnetic forces, it would not have been slowed in the same way as the X-ray visible gas, so the dark matter components of the two clusters passed through each other without slowing down substantially. This accounts for the separation between dark matter and baryons. Other system like the Bullet Cluster have been discovered (Mahdavi et al. 2007).
• Supernovae. The luminosity distance of this kind of standard candles depends on the cosmological parameters, and thus also on the dark matter content of the Universe.

• The CMB, as its anisotropies depend on cosmological parameters.

Dark matter is usually classified as Hot, Warm or Cold Dark Matter (respectively HDM, WDM and CDM), depending on when it decoupled from the rest of the cosmic plasma. If a DM species decoupled before becoming non-relativistic is called Hot Dark Matter, if it decoupled when it was already non-relativistic is classified as Cold Dark Matter. Warm Dark Matter became non-relativistic at a $a_{\text{NR}}$ which is very close to that of decoupling $a_D$. We expect that a certain species becomes non-relativistic depending on its mass: the less the mass, the greater the $a_{\text{NR}}$. Today, amongst the best candidates for the HDM we find the massive neutrinos ($m_\nu \approx 10^{-30}$ eV), while gravitinos and neutralinos ($m \approx 100$ GeV) are two possible species of CDM. Relativistic species such as photons are not able to contribute substantially to structure formation, therefore we will need a CDM model.

Neutrinos

In the SCM, a neutrino background is expected and the density is estimated from CMB measurements to be:

$$\Omega_\nu = \frac{\rho_\nu(t_0)}{\rho_c} = \frac{1.68 \times 10^{-5}}{h^2},$$

(1.26)

where neutrinos are assumed as massless. It is now known however from neutrino oscillation experiments that neutrinos are massive. Neutrinos can be considered as relativistic as far as their kinetic energy is much larger than their rest mass energy. Whenever the non-relativistic regime applies, the energy density of massive neutrinos is:

$$\Omega_\nu = \sum_i \frac{m_\nu^i}{92.5h^2eV},$$

(1.27)

where the sum is done over the three neutrino generations.

The best upper limit on the sum of neutrino masses comes from the CMB, and it is estimated to be $\sum m_\nu < 0.23$ eV (Planck Collaboration et al. 2016b) If neutrinos have mass, they could account for part of the Dark Matter density. Nevertheless structure formation theories and observations suggest that this fraction must be small. In fact,
neutrinos are relativistic or semi-relativistic for most of the history of the universe (that means that they are a kind of HDM). Therefore, due to their velocity, they are unlikely to collapse in small gravitationally bound structures.

**Dark Energy**

In 1917 Albert Einstein realized that, in order to have a static Universe, as believed before cosmic expansion was observed, he could introduce a constant $\Lambda$ into his equations. A cosmological constant, intended as a component with constant energy density, is able to counteract the attractive effect of gravity because in General Relativity the normalization of energy is not arbitrary as in classical, non-gravitational physics, and the actual value of the energy density has a role in the dynamics. If the effect of adding in a constant energy density has to be insensitive to the choice of coordinates, then it can be shown that $P_\Lambda = -\rho_\Lambda$, i.e. $w_\Lambda = -1$ in the equation of state. $\Lambda$ might be considered as a new mathematical degree of freedom, including it in the purely geometrical, left-hand side of Einstein’s equations:

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi GT_{\mu\nu}, \quad (1.28)$$

or as a new component of the Universe with $\rho_\Lambda = \Lambda/(8\pi G)$, as included in the right-hand side of Einstein’s equations:

$$G_{\mu\nu} = 8\pi G(T_{\mu\nu} - \rho_\Lambda g_{\mu\nu}). \quad (1.29)$$

Both of these interpretations are mathematically and dynamically equivalent. The effect of this new component is that an accelerated expansion is allowed in Einstein’s equations if $\Lambda$ dominates.

When Hubble proved the Universe’s expansion, the need for this constant seemed to disappear, until in 1998 supernovae studies (Riess et al. 1998; Perlmutter et al. 1999) revealed that the universe is accelerating, and this can be accomplished if the equation of state parameter of the dominant component satisfies $w < -1/3$. The cosmological constant is one of the simplest candidates for Dark Energy and is consistent with several cosmological probes, such as supernovae, CMB and Baryonic Acoustic Oscillations (BAO). However, the introduction of a cosmological constant gives rise to some theoretical problems:
• Fine-tuning problem: if we consider $\Lambda$ originating in the vacuum energy, why is it much smaller than the value estimated by the Standard Model (or any other particle model)?

• Coincidence problem: why does its density have the same order of magnitude of the matter energy density at present?

Moreover, a physical meaning for this puzzling cosmological constant term has still to be found. Several alternative theories with different equations of state have been developed, and they can be divided into two main classes: physical Dark Energy models, that attribute the energy density to a new physical field, and geometrical Dark Energy models, or modified gravity models, for which gravity is not described by General Relativity, and the acceleration is simply an effect of this modification (see Silvestri & Trodden 2009 for a review). Distinguishing between these two kind of models is impossible using only background observations (or rather, probes of cosmic expansion history), since the equation of state is the same, but a study of structure formation might be relevant to solve this problem.

The most widely used parametrization for the dark energy equation of state, useful for constraining the non-standard cosmological models with a time-dependent $w$, makes use of a Taylor series in the scale factor:

$$w(a) = w_0 + (1 - a)w_a.$$  \hspace{1cm} (1.30)

### 1.1.6 The perturbed Universe

The Universe we observe today is far from being homogeneous and isotropic on scales smaller than the Hubble length. The standard scenario for structure formation (galaxies, clusters, voids, etc.) is based on several key points:

• The CDM is the dominant component in the evolution of perturbations, and the DE contributes only on a global level.

• Baryonic matter has an abundance given by the nucleosynthesis and only a small fraction is in bound structures.

• Inflation (Guth 1981; Linde 1982) is a theory that posits a period of exponential expansion of the Universe during its early stages. It is responsible for the production
of the first inhomogeneities, and predicts adiabatic and Gaussian perturbations.

- Gravitational instability is the phenomenon that guides the growth of such perturbations: over-dense regions where gravity is stronger than the background expansion can become denser and denser. The so-called DM halos can then form in the most overdense regions, followed by the cosmological structures we observe today through a hierarchical formation (i.e. smaller structures form first).

In this picture, galaxies form within the DM halos, and have physical properties determined by the halos in which they live. See Cooray & Sheth 2002 for a review on the halo model. Perturbations are usually defined in terms of the density contrast \( \delta = \delta \rho / \bar{\rho} \), where \( \bar{\rho} \) is the average background density, and \( \delta \rho \) is the difference between the overdensity and \( \bar{\rho} \). Assuming that galaxies trace DM, the galaxy density contrast is related to the matter density contrast \( \delta_M \) through a bias factor \( b: \delta_g = b\delta_M \). These quantities are often studied through their Power spectrum \( P(k) \), defined in Fourier space.

### 1.1.7 Cosmological parameters

In the previous sections, we have introduced some of the basic set of cosmological parameters, listed in Table 1.1, where all the densities and the Hubble constant are considered at present. The new parameter \( \tau \), the optical depth to scattering, is the probability that a photon scatters once, and it is important for a description of the CMB anisotropies alterations due to the scatterings between electrons and CMB photons. In fact, the low-redshift Universe is known to be highly ionized. Moreover \( r \) is the tensor–to–scalar ratio, given by the amplitude of tensor over scalar perturbations, and \( n_s \) is the spectral index of density perturbations, defined from the initial power spectrum of density fluctuations.

Models based on these eleven parameters are able to give a good fit to the data available up to now, but not all of them are used in the cosmological models most accepted today. This happens for the \( \Lambda \)CDM model, which requires only six of the base parameters (plus the bias). The \( \Lambda \)CDM model is based on a spatially flat, expanding Universe governed by General Relativity as described in this chapter, and whose principal components are CDM and a cosmological constant for times close to present. These assumptions, consistent with observations, allow us to neglect spatial curvature \( (\Omega_k = 0) \), therefore all the other components’ density parameters must sum to one, and one of them can be regarded as a dependent parameter. The neutrino density is usually eliminated. Moreover, if
Table 1.1: List of cosmological parameters. The top block contains the basic set, the lower blocks list respectively some additional parameters, and some derived parameters. We report the latest Planck results (Planck Collaboration et al. 2016b) for a ΛCDM model from primary CMB data, including polarization at low multipoles, plus CMB lensing measurements. Uncertainties are 68% confidence level.

Note that density parameters are usually given as physical densities \( \omega_X \equiv \Omega_X h^2 \), for a general \( X \) component. Other additional parameters are also listed in Table 1.1.

Derived parameters are often used in place of those in the top block of Table 1.1. For example, in a model that allows curvature values different from zero, spatial curvature can only standard neutrino interactions are considered, we saw how relativistic neutrinos and photon energy densities can be related. There is no observational evidence for tensor perturbations, so the tensor–to–scalar ratio \( r \) can be set to zero. There are only six parameters to be studied, and they consist in the smallest set that can be consistently used with present observations. Despite its simplicity, this model is successful in describing many cosmological probes, which we shall discuss below.
be obtained from the other parameters through

\[\sum_i \Omega_i + \Omega_\Lambda - 1 = \frac{k}{a^2 H^2},\]  

(1.31)

and the total present matter density \(\Omega_m\) might be used instead of the CDM density through

\[\Omega_m = \Omega_b + \Omega_c.\]

In linear perturbation theory, one can define the rms fluctuation in the total matter in \(r = 8 h^{-1}\) Mpc spheres at \(z = 0\) as \(\sigma_8\), which is often used instead of the initial amplitude \(A_s\) of the power spectrum of density fluctuations. Introducing derived parameters might seem redundant, but different types of observations are more easily studied in terms of different parameters. For further information on cosmological parameters, see the review by Lahav & Liddle (2017).

1.1.8 Observational probes

Cosmological parameters can be estimated through a variety of methods. Amongst them, studies of CMB anisotropies have played a central role over the last decades, and they represent a unique, high–redshift probe to complement lower redshift methods. The state of the art of this measurement is given by Planck (Planck Collaboration et al. 2016a), as presented in Planck Collaboration et al. (2016b). Here we briefly review probes that are relevant to the Dark Energy Survey.

*Type Ia Supernovae (SN)*: Type-Ia Supernovae are transients produced by the thermonuclear explosion of white dwarfs. They are used to measure distances as the spectral properties, absolute magnitudes, and light curve shapes of the majority of SNe Ia are remarkably homogeneous. Thus, by measuring the observed light curve of a supernova and comparing it to a reference light curve at known distance, one can infer the luminosity distance of the supernova. The application of these methods to studies of high-redshift supernovae provided the first direct evidence of the accelerating expansion of the Universe (Riess et al. 1998; Perlmutter et al. 1999). Quantitatively speaking, we know that the luminosity distance is \(d_L = (1 + z)\chi(z)\), where \(\chi(z)\) is the comoving distance given by (in a flat Universe):

\[\chi(z) = \int_0^z \frac{dz'}{H(z')}\]  

(1.32)
Therefore by measuring the luminosity distance of Supernovae, one can infer dark energy properties and the matter density $\Omega_m$ through the evolution of the Hubble parameter. In fact, in a flat CDM Universe:

$$H^2(z) = H_0^2 \left[ \Omega_m (1 + z)^3 + \Omega_{DE} e^{3 \int_0^z dz' [1 + w(z')]} \right].$$

(1.33)

Recently, Betoule et al. (2014) measured $\Omega_m = 0.295 \pm 0.034$ from 740 spectroscopically confirmed SNe Ia for a flat $\Lambda$CDM model, consistent with estimates from CMB experiments. Most SNe experiments to date are consistent with $w = -1$, while future results from DES and other surveys aim at constraining also the redshift evolution of the DE equation of state.

Galaxy clustering: The distribution of dark matter can be probed by the galaxy distribution, provided that a bias is introduced to link matter and galaxy power spectra. The matter power spectrum is mostly sensitive to the primordial power spectrum and to $\Omega_m h$. If spectroscopic redshifts are not available, as in DES, it is preferable to work with the angular correlation function within redshift shells. Because of the effect of baryonic matter, the matter power spectrum is different from the dark matter one. Baryons are strictly coupled to photons before decoupling and they oscillate before decoupling. The characteristic scale of these oscillations (the Baryon Acoustic Oscillations, BAOs) is imprinted in both the matter power spectrum at decoupling, giving rise to a preferential scale called the acoustic peak in the spatial distribution of galaxies, and in the CMB temperature anisotropies. Both these characteristic scales have been detected in observations and are used as standard rulers\(^5\) to investigate the history and the accelerated expansion of the Universe. The first detections of BAOs were made by Eisenstein et al. (2005) and Cole et al. (2005).

Weak gravitational lensing: The matter distribution between an observer and a distant source galaxy has the effect of bending the light coming from the galaxy and shears its shape. The shear produced by small density perturbations is “weak”, thus the name “weak lensing”. It also follows that the effect is so small that a statistical analysis is needed. A measurement of the shear signal for source galaxies binned in redshift probes the distribution of matter along the line of sight, and it is thus a probe of the history of structure growth. The signal mainly depends on $\sigma_8 \Omega_m^\alpha$ (with $\alpha \simeq 0.3 - 0.5$). For a review

\(^5\)Note that in this case we are dealing with statistical standard rulers, in the sense that they are related to a statistical length as a property of spatial distributions.
1.2. Galaxy clusters

Galaxy clusters are described in more detail in the next Section.

1.2 Galaxy clusters

Galaxy clusters are the largest gravitationally collapsed structures in the Universe. As such, they represent unique laboratories to probe the peaks of the large scale matter density. They also represent a peculiar environment where the existence of baryonic matter under different phases, hot and cold, following both the gravitational potential of the main halo and of the subhalos complicates the understanding of their structure and evolution over cosmic time. The multicomponent nature, however, is an interesting aspect of clusters, offering several observable signals over the whole electromagnetic spectrum. It is thanks to these features that clusters provide both observables for cosmology and insights into astrophysical processes, such as the formation and evolution of galaxies, AGN (Active Galactic Nuclei) feedback, and the effects of dark matter over these structures. Given the interplay of cosmology and astrophysics, we must attempt to understand both in order to perform cosmological analyses. See Biviano 2000 for a review on galaxy clusters.

1.2.1 Galaxy clusters as a cosmological probe

The formation of structures is driven by the gravitational instability of initial perturbations in a dynamically evolving space–time. When observing structures at the present epoch, we therefore expect to find the traces of three elements: primordial fluctuations, gravitational collapse and dynamics of the background spacetime. The formation of large potential wells, the seeds of the clusters, are mainly due to the DM dynamics, so galaxy clusters provide an excellent tool to probe DM fluctuations and properties.

A measurement of cluster abundance is a very powerful probe for cosmology. The quantity of interest here is the cluster redshift distribution $d^2N(z)/(dzd\Omega)$, given by the product between the comoving density of detected clusters $n_{\text{com}}$ and the comoving volume per unit redshift and solid angle $d^2V/(dzd\Omega)$ (e.g. The Dark Energy Survey Collaboration 2005).\(^6\)

$$
\frac{d^2N(z)}{dzd\Omega} = \frac{d^2V(z)}{dzd\Omega} n_{\text{com}}(z) = \frac{c}{H(z)} d_A^2 (1+z)^2 \int_0^\infty dM f(M, z) \frac{dn(M, z)}{dM},
$$

\(^6\)Let us put the speed of light back into the equations now that we are not dealing with pure GR anymore.
where $d_A$ is the angular diameter distance, $f(M, z)$ is the redshift-dependent mass selection function of the survey, and $dn/dM$ is the cluster mass function, which has to be compared with theoretical predictions. One of the most accepted models for predicting the abundance of clusters is the extended Press-Schechter model (see e.g. Hiotelis 2003), which includes the so-called excursion sets model and the merging history of halos into the more traditional Press-Schechter model (Press & Schechter 1974). Broadly speaking, given an underlying cosmological model and an initial spectrum for perturbations, more accurate (compared to the Press-Schechter model) analytical (Sheth & Tormen 2002) and numerical (e.g. Jenkins et al. 2001) models have been developed.

Eq. (1.34) shows that a galaxy cluster abundance measurement depends on the cosmological parameters through the following:

- the volume per unit solid angle and redshift;
- the evolution of cluster abundance $\frac{dn(M, z)}{dM}$, which strongly depends on the growth rate of structures (that is in turn dependent on the expansion rate $H(z)$ and thus on cosmological parameters);
- the Hubble parameter $H(z)$;
- the mass selection function. In fact, masses are determined through an observable related to the cluster’s mass, namely X-ray temperatures, the Sunyaev-Zel’dovich effect, the richness or weak lensing. These quantities may be available only for some specific subsets of the overall cluster population (e.g. only the most massive clusters), and they may depend on the cosmology.

One of the most challenging aspects of cluster cosmology consists in deriving the relation between the halo mass $M$ from the theory, that appears in Eq. (1.34), to the mass observable $O$ of our survey. Such relation is usually called a scaling relation, and was first introduced in Kaiser (1986). In general, this will not be a one–to–one relation, because single objects’ mass observables are affected by baryonic physics, different formation histories and observational limitations. Therefore, scaling relations are usually modeled in the form of a probability distribution function $p(M|O)$. A good mass observable should be relatively easy to measure and tightly correlated with halo mass. Commonly used mass proxies are different depending on the wavelengths observed:

\footnote{Note again the degeneracy between the astrophysics of the system and the cosmology.}
1.2. Galaxy clusters

- **X-ray**: temperatures or luminosities (e.g. Shimizu et al. 2003; Zhang et al. 2007). Even though most of the baryonic matter is in the form of diffuse gas, it is not usually trivial to observe it. However, the diffuse intra–cluster matter (ICM) in galaxy clusters can reach temperatures high enough ($10^7 - 10^8$ K) to be observable in the X-ray. Under the assumption of hydrostatic equilibrium, the total mass of a cluster can be derived from measurements of the ICM temperature and density (e.g. Sarazin 1988).

- **Optical–NIR**: luminosities or richness (e.g. Rozo et al. 2009b; Andreon 2012). These wavelengths are dominated by starlight, mostly from old elliptical galaxies. The luminosity or the counts of these galaxies (the richness) within some aperture are often used as mass proxies. Despite the fact that the mass observed through galaxies’ luminosity is only a small fraction (~ 1%) of the total cluster mass, galaxies do trace well the underlying dark matter distribution, as expected within the standard scenario of structure formation described in this Chapter. In particular, we shall see in Chapters 4 and 5 how stellar mass is able to trace dark matter.

- **Microwaves**: Sunyaev–Zel’dovich (Sunyaev & Zeldovich 1972) observables (see Carlstrom et al. 2002). The CMB photons traveling through a galaxy cluster interact with the hot ICM and undergo inverse Compton scattering. This results in a shift of the contribution of the photons to the CMB towards higher energies in the direction of the cluster, in a way that depends on the density of the ICM.

The stacked weak lensing signal arising from galaxy clusters also probes the total mass in clusters, without assumptions on its dynamical state, and has proven to be an effective method to calibrate scaling relations (e.g. Johnston et al. 2007; Rozo et al. 2009a), and we shall see in Chapter 5 how this method has been successfully applied to the mass observable presented in this thesis. Note that the DES data can be used to simultaneously constrain cosmological parameters from cluster abundance and the mass proxy–total mass relation from weak lensing. This has previously been done in X-ray studies (Mantz et al. 2010) and will be done with DES clusters in the near future.

Recent cosmological results for $ΛCDM$ models from X-ray clusters are $Ω_m = 0.23±0.04$ and $σ_8 = 0.82 ± 0.05$ (from Mantz et al. 2010) and $Ω_m = 0.27 ± 0.04$ (similarly in a CDM model where the DE equation of state is allowed to differ from that of a cosmological constant, with $w = −0.98 ± 0.26$) from Mantz et al. (2014). Optical studies (Rozo et al.
2010) estimate $\Omega_m = 0.28 \pm 0.07$ and $\sigma_8 = 0.80 \pm 0.07$.

It is remarkable that results coming from different datasets, with completely different systematics involved, still provide similar results. For a review on cosmological parameters estimation from galaxy clusters see Allen et al. (2011).

1.2.2 Clusters and galaxy evolution

We have discussed how clusters are observable over a wide range of wavelengths, and an optical survey such as DES can mostly capture the stellar component. In the next Chapters, we will focus on deriving stellar masses for galaxies, and show that they can be robustly estimated with DES data. However, clusters show the presence of additional diffuse stellar content: the intra–cluster light (ICL). This component may contribute to 10–40% of the total cluster stellar mass (e.g. Zibetti et al. 2005; Gonzalez et al. 2005), and it is therefore a key player in determining the total cluster stellar mass fraction. The diffuse nature of this component in the crowded core of clusters, makes measurements of ICL properties extremely challenging. Zibetti et al. (2005) have overcome this problem through stacking methods of SDSS clusters. The available data from DES is already deeper than SDSS, and it will be able to probe even fainter levels by its completion. This makes DES a promising survey to detect the ICL and measure its properties over a broader redshift range. We will discuss the detection of ICL with DES is Chapter 6.

In Section 1.1.5 we have shown the importance of estimating the stellar and more generally the baryon content of the Universe, and how that is still a matter of debate. It is therefore interesting to combine DES with other surveys, such as X-ray, to estimate the total content of baryons. Chiu et al. (2017) have done this analysis using a subset of 91 DES clusters from Year 1 data. They found that the fraction of baryons (in terms of the total mass) in clusters with mean mass and redshift from their sample is $f_b = (12.8 \pm 0.25 \pm 1.28)\%$, and this changes very little over the past $\sim 9$ Gyr. They claim that their results are a direct indication of the presence of the “missing baryons”: if those baryons were not present outside clusters at the expected densities, it would have not been possible to explain how the scaling relations they found could vary steeply with mass and stay roughly constant with redshift within a hierarchical structure formation scenario. In other words, if the largest structures form later than the smaller ones, but the stellar and baryon to halo mass relations of clusters do not evolve with redshift, it means that there

\footnote{All errors are at 68% confidence level.}
must be a source of infalling material outside of the clusters to keep those relations fixed.

Understanding the stellar, and generally, baryonic, content is important to understand the evolution of clusters and galaxies and the systematics that may affect mass estimates for cosmology. The discrepancies between simulations and observations (as pointed in several works, e.g. Arthur et al. 2017), may arise from the fact that we have not yet fully understood this evolution. We will come back to this problem in Chapter 6.

1.3 Gravitational waves

The first detection of gravitational waves (GW) in 2015 (Abbott et al. 2016a), which was worthy of a Nobel prize in 2017, and of an electromagnetic (EM) counterpart to a GW event (LIGO Scientific Collaboration et al. 2017) mark the beginning of a new era of astronomy.

Gravitational waves were predicted by Einstein in 1916 (Einstein 1916; Einstein 1918) within the Theory of General Relativity, and scientists had been searching for them for decades before the first detection. GWs are ripples in the space–time that travel at the speed of light,\(^9\) and are a consequence of Einstein’s equations. Suppose that there is a small perturbation \(h_{\mu\nu}\) on a nearly flat spacetime, i.e. a Minkowski spacetime with a metric \(\eta_{\mu\nu} = \text{diag}(-1, 1, 1, 1)\). Then the metric will be:

\[
g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}(x) \quad \text{with } |h_{\mu\nu}| \ll 1.\tag{1.35}
\]

In this “linearised gravity” regime, in the Lorentz gauge (which is equivalent to a coordinate choice), Einstein’s equations simplify to (in vacuum, \(T_{\mu\nu} = 0\)):

\[
\left(-\frac{\partial^2}{\partial t^2} + \nabla^2\right) h_{\mu\nu}(x) = 0, \tag{1.36}
\]

which is an ordinary wave equation propagating at the speed of light. Plane waves of the type \(h_{\mu\nu} = A_{\mu\nu} \exp(2\pi i k_{\mu} x^\mu)\) are a solution, with \(k_{\mu} k^\mu = 0\). If in addition to the Lorentz gauge, one assumes the so called transverse–traceless gauge (which is also allowed because we have 4 degrees of freedom to specify), and chooses the \(z\) axis to be along the direction of wave propagation, the line element can be written with 2 only independent amplitudes,

\(^9\)At least within GR predictions. We shall see below that the speed of GWs has been confirmed to be the same as the speed of light, or very close to it.
Chapter 1. Introduction

$h_+$ and $h_\times$, 2 independent degrees of freedom for the polarisation. It can be shown that the metric perturbation becomes (see e.g. the review by Riles 2013):

$$h_{\mu\nu}(x) = \begin{pmatrix}
0 & 0 & 0 & 0 \\
0 & h_+ & h_\times & 0 \\
0 & h_\times & -h_+ & 0 \\
0 & 0 & 0 & 0
\end{pmatrix} \exp[ik(z - t)].$$

1.3.1 Detection

In order to measure these distortions of spacetime, one needs to define some standard “ruler” that is not affected by gravity. The speed of light is a quantity which is not affected by the tidal forces: the idea is to send light to a point where it can be reflected, and measure the return time on a clock at the initial position. Given that we want to measure the proper distance between the initial and reflecting point in order to detect any changes in spacetime, we also need to measure the proper time (i.e. in an inertial frame). The return time of the light beam gives us a measurement of that proper distance. In the simple case in which $A_{xy} = h_\times = 0$, the wave propagates with a $+\,$ polarisation along the $z$ axis, and a photon emitted at time $t$ reaches the position $x = L$ at the time:

$$t_L = t + \int_0^L [1 + h_+(t(x))]^{1/2} dx,$$

and in the linearised theory the rate of change of the return time $t_{\text{ret}}$ of the photon is:

$$\frac{dt_{\text{ret}}}{dt} = 1 + \frac{1}{2} [h_+(t + 2L) - h_+(t)].$$

Note that this change depends on the wave amplitude at the origin when the photon is sent out and when it returns. In the general case, the return time will depend on the amplitude at the reflecting end, too. The technology used in the gravitational wave detectors such as the Laser Interferometry Gravitational-wave Observatory (LIGO; LIGO Scientific Collaboration et al. 2015) and Virgo (Acernese et al. 2015) utilise this concept through laser beams in very large interferometers. They are enhanced (i.e. with an extra mirror) Michelson interferometers. The length of the arms of these detectors is much smaller than the typical wavelength $\lambda$ of a gravitational wave, so that Eq. (1.38) can be expanded in $L/\lambda$. Unfortunately, the GW amplitudes are too small to produce any change.
1.3. Gravitational waves

in time detectable with the accuracy of current clocks. However, a measurement of such
amplitudes can be made by comparing the variation of the return time in perpendicular
directions, as in the arms of interferometers.\textsuperscript{10} The length of the arms are typically very
large ($L = 4$ km for LIGO, 3 km for Virgo) to increase the precision on the actual measured
quantity, the strain $h = \Delta L / L$, where the change in length $\Delta L$ is due to a gravitational
wave and is limited by instrumental and environmental noise. A typical amplitude for
a gravitational wave generated by a compact binary system merger at the distance of
the Virgo cluster is $h \sim 10^{-21}$. For a detector arm of length 4 km, this corresponds to
measuring a change in length of 1/1000 the size of a proton. The strain sensitivity of
the detectors depends on the frequency of the wave, and it lies between $10^{-20} - 10^{-23}$ for
the last LIGO-Virgo observation run over the expected range of compact object binaries
frequencies. The strain is comparable to the GW amplitude because a detector with arm
length $L$ responds to a GW of amplitude $h$ as $\Delta L \sim hL$. The instruments have recently
been upgraded to advanced LIGO (aLIGO) and Virgo (AdV or aVirgo), with an increased
sensitivity of an order of magnitude, corresponding to an increase in search radius of a
factor 10, and therefore of $10^3$ in volume. The previous instrument sensitivity was too low
for the rate of observable events to detect anything with decent probability.

Given that the wavelength of the GW events is much larger than the detectors’ length,
they can be thought of as antennas that are only able to localise the position of the GW
source over broad areas. Triangulating a detection with multiple interferometers can help
in constraining the position: a pair of detectors restricts the location to an annulus over
the sky, and combining pairs of detectors at different locations allows intersections of these
annuli. LIGO interferometers are located in isolated areas by Washington (LIGO Hanford)
and Louisiana (LIGO Livingston), and separated by $\sim 3,000$ km, while Virgo is in Pisa
(Italy).

Note that the calculations shown in the linearised gravity are only meant for a qualita-
tive understanding, and more sophisticated calculations need to be performed in a practical
analysis. For more detailed analyses of gravitational waves, detectors and searches see the
reviews by Sathyaprakash & Schutz (2009), Pitkin et al. (2011) and Riles (2013).

\textsuperscript{10}This comparison is allowed by the fact that gravitational radiation is not isotropic.
Figure 1.1: Strain amplitude from GW150914, showing the different stages of the binary coalescence and the behaviour with time of the orbital velocity and separation. From Abbott et al. (2016a).

1.3.2 Sources of GWs

The most promising sources of gravitational waves detectable by current and upcoming GW experiments are mergers of compact binaries (CB). Considered binaries include binary neutron stars (BNS or NS-NS), binary black holes (BBH or BH-BH) and black hole-neutron star (BH-NS) systems. These systems tend to gradually lose angular momentum while radiating gravitational waves, so that their orbit shrinks as they proceed towards an inevitable collision. The gravitational radiation emitted during the highly relativistic final moments of this process is huge, corresponding to ~ 5 – 10% of the initial mass of the system, and this is why we regard CBs as the most promising sources to be detected from Earth. The stages that characterise a CB coalescence can be distinguished into: inspiral, merger and ringdown. During the inspiral phase, one can use a quasi–Newtonian approximation and work out analytic expressions. It can be shown that the GW frequency $f$ and amplitude $h$ for a binary system of objects with masses $M_1$ and $M_2$ in a circular
orbit are (Riles 2013):

\[ f = \frac{1}{8\pi} \left[ \frac{5^3}{G^3 \mathcal{M}^5 (\tau - t)^3} \right]^{\frac{1}{2}}, \]  

(1.39)

\[ h = \frac{1}{r} \left( \frac{5G^3 \mathcal{M}^5}{\tau - t} \right)^{\frac{1}{2}}, \]  

(1.40)

where \( \mathcal{M} \equiv \left( \frac{M_1 M_2}{M_1 + M_2} \right)^{\frac{3}{5}} \) is the chirp mass, \( \tau \) is the time at coalescence and \( r \) is the distance to the system. Note that: (i) both frequency and amplitude depend on the chirp mass, so we can estimate its value from a GW measurement, but that at this level one cannot disentangle the values of the two masses; (ii) the frequency diverges as \( t \to \tau \); (iii) the amplitude, effectively our observable, declines as \( 1/r \), which on cosmological scales has the meaning of luminosity distance. An example of strain signal is shown in Figure 1.1. Other parameters are needed to fully describe the binary system, such as orbit ellipticity, object spin and system orientation.

As the radius of the orbit approaches zero, the post–Newtonian approximation breaks down and numerical simulations are required. The coalescence is expected to form a black hole highly distorted in shape. The remnant is expected to go through a “ringdown” phase during which these “distortions” are radiated away through GWs.

Other sources of GW signals include continuous waves from spinning neutron stars and primordial GW background, but these topics go beyond the scope of this thesis.

1.3.3 The electromagnetic counterpart

While no electromagnetic emission is expected from the collision of two black holes due to the lack of baryonic material,\(^{11}\) the merger of a compact object system containing a NS should produce a range of different transients emitting at different wavelengths, from radio to gamma-ray, and with different timescales (e.g. Bloom et al. 2009; Metzger & Berger 2012; Piran et al. 2013; Rosswog 2015). Let us shortly review the processes that lead to such emission, shown in the schematic cartoon in Figure 1.2, as predicted by popular models and simulations.

First, the binary can collapse into a NS or a BH depending on its final baryonic mass.

\(^{11}\)Supermassive black holes (SMBHs) may be an exception, but they are not observable with current and near term GW experiments because of their typical strain and frequency values. Future GW experiments such as LISA may be able to detect SMBH mergers, but we do not consider those in this thesis.
Chapter 1. Introduction

Figure 1.2: A schematic cartoon of the origin of the predicted EM counterparts to BNS or NS-BH binaries. From Metzger (2017a).

$M_{\text{rem}}$ after the coalescence. If $M_{\text{rem}} \lesssim fM_{\text{max}}$, where $f = 1.3 - 1.6^{12}$ and $M_{\text{max}}$ being the maximum mass of a NS (Bauswein et al. 2013), the remnant will produce a massive, shortly-lived NS, that will eventually collapse into a BH in a matter of milliseconds to seconds. Otherwise, if the mass of the binary is larger than this limit, the remnant is directly a BH.

At the time of the merger, part of the binary mass can be ejected outside of what will be the remnant. The ejecta are neutron rich and are expected to undergo rapid-neutron capture processes, or $r$-processes, a set of nuclear reactions that allows nuclei to capture neutrons more quickly than their radioactive decay. This processes allow the formation of heavy nuclei and occur in regions with high neutron densities.

The ejecta originate through two main mechanism. The first one occurs within milliseconds during the merger itself, and it is due to the tidal forces produced by the coalescence. When the stars come into contact, additional material is squeezed into the polar regions. The ejecta produced with this mechanism have velocities of $\sim 0.2 - 0.3c$. The merger is also expected to produce a centrifugally-supported disk around this remnant. This material is partially blown away by roughly spherical winds about a second after the merger with velocities of $\sim 0.05 - 0.1c$.

A rapid accretion of the disk is able to power a collimated relativistic jet within seconds from the merger, which can be seen as a sGRB if observed with a viewing angle $\theta_{\text{obs}} \lesssim \theta_j$, where $\theta_j$ is the half-opening angle of the jet, shown in Figure 1.2.

$^{12}$This value is still uncertain (Bauswein et al. 2013).
1.3. Gravitational waves

In the ejecta, heavy nuclei are produced through $r$–processes, and they will be heavier where the neutron mass fraction is higher, otherwise, the processes stall at lower mass numbers. While the tidal ejecta produced at first towards all directions are expected to be more neutron rich, the material squeezed in the polar regions and that ejected from the disk have a lower neutron density due to the neutrino irradiation and weak interactions converting neutrons into protons (Kasen et al. 2017). As the ejecta expand and decompress from their original high densities, and the neutron flux is exhausted, the unstable nuclei produced by the $r$–processes will $\beta$–decay, transforming its neutrons into protons, and producing stable $r$–process heavy elements. The $\beta$–decays release energy, keeping the ejecta warm at temperatures of $10^3 - 10^4$ K. At first, the outflows are optically thick due to the high densities, until the photon diffusion time through the ejecta becomes comparable to the expansion time of the ejecta themselves. At this point, significant EM radiation can be produced (Metzger et al. 2010a). The luminosity of this thermal radiation depends on the mass of the ejecta and on its expansion velocity: larger masses produce brighter and longer lived radiation, higher velocities mean brighter and shorter lived emission.

The observed radiation depends on the composition of the ejecta. If they contain a high fraction of heavier $r$–process elements, such as lanthanides (atomic numbers $57 < Z < 71$) or actinides ($89 < Z < 103$), their optical opacity and typical photon diffusion times are higher than what they would be with lighter elements. Thus, ejecta containing heavier elements (such as the tidal ejecta) obscure the optical wavelengths and are primarily visible in the infrared, with longer-lasting light curves (with timescales of days to 1 week). The polar ejecta can contain lighter elements, and give rise to a briefer and bluer light curve.

The emission associated with these ejecta is what we call a kilonova, and it has been identified by Metzger & Berger (2012) as the most promising EM counterpart, given its isotropic nature, as opposed to the collimated GRB. For the reasons explained above, kilonovae can show a “blue” and fast evolving (over timescales of $\lesssim 1$ day, Metzger et al. 2010b) component in addition to a “red” and longer lived one (Barnes & Kasen 2013; Tanaka & Hotokezaka 2013).

A non–thermal GRB afterglow, i.e. the emission that follows the prompt sGRB at

---

13 Fun fact: the predicted peak luminosities (Metzger et al. 2010b) of disk ejecta were $\sim 1000$ times those from classical novae.

14 The isotropy is due to material ejected by the tidal forces towards all directions, and the roughly spherical winds acting on the accretion disk.
longer wavelengths, is expected to be produced by the interaction of the jets with the surrounding medium. The afterglow is observed in the optical over timescales up to days or weeks by observers at $\theta_{\text{obs}} \lesssim 2\theta_j$. An isotropic radio afterglow is expected to be produced when the jet decelerates to moderate relativistic speeds by shocking the interstellar matter (ISM).

An analysis of the expected EM counterparts at different wavelengths is described in Metzger & Berger (2012) and Metzger (2017b) (in the light of GW170817), while a specific review on kilonovae is presented in Metzger (2017a). These reviews have been mostly followed when writing this introductory section.

There are several motivations to search for the EM counterpart to a GW event:

- The closest to a cosmologist’s heart is surely the possibility of constraining the Hubble constant. Recall from Eq. (1.40) that we can estimate the luminosity distance from the GW amplitude, and if an EM counterpart is detected and associated with an host galaxy having a measured redshift, then $H_0$ can be constrained through Eq. (1.14). In other words, GW triggers with an identified EM emission can be used as standard sirens (Schutz 1986; Holz & Hughes 2005), similarly to what is usually done with Supernovae as standard candles. This analysis has been performed for GW170817 in Abbott et al. (2017a), and a larger number of GW triggers with an associated EM counterpart will place competitive constraints on $H_0$ (Nissanke et al. 2010).

- To constrain gravity models through estimates of the difference between the speed of light and the speed of gravitational waves (Nishizawa 2016, Baker & Trodden 2017 and references therein). In fact, we have seen how GR predicts that GWs propagate at the speed of light. The time elapsed between the detection of the GW signal and the detection of the GRB is at least partially intrinsic to the kilonova model we have described, but it can rule out gravity theories that predict a larger time delay in between the two signal due to their different velocities. This analysis has been performed in Abbott et al. (2017b).

- To study the astrophysics of these systems to constrain the equation of state of NSs and the origin of the $r$–process elements.
1.3. Gravitational waves

GW170817
DECam observation
(0.5–1.5 days post merger)

GW170817
DECam observation
(>14 days post merger)

Figure 1.3: DECam observations of the kilonova associated to GW170817. Left panel: coadded image from 0.5–1.5 days post GW trigger. Right panel: coadded image after two weeks from the trigger. The transient has significantly faded away within this timescale, as expected from kilonova models. From Soares-Santos et al. (2017), credits to Will Hartley.

1.3.4 LIGO–Virgo GW triggers

Coalescences of compact binaries were indeed observed during the first observing runs. During the first observing run (O1, September 2015 – January 2016) only the two LIGO detectors were working, with a sensitivity out to 60 – 80 Mpc for BNS. During O1 there were two detections of BBH mergers (GW150914, Abbott et al. 2016a, and GW151226, Abbott et al. 2016a) and a lower significance candidate (LVT151012, Abbott et al. 2016b).

During O2, the second observing run (November 2016 – August 2017), aLIGO was able to detect BNSs out to 100–220 Mpc, and it was joined for the last month by aVirgo, with a horizon reaching 50-60 Mpc (Abbott et al. 2017a). Four detections were made during O2: three BBH coalescences (GW170104, Abbott et al. 2017b, GW170608, Abbott et al. 2017d, and GW170814 Abbott et al. 2017c) and a BNS merger (GW170817, Abbott et al. 2017a).

GW170814 was the first detection made by LIGO together with Virgo, and the triangulation of the signal permitted a reduction of the 90% sky localization area from 1160 deg² (with LIGO only) to 60 deg². All of the mentioned BBH coalescence detections feature black holes of masses \(\sim 20 – 30 \, M_\odot\), which are not usually expected within standard stellar evolution theories. It is usually thought that BH of stellar origin can hardly reach these masses due to the large mass loss from stellar winds in the late phases of a
massive star life. However, stellar evolution models of these late stages are uncertain, and Belczynski et al. (2010) show that BHs of up to 80 $M_{\odot}$ can have a stellar origin. The study of the origin of these black holes has started to involve more exotic models, including Primordial Black Holes (PBH, e.g. García-Bellido 2017), and it provides the opportunity of constraining the amount of dark matter present in the Universe in the form of PBHs (e.g. Raidal et al. 2017). Typical luminosity distances of these events are 200–400 Mpc. GW170817 was the first GW event for which an EM counterpart was confirmed (LIGO Scientific Collaboration et al. 2017). A description of the EM counterpart to this event with DECam data is presented in Chapter 3. In the meantime, enjoy a DECam coadded image of the first observed kilonova on the left–hand panel of Figure 1.3.

For a discussion on past and future observing plans with LIGO, see Abbott et al. (2016b).

So far, we have discussed how gravitational waves events can have an associated optical counterpart, and how the redshift of the host galaxy is needed in order to make cosmological measurements. We have also discussed how galaxy clusters can constrain cosmology and how they represent an interesting and peculiar environment for galaxy evolution studies. It is now time to introduce the source of data necessary to such analyses: the large galaxy surveys.

### 1.4 The era of large galaxy surveys

A remarkable number of on–going and planned galaxy surveys will provide data for hundreds of millions, or even billions, of galaxies back to when the Universe was only a fraction of its present age. These surveys were born and funded with the goal of measuring dark energy and other cosmological parameters with unprecedented accuracy. The constraining power of a particular survey or cosmological probe on DE is often quantified in terms of its Figure of Merit (FoM; Huterer & Turner 2001). The FoM is given by the reciprocal of the area of the 95% confidence limit uncertainty ellipsoid for the DE parameters $w_0, w_a$ defined in Eq. (1.30). In the Fisher matrix formalism\textsuperscript{15} this corresponds to:

$$\text{FoM} \propto \left[ \sigma(w_0)\sigma(w_a) \right]^{-1},$$

\textsuperscript{15}The Fisher matrix formalism is often used in astronomy and provides a prescription to forecast errors and covariances for the parameters to be estimated from a future experiment, given the specifics of the experiment.
where $\sigma(w_0)$ $\sigma(w_a)$ are the uncertainties on the parameters. This choice was first adopted by the Dark Energy Task Force (DETF; Albrecht et al. 2006) as a metric to compare and classify different surveys and methods. The DETF divided dark energy experiments into different Stages. Stage I experiments have provided the data that were known at the time of writing (back in 2009) from observations of Type Ia Supernovae (SN), CMB anisotropies, weak lensing and Baryonic Acoustic Oscillations (BAO). Stage II surveys include DE experiments that were on–going. Stage III comprises on–going medium cost experiments that will improve the FoM by a factor of 3–5 compared to Stage II. Stage IV includes large scale, longer term projects that will improve the FoM by a factor of $\sim 10$ compared to Stage II.

Table 1.2 presents a representative, albeit not exhaustive, list of on–going and upcoming galaxy surveys, both imaging and spectroscopic. Spectroscopic datasets are usually smaller than photometric ones, due to the time involved in taking spectra, and they usually go down to brighter flux limits than imaging surveys. On the other hand, spectra trace in greater detail the fingerprints of galaxies’ stellar populations, and can provide better measurements of the stellar chemical composition, redshift, dust content, amongst other properties. As a result, spectroscopic surveys can provide complementary means to constrain galaxy evolution models and cosmology, as well as calibration sets for photometric surveys.

Stage II projects include the famous optical imaging surveys Sloan Digital Sky Survey II (Abazajian et al. 2009) and PanSTARRS I (Chambers et al. 2016), and the XMM Cluster Survey (Romer et al. 2001) in the X–ray. Stage III imaging experiments comprise DES, described in Section 1.4.1, and the Hyper–Suprime Camera (HSC; Aihara et al. 2018), carrying out similar observations to DES, but to a greater depth on a smaller area. The HSC is only one part of the greater Subaru Measurement of Images and Redshifts (SuMIRe) project. On the spectroscopic side, the Baryon Oscillation Spectroscopic Survey (BOSS; Dawson et al. 2013) and its successor extended BOSS (eBOSS; Dawson et al. 2016) probe the distribution of millions of galaxies and quasars, and the Hobby–Eberly Telescope Dark Energy Experiment (HETDEX; Hill et al. 2008) maps a smaller area but out to a greater distance. Stage IV projects feature the optical imaging Large Synoptic Survey Telescope (LSST; Ivezić et al. 2008), the great successor of DES. LSST will image the southern sky every four nights, providing a huge amount of data for transients science (in particular, SN cosmology). The images will be coadded over ten years of observations,
Table 1.2: A selection of major recent, on-going and future dark energy experiments. Abbreviations in the “Data” column refer to optical (Opt) or near-infrared (NIR) imaging (I) or spectroscopy (S). For spectroscopic experiments, the “Spec-z” column lists the primary redshift range for galaxies (gals), quasars (QSOs). Abbreviations in the “Methods” column are weak lensing (WL), clusters (CL), supernovae (SN) and baryon acoustic oscillations (BAO). Adapted from Weinberg & White (2017).

<table>
<thead>
<tr>
<th>Project</th>
<th>Dates</th>
<th>Area [deg²]</th>
<th>Data</th>
<th>Spec-z range</th>
<th>Probes</th>
<th>Stage</th>
</tr>
</thead>
<tbody>
<tr>
<td>BOSS</td>
<td>2008-2014</td>
<td>10,000</td>
<td>Opt-S</td>
<td>0.3 – 0.7 (gals)</td>
<td>BAO</td>
<td>III</td>
</tr>
<tr>
<td>DES</td>
<td>2013-2019</td>
<td>5,000</td>
<td>Opt-I</td>
<td></td>
<td>BAO, WL</td>
<td>III</td>
</tr>
<tr>
<td>eBOSS</td>
<td>2014-2020</td>
<td>7,500</td>
<td>Opt-S</td>
<td>0.6 – 2.0 (gal/QSO)</td>
<td>BAO</td>
<td>III</td>
</tr>
<tr>
<td>SuMIRe</td>
<td>2014-2024</td>
<td>1,500</td>
<td>Opt-I</td>
<td></td>
<td>WL, CL</td>
<td>III</td>
</tr>
<tr>
<td>HETDEX</td>
<td>2014-2019</td>
<td>300</td>
<td>Opt-S</td>
<td>1.9 – 3.5 (gals)</td>
<td>BAO</td>
<td>III</td>
</tr>
<tr>
<td>DESI</td>
<td>2019-2024</td>
<td>14,000</td>
<td>Opt-S</td>
<td>0 – 1.7 (gals)</td>
<td>BAO</td>
<td>IV</td>
</tr>
<tr>
<td>LSST</td>
<td>2020-2030</td>
<td>20,000</td>
<td>Opt-I</td>
<td></td>
<td>BAO, WL</td>
<td>IV</td>
</tr>
<tr>
<td>Euclid</td>
<td>2020-2026</td>
<td>15,000</td>
<td>Opt-I</td>
<td></td>
<td>WL, CL</td>
<td>IV</td>
</tr>
<tr>
<td>WFIRST</td>
<td>2024-2030</td>
<td>2,200</td>
<td>Opt-S</td>
<td>0.7 – 2.2 (gals)</td>
<td>BAO</td>
<td>IV</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>NIR-S</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
resulting in an incredibly deep survey for a ground based experiment.

Space missions include Euclid (Laureijs et al. 2011) and WFIRST (Wide Field Infrared Survey Telescope; Green et al. 2012), and will provide both imaging and spectroscopic data for billions of galaxies.

Surely datasets mapping huge volumes of the Universe can be exploited for astrophysical studies beyond cosmological parameters. It is in this spirit that gravitational wave follow up programs were born with the goal of observing kilonovae, and that we perform galaxy evolution studies by looking at the astrophysical properties of single galaxies. In addition, galaxy surveys have enabled observations of the host galaxy to the first BNS GW signal, so that we could provide a measurement of the cosmological parameter $H_0$. In this thesis we also show how galaxy properties can be used to estimate the total mass of galaxy clusters, which again is a necessary step towards cosmological measurements.

1.4.1 The Dark Energy Survey

The DES (for further information see The Dark Energy Survey Collaboration 2005 and www.darkenergysurvey.org) is an optical-near-infrared survey that is imaging 5000 deg$^2$ of the South Galactic Cap in grizY bands over 525 nights spanning almost six years. The DES filters transmission curves are shown in Figure 1.4. The survey is being carried out using a $\sim 3$ deg$^2$ CCD camera (the DECam, see Flaugher et al. 2015) mounted on the Blanco 4-m telescope at the Cerro Tololo Inter-American Observatory (CTIO) in Chile. DES started in 2012 with a testing period (November 2012 – February 2013) called Science Verification (SV). At the time of writing, five observing seasons have been completed, and the survey will be completed in January 2019.

The survey strategy is designed to optimize the photometric calibration by tiling each region of the survey with several overlapping pointings in each band. This provides uniformity of coverage and control of systematic photometric errors. This strategy will allow DES to determine photometric redshifts of $\sim 300$ million galaxies to an accuracy of $\sigma(z) \approx 0.07$ out to $z \gtrsim 1$, with some dependence on redshift and galaxy type, and cluster photometric redshifts to $\sigma(z) \sim 0.02$ or better out to $z \approx 1.3$ (The Dark Energy Survey Collaboration 2005). It will find $\sim 380,000$ groups and clusters and also provide shapes for approximately 200 million galaxies for weak lensing studies. The survey is expected to reach median 10$\sigma$ depths of $g \sim 24.45$, $r \sim 24.30$, $i \sim 23.50$, $z \sim 22.90$, $Y \sim 21.70$ through exposure times of 90 s for griz and 45 s for Y, over 10 passes. The Supernova fields (shown
in yellow in Figure 1.5) cover $\sim 30$ sq. deg. and are observed to a greater depth.

The DES Data Management (DESDM) pipeline is used for data reduction, as described in detail in Sevilla et al. (2011), Desai et al. (2012) and Mohr et al. (2012). The process includes calibration of the single-epoch images, which are co-added after background subtraction and then cut into tiles. The source catalogue was created using Source Extractor (SEXTACT OR, Bertin & Arnouts 1996) to detect objects on the riz co-added images. The photometric data computed with SExtractor and included in the data releases, includes fluxes, magnitudes and star/galaxy separation classifiers used in this work. Fluxes and magnitudes are computed using different apertures, in particular \texttt{MAG\_AUTO} magnitudes are computed within a Kron radius (which changes from object to object), \texttt{MAG\_ISO} magnitudes are isophotal, and \texttt{MAG\_APER} magnitudes are computed within circular apertures of fixed radius. Outputs that are often used for star/galaxy separation purposes are \texttt{CLASS\_STAR} and \texttt{SPREAD\_MODEL}. \texttt{CLASS\_STAR} is a “stellarity” index ranging between 0 and 1, and it is the output of a neural network trained on simulations of galaxy and star images. \texttt{SPREAD\_MODEL} was originally developed for the DESDM pipeline (Desai et al. 2012), and it is able to discriminate between a Point Spread Function (PSF)–like object (which is more likely a star), and a more extended one (more likely to be a galaxy). These quantities are described and used in Chapter 4. However, the DES collaboration has produced some more sophisticated photometric catalogs for the latest releases. These include fluxes and magnitudes computed through the Multi-Object Fitting (MOF) pipeline\footnote{https://github.com/esheldon/ngmixer/wiki/mof-example}, using the \texttt{ngmix} code\footnote{https://github.com/esheldon/ngmix}, initially thought as a code for weak lensing shape measurements. MOF uses an iterative method to simultaneously fit light profiles to several objects, and it has been shown to perform better than standard SExtractor magnitudes on DES data, especially in crowded environments (results internal to the collaboration). In addition, a star/galaxy separation classifier, \texttt{MODEST\_CLASS}, is defined as a function of \texttt{SPREAD\_MODEL} and its error, and has been optimised for DES data. A full description of the classifiers used in DES and their performance is presented in Sevilla-Noarbe et al. (2018).

The data used in this thesis come from three different data releases: SV, Year 1 (Y1) and Year 3 (Y3). SV covers a small portion of the sky ($\sim 200$ deg$^2$, shown in green in Figure 1.5), with depths similar to the final expected depths mentioned above. SV data (including a high quality catalogue of selected objects, the SVA1 “gold” catalogue)
are publicly available at https://des.ncsa.illinois.edu/releases/sva1 and they are used in Chapter 2 for photometric redshift computation, and in Chapter 4 for the analysis of the galaxy cluster RXJ2248.

Year 1 (Diehl et al. 2014) catalogues contain data from the first year of observations (August 2013 – February 2014), and covers 1,839 deg$^2$ (red area in Figure 1.5) with up to 4 passes per filter. Its median 10$\sigma$ depths are $g \sim 23.4$, $r \sim 23.2$, $i \sim 22.5$, $z \sim 21.8$, $Y \sim 20.1$. Similarly to SV, Drlica-Wagner et al. (2017) made specific selections to produce a high-quality object catalogue, the Y1A1 “gold” catalog, used in Chapters 5 and 6. Value-added catalogues from Y1 data, namely the redMaPPer clusters (described in the following subsection) and the Bayesian Photometric Redshifts (BPZ, Benítez 2000) photo-z’s, are also used in Chapters 5 and 6.\footnote{These catalogs were not available for newer DES data at the time of the analyses.}

Y3 data comes from the first three years of observations (August 2013 – February 2016), which cover $\sim 5,000$ deg$^2$ with up to 5 passes per filter. The DES Y3 footprint, which corresponds to the final footprint, is shown in black in Figure 1.5. As a consequence, Y3 is as wide as the final Year 6 (Y6) footprint will be, but shallower. Some of the Y3 data (the wide-field coadd source catalogues) is now publicly available at https://des.ncsa.illinois.edu/releases/dr1 and described in Abbott et al. (2018). Y3 photometry is used in Chapters 3, 5 and 6. Target of opportunity data from the fourth year of observations are also used in the GW follow up work. The final Y6 source catalogues will be available within the DES collaboration in 2019, while the data will be made public in a timescale of a year after that.

The data from DES will allow high precision measurements of dark energy and dark matter through the four cosmological probes previously described: weak gravitational lensing, galaxy clusters abundance, galaxy angular clustering and Supernovae. Several papers using these methods have recently been published for the early DES data covering the Y1 area, in particular from weak lensing and galaxy clustering (The Dark Energy Survey Collaboration et al. 2017\textsuperscript{a}; Gruen et al. 2017; The Dark Energy Survey Collaboration et al. 2017\textsuperscript{b}; DES Collaboration et al. 2017). The DES collaboration has also been able to publish significant work beyond cosmology and Dark Energy, including Milky Way studies, Trans-Neptunian Objects and much of the work included in this thesis regarding galaxy evolution and gravitational waves. See Dark Energy Survey Collaboration et al. (2016) for an overview on non-Dark Energy studies with DES.
Chapter 1. Introduction

Figure 1.4: DES filters transmission curves. From Abbott et al. (2018).

Figure 1.5: DES footprint. The green area is covered by the Science Verification data, used in Chapter 2 and 4. The red area represents the observations from the first year of observations, and it is the area studied with the Y1 redMaPPer clusters in this thesis (Chapter 6). The 5 years planned footprint is shown by the black contours, and it is the same area covered by the Y3 data used in Chapters 3, 5 and 6. The difference between Y3 and Y5 is in the number of passes, and therefore the depth. Plot from Dark Energy Survey Collaboration et al. (2016).
The era of large galaxy surveys

The data used in this thesis also includes Anglo-Australian Telescope (AAT) target of opportunity time data. Other publicly available datasets have been used (VHS, HST, 2dF, 6dF, 2MASS).

**DES redMaPPer clusters**

The most widely used cluster finder within DES is the red-sequence Matched-filter Probabilistic Percolation (redMaPPer; Rykoff et al. 2014). This algorithm is based on the “red sequence” technique. In fact, cluster galaxies are known to occupy a red, specific region in the colour-magnitude diagram, the red sequence (e.g. Visvanathan & Sandage 1977; Worthey et al. 1995). This peculiar feature can be used to identify clusters using photometric data. The redMaPPer algorithm is iterative over two main steps: a calibration of the red sequence over redshift, and a clusters identification. The iteration is started with a set of “training clusters” , that have a spectroscopic redshift measurement for the central galaxy. During step one, the code computes the cluster richness $\lambda$ (which is an estimate of the number of cluster members, and the redMaPPer clusters mass proxy used for cosmological analyses) and its likelihood. When more than 3 galaxies are assigned to the cluster, the algorithm re-estimates the cluster redshift through fitting all the members to the red sequence model. When member selection and redshift estimation converge, the iterations end.

RedMaPPer has been extensively studied and its mass proxy calibrated for large photometric surveys such as the Sloan Digital Sky Survey (SDSS) and the DES over the past decade (Rozo et al. 2009a; Rozo et al. 2009b; Rozo et al. 2011). In particular, Rykoff et al. (2016a) present the first DES redMaPPer catalogue, based on SV data. Several DES works have been finalised using this catalogue: Melchior et al. (2016) have calibrated the relation between richness and total cluster mass using weak lensing measurements. Saro et al. (2015) have done a similar calibration using the Sunyaev–Zel’dovich effect (SZE) detected from South Pole Telescope (SPT) data. The work presented in Chapter 4 on the cluster RXJ2248, also utilises this cluster catalog.

Several works have used the Year 1 redMaPPer catalogue, not released to the public at the time of writing. Notably, Chiu et al. (2017) have used DES, Chandra, and SPT data to estimate the baryon content of redMaPPer clusters, as discussed in Section 1.2.2, and also in Chapter 6. Chang et al. (2017) have analysed the clusters profiles and measured
the so-called splashback radius (corresponding to the radius where matter accreting onto a dark matter halo reaches its first orbital apocenter; Diemer & Kravtsov 2014). The Year 1 cluster catalogue is also used in this thesis, and presented in Chapters 5 and 6.

We shall describe in more detail the redMaPPer mass proxy in Chapter 5, where we compare it to the stellar mass based mass proxy developed in this thesis.

1.5 Thesis Outline and notation

This thesis is structured as follows:

- In Chapter 2 I describe the methods used to derive galaxy properties (mainly stellar mass) and redshifts from galaxies’ Spectral Energy Distribution. I introduce a method that uses a Bayesian Model Averaging technique, and show how I have produced photo-\( z \) estimates for early DES data. An approach to compute stellar masses with machine learning techniques is also introduced.

- In Chapter 3 I show how large galaxy samples with available redshifts and properties are fundamental for electromagnetic follow ups of gravitational wave events. Furthermore, they can be used to understand the formation and evolution of the binary systems they contain. An analysis of this type is presented for the golden event GW170817.

- Chapter 4 includes a study on early DES data showing that stellar masses can be estimated in a robust manner with DES, in particular concerning galaxy clusters. A first estimate of stellar mass fraction in clusters from DES is presented.

- In Chapter 5 I introduce a promising cluster mass proxy, \( \mu_* \), based on stellar masses. Its performance is calibrated against X-ray and weak lensing measurements.

- Chapter 6 shows cluster evolution results for \( \sim 80,000 \) DES clusters. We measure the stellar–to–halo mass relation and the stellar mass function for central galaxies and satellites. Other results on central galaxies and ICL are shown.

- Finally, Chapter 7 is dedicated to the conclusions of this work and to future prospects for expanding my GW host analyses to binary black hole events and to BNS triggers from the fast approaching third LIGO observing season. The plan
for producing $\mu_*$ for Voronoi–Tesselation clusters over the DES Year 3 area is also already undergoing.

Throughout this work we assume a ΛCDM flat cosmology with $h = 0.7$, $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$ unless otherwise stated. The notation adopted for the cluster mass and radius follows the one often used in literature. The radii of spheres around the cluster centre are written as $r_{\Delta m}$ and $r_{\Delta c}$ where $\Delta$ is the overdensity of the sphere with respect to the mean matter density (subscript $m$) or the critical density (subscript $c$) at the cluster redshift. Masses inside those spheres are therefore $M_{\Delta m} = \Delta \frac{4\pi}{3} r_{\Delta m}^3 \rho_m$ and similarly for $M_{\Delta c}$. In the following, we quote $\Delta = 200$, which roughly corresponds to the density contrast at virialisation for a dark matter halo at $z = 0$. In order to convert between the different mass definitions we use the Python Colossus tools (Diemer 2017). Logarithms indicated as Log have base 10. The galaxies’ Initial Mass Function adopted follows Chabrier (2003), unless otherwise stated. Errors quoted are $1\sigma$. 
Chapter 2

Galaxy SED fitting methods and applications

“Everything we see hides another thing, we always want to see what is hidden by what we see.”

René Magritte

The work presented in this Chapter contains part of Palmese et al., 2018, currently in the DES review process, and of my contribution to the SV public release and DES SV papers with photometric redshift estimation with ANNz2. The machine learning method for stellar mass estimation is unpublished.

Fundamental properties of the unresolved stellar populations within galaxies are encoded in the galaxy Spectral Energy Distribution (SED) that we observe. These include the Star Formation History (SFH), stellar mass, initial mass function (IMF) and the metallicity. The SED are also more or less shifted towards longer wavelengths depending on the galaxy’s redshift. Extracting as much information as possible from the DES galaxy SEDs is the first goal of this thesis, as the derived properties are fundamental to the analyses that we want to make for gravitational wave source host galaxies and clusters. Thankfully, a huge effort has been spent by the astrophysical community to model and fit SEDs
of unresolved stellar populations over the past decades. In this Chapter we first provide an introduction to redshift estimation and stellar population synthesis models, then we describe the methods used in this thesis to evaluate galaxy properties, from photometric redshifts to stellar masses and star formation rates. In particular, we present a code written by James Annis and myself that uses Bayesian Model Averaging to evaluate galaxy properties that we have made publicly available. We show the first application of machine learning methods to stellar mass estimates from photometric data. Finally, we present some applications of these methods with DES data.

2.1 Redshifts

We recall that the redshift of a galaxy is defined in Eq. (1.5) as:

\[ z \equiv \frac{\lambda_{\text{obs}}}{\lambda_{\text{em}}} - 1, \]  

though not all of it is due to the expansion of the Universe as in Eq. (1.5). The redshift of a galaxy includes contributions coming from the cosmological redshift due to the expansion of the Universe \( z_H \), from peculiar motions with respect to the observer \( z_{\text{phys}} \) and possibly to gravitational redshifts \( z_{\text{grav}} \), due to galaxies motion within gravitational potential wells, so that:

\[ z_{\text{tot}} = z_H + z_{\text{phys}} + z_{\text{grav}}. \]  

The gravitational redshift is usually neglected as it is a very small contribution to the total redshift.\(^1\) Peculiar motions can arise from the motion of Earth around the Sun (with a velocity of \( \sim 29 \text{ km s}^{-1} \)), the Milky Way’s motion with respect to the CMB reference frame (\( \sim 630 \text{ km s}^{-1} \) corresponding to \( z \sim 0.002 \)) and orbital motions of galaxies around each other or in cluster potential wells. The galaxies’ velocity dispersion in clusters can reach values of \( \sim 1500 \text{ km s}^{-1} \) (corresponding to \( z \sim 0.005 \)).

Photometric surveys such as DES measure the redshift of galaxies through photometry, and the estimated redshifts are called photometric redshifts or photo-z’s. Photo-z’s have been introduced back in the 60s by Baum (1962), and they have been extensively

\(^1\)Works on gravitational redshifts in clusters and galaxies have tried to estimate this contribution through statistical methods such as stacking (e.g. Wojtak et al. 2011; Sadeh et al. 2015).
studied and utilised since the advent of the recent wide-field photometric surveys. While spectroscopy can produce more precise redshift measurements, it is technically arduous work to measure spectra for hundreds of millions of galaxies in a reasonable time span using current technology. While a whole region of galaxies can be imaged with DECam at once, spectroscopy can only be obtained for those galaxies that can be targeted with slits or fibers. Even though photo-z’s are subject to large uncertainties, some analyses, such as weak lensing, can benefit more from larger number statistics than from precise redshift measurements. The requirements on the photo-z accuracy for a galaxy survey are usually computed from the requirements on the estimates of cosmological parameters. The requirements on DES redshifts are defined through several metrics computed for a sample of galaxies that has both a photo-z estimate and a reference redshift given by spectroscopy. We assume that those spectroscopic redshifts are the true redshifts of galaxies. The metrics are defined in Sánchez et al. (2014):

- $\bar{\Delta z}$: the mean of the bias distribution $\Delta z$, given by the difference between estimated photo-z’s and the reference redshifts.

- $\sigma_{\Delta z}$: the standard deviation of the bias distribution.

- $\sigma_{68}$: the scatter expressed as the half–width of the bias distribution around the median of the $\Delta z$ distribution, containing 68% of the galaxies. This scatter is required to be $< 0.12$ for DES.

- out$_{2\sigma}$: the outlier fraction, i.e. the fraction of galaxies with $|\Delta z - \bar{\Delta z}| > 2\sigma_{\Delta z}$, which is required to be $< 0.1$.

- out$_{3\sigma}$: the fraction of galaxies with $|\Delta z - \bar{\Delta z}| > 3\sigma_{\Delta z}$, which is required to be $< 0.015$.

One of the main features of galaxies’ SEDs that allow us to measure redshifts with DES is the relatively sharp drop at 4000 Å: the 4000 Å break. This feature is produced by the absorption of various metallic lines around similar wavelengths, and can be further enhanced by a deficiency of young, blue stars (e.g. Hamilton 1985). The drop is shown in the blue line in Figure 4.2, which represents the spectrum of a typical early–type galaxy at $z = 0$. For more distant galaxies the 4000 Å break is shifted towards longer wavelengths, as shown in green and red lines in the plot. This feature is covered by the DES filters out
to redshifts just above \( z \sim 1 \), hence we do not (usually) exceed this redshift with DES analyses.

For DES galaxy evolution and clusters studies, objects are usually at cosmological distances (outside the Local Group, mostly \( 0.1 < z < 1 \)) so the only contribution to the redshift we consider from photometric data is due to the Hubble expansion. The remaining parts are negligible compared to \( z_H \) and well below our photometric redshift uncertainty. GW follow up studies are an exception, as GW sources are in the local universe (usually \( z < 0.1 \)) and the redshift estimation becomes tricky with DES data alone, and we require spectroscopic data. The Supernova rejection study is exempted from a spectroscopic follow up as it falls again into the cosmological distance regime.

Note that in some analysis, estimation of the full redshift probability density function (PDF) may be useful (or from it, even just a random draw). Some redshift estimation codes are able to provide that as their output, although storing and sharing a full PDF for each entry in a large galaxy sample such as DES is a known issue (see e.g. Rau et al. 2015).

### 2.2 Stellar population synthesis modeling

The spectral evolution of galaxies is usually studied through what we call “Stellar Population Synthesis” (SPS) modeling, or “evolutionary synthesis” modeling. This method relies
2.2. Stellar population synthesis modeling

Figure 2.2: Schematic illustration of stellar population synthesis modeling, from Conroy (2013).

on stellar evolution models to constrain stellar populations with a certain metallicity and age; the first synthesis models of this type were developed in the late 60s and 70s (e.g. Tinsley 1968; Tinsley 1972; Searle et al. 1973). Note that in the following we describe a commonly used, though not universal, methodology.

2.2.1 Simple stellar populations

The first step in constructing SPS models is building the simple stellar population (SSP) models, i.e. the evolution over time of a stellar population having a single metallicity and age. For an SSP, an SED $f_{\text{SSP}}$ that depends on time $t$ and stellar metallicity $Z$ is given by (Conroy 2013):

$\frac{\text{mass fraction in elements heavier than helium}}{\text{mass fraction in helium}}$
Chapter 2. Galaxy SED fitting methods and applications

\[ f_{\text{SSP}}(t, Z) = \int_{m_{\text{lo}}}^{m_{\text{up}}} f_{\text{star}}[T_{\text{eff}}(M_\star), \log g(M_\star)|t, Z]|\phi(M_\star)\,dM_\star, \]  

(2.3)

where \( M_\star \) is the stellar mass at the zero–age main sequence. The constituents of Eq. (2.3) are:

- Isochrones from a stellar evolution theory. Isochrones represent the position of stars in the Hertzsprung–Russell diagram with same age and metallicity. The theory has lower and upper limits (\( m_{\text{lo}} \) and \( m_{\text{up}} \)) on stellar masses and the isochrones dictate the relation between the effective temperature \( T_{\text{eff}} \), the surface gravity \( g \) and \( M_\star \) at each time and metallicity values. Some popular isochrones include the Padova (Bertelli et al. 1994; Girardi et al. 2000) and the BaSTI (Pietrinferni et al. 2004) models.

- Stellar spectra \( f_{\text{star}} \). These are derived from stellar spectral libraries, that deal with converting the stellar evolution outputs into actual spectral energy distributions. Usually several libraries are used together in order to cover a wider range of the parameter space. Libraries can be theoretical (e.g. BaSeL, Lejeune et al. 1997, Lejeune et al. 1998, Westera et al. 2002 which is the most used theoretical stellar library) or empirical (e.g. STELIB, Le Borgne et al. 2003, MILES, Sánchez-Blázquez et al. 2006).

- The Initial Mass Function \( \phi(M_\star) \), which gives the stellar mass distribution of the zero–age main sequence. Typically, this has the form of a power law or a broken power law. A set of widely used IMFs is discussed in Chapter 6.

The choice of the IMF is an important step as the IMF not only determines the normalisation of the \( M_\star/L \), but it also significantly impacts composite stellar populations SEDs. In fact, the luminosity of an SSP is dominated by the stars at the turnoff mass, which translates into a range of several turnoff masses within a composite population. The most widely used IMFs differ at the low mass end (\( M_\star < 1M_\odot \)): stars in this regime dominate the stellar mass of a galaxy but contribute very little (a few percent) to the overall galaxy bolometric luminosity for an old stellar population. It is thus impracticable to discern between these different models with the photometric data from DES without introducing degeneracies with stellar mass/mass-to-light ratio.
2.2. Stellar population synthesis modeling

2.2.2 Composite stellar populations

A galaxy’s spectrum can be built up by adding the spectra of several SSPs of different ages and metallicities into a Composite Stellar Population (CSP) model of the form:

\[
f_{\text{CSP}}(t) = \int_{t'=0}^{t} \int_{Z=0}^{Z_{\text{max}}} (f_{\text{SSP}}(t', Z)SFR(t-t')P(Z,t-t')e^{-\tau_d(t')} + A_{\text{dust}}(t', Z)) dt' dZ,
\]

The ingredients needed to build such SED are:

- The star formation history (SFH), dictating the ages of stars from SSPs. This is given in the form of a star formation rate (SFR) as a function of time. Widely adopted SFHs include very simplistic models, such as the exponential or \( \tau \) model (Schmidt 1959), that follows \( \text{SFR}(t) \propto e^{-t/\tau} \). A more realistic SFH includes an early rising SFR as \( \text{SFR}(t) \propto t^\beta e^{-t/\tau} \). In this thesis we adopt more complicated models that include log-normal and Simha et al. (2014) models.

- A time–dependent metallicity distribution \( P(Z,t) \), often reduced to a \( \delta \)–function, i.e. a single metallicity value.

- A dust model. Interstellar dust has an important effect on galaxies’ SEDs through UV–to–NIR obscuration and IR emission, and the impact is stronger for star–forming galaxies. Usually, when modelling SPS we fix the shape of the attenuation curve to a Calzetti et al. (2000) or a Charlot & Fall (2000) law and fit for the normalisation. The dust attenuation enters in Eq. (2.4) through the dust optical depth \( \tau_d \). Dust emission is modelled through \( f_{\text{dust}} \), including a normalisation constant \( A \). However, this component is not usually relevant for DES bands, and in our work we often ignore it to avoid adding parameter degeneracies to our SED fitting.

We refer to the total amount of mass in stars contained in a galaxy as the galaxy’s stellar mass. This quantity is usually measured from a mass-to-light ratio \( M_\star/L \), which is derived from some SED fitting and then multiplied by the luminosity. Figure 2.2 shows all the components necessary for building a CSP model. For a comprehensive review on SPS models see Conroy (2013).
Synthetic photometry can then be derived from the computed spectra \( F(\lambda) \) by integrating them after convolution with the filters transmission curves \( S(\lambda) \). The derived fluxes or magnitudes can then be compared with the observed values to constrain galaxy properties. For a filter \( i \) with transmission curve \( S_i(\lambda) \), the magnitude is given by (e.g. Girardi et al. 2000a):

\[
m = -2.5 \log \left( \frac{\int \frac{\lambda}{hc} F(\lambda) S_i(\lambda) d\lambda}{\int \frac{\lambda}{hc} F^0(\lambda) S_i(\lambda) d\lambda} \right);
\]

where the factors \( \frac{\lambda}{hc} \) come from the fact that photons are counted in CCD cameras, and \( F^0(\lambda) \) is a normalisation that depends on the magnitude system used. In this thesis and more generally in DES, we usually work with magnitudes in the AB system, which is normalised so that a spectrum with constant flux per unit frequency has zero magnitude. This translates into \( F^0_{AB}(\nu) = 3.631 \times 10^{-20} \text{erg s}^{-1} \text{cm}^{-2} \text{Hz}^{-1} \) and \( F^0_{AB}(\lambda) = F^0_{AB}(\nu)c/\lambda^2 \).

### 2.3 Methods

There are two common approaches to photo-z’s estimation: template–fitting methods and machine learning methods.

**Template fitting** methods involve the compilation of a library of expected magnitudes for a range of galaxy spectra over a grid of redshifts. The latter can be either synthetic (e.g. Bruzual & Charlot 2003; Conroy & Gunn 2010), as described in Section 2.2, or empirical (e.g. Coleman et al. 1980). The expected magnitudes \( t_i \) for each \( i \)-th filter are estimated through Eq. (2.5) and compared to the observed ones, \( m_i \), with error \( \sigma_i \). The fit can be performed through a \( \chi^2 \) minimisation. Thus minimise:

\[
\chi^2(z, \text{SED}) = \sum_i \left( \frac{m_i - \alpha(z, \text{SED}) t_i(z, \text{SED})}{\sigma_i} \right)^2,
\]

with respect to redshift and template SED to find the best–fit SED at redshift \( z \). The scaling factor \( \alpha(z, \text{SED}) \) normalises the template magnitudes to the observed ones:

\[
\alpha(z, \text{SED}) = \left( \sum_i \frac{m_i t_i(z, \text{SED})}{\sigma_i^2} \right) / \left( \sum_i \frac{t_i(z, \text{SED})}{\sigma_i^2} \right).
\]
2.3. Methods

Examples of template–fitting methods are HyperZ (Bolzonella et al. 2000), EAZY (Brammer et al. 2010), LePHARE (Ilbert et al. 2006) and BPZ (which also incorporates priors through a Bayesian method; Benítez 2000). The template fitting algorithms used in this thesis are LePHARE and a Bayesian Model Averaging (BMA) code. Thus we describe them in more detail below.

**Machine learning** (ML) techniques attempt to determine a mapping from colour space to redshift through training on spectroscopic data. The mapping can be reproduced with a simple polynomial fit (Connolly et al. 1995) or through more complicated relations, such as those arising from artificial neural networks (ANNs). Examples of codes using neural networks are ANNz (Collister & Lahav 2004), ANNz2 (Sadeh et al. 2016) and skynet (Graff & Feroz 2013), while TPZ (Carrasco Kind & Brunner 2013) uses random forests.

One of the main concerns with machine learning derivation of redshifts for deep photometric surveys such as DES is the incompleteness of the training sample. This relates to the incompleteness of the spectroscopic data, in other words to the unrepresentativeness of the galaxies from photometric data. This is a particular problem towards the faint end of galaxy samples, where there is a lack of spectroscopy. Several studies have tried to mitigate this problem, for example through means of galaxy colours weighting (Lima et al. 2008). On the other hand, with template–fitting methods one needs to be careful that the library used is representative for the observed data, and that synthetic SEDs are realistic.

As far as we are concerned, machine learning methods have been extensively used to estimate redshifts from photometric data, but not other parameters that go into the galaxy evolutionary modelling described in the previous Section. Principal Components Analysis (PCA) and machine learning techniques have been applied to spectroscopic data (e.g. Chen et al. 2012), in particular to solve classification problems (e.g. Teimoorinia et al. 2016), and for morphological studies (Gauci et al. 2010; Schutter & Shamir 2015). We decided to apply for the first time a machine learning method to estimate stellar mass from photometric surveys. The same method could ideally be applied to any other quantity that can enters the evolutionary synthesis models.

In this thesis we have used ANNz2, thus we explain this method in more detail below, along with the template fitting methods LePHARE and BMA.

In this Section we describe the methods used in this thesis as SED fitting methods,
rather than simply photo-z estimation codes, as we use them to derive galaxy properties beyond the photo-z’s.

2.3.1 LePhare

The main purpose of LePhare (PHotometric Analysis for Redshift Estimation) is to compute photometric redshifts by comparing template SEDs to the observed broadband photometry, but it can also be used to calculate physical parameters such as stellar masses and rest-frame luminosities. Several spectral libraries, both theoretical and empirical, are available within the code (including Coleman et al. 1980, Poggianti et al. 2001, Bruzual & Charlot 2003), and these are redshifted and integrated through the instrumental transmission curves. Additional contribution of emission lines in the different filters can be included and extinction by dust can be taken into account. The synthetic colours obtained from the SEDs for each redshift are then compared to the data. The best fitting template and redshift for each object is then found by $\chi^2$ minimisation as described above for a generic template fitting method. In addition, prior information can be supplied, including a photo-z distribution prior by galaxy type computed from the VVDS survey in the $i$ band (see Ilbert et al. 2006).

Previous works on DES photo-z’s have tested the performance of this code in comparison with other softwares and spectroscopic redshifts. In particular, Sánchez et al. (2014) found that LePhare fulfils the DES requirements on scatter and $2\sigma$ outlier fraction when it is run on SV data, and the metrics obtained are compatible with those from other template-based methods within 10%.

This method is used in the results section of this Chapter (Section 2.4) to compare stellar mass estimates from a novel, machine learning method to this more traditional algorithm. LePhare is also the method adopted in Chapter 3 to perform the SED fit of the GW170817 host galaxy (fixing the redshift, to estimate galaxy properties), and in Chapter 4 to estimate photo-z’s and stellar masses for the galaxy cluster RXJ2248.

2.3.2 Bayesian Model Averaging algorithm

A major cause of uncertainty in stellar mass estimation from broadband photometry is in the model assumptions (see e.g. Mitchell et al. 2013) that are needed in model fitting techniques. These assumptions mainly involve redshift, star formation history (SFH), the initial mass function, the dust content and the knowledge of stellar evolution at all stages.
When developing our BMA algorithm, we therefore chose not to ignore the uncertainty on model selection and use a set of robust, up-to-date stellar population synthesis (SPS) models and average over all of them, marginalising over the model uncertainty. The method used for this purpose is called, indeed, Bayesian Model Averaging (see e.g. Hoeting et al. 1999). BMA has already been successfully applied to galaxy SED fitting parameter estimation in Taylor et al. (2011).

Our code can be used to estimate physical parameters of galaxies (stellar masses, specific star formation rates, ages, metallicities) as well as cluster stellar masses and total SFR (when provided with cluster membership probabilities), and it is publicly available at https://github.com/palmese/BMAStellarMasses. We provide some validation test results for this method in this subsection, while performance tests of the other SED fitting codes presented are widely presented in the relevant papers.

The BMA starting point is Bayes’ theorem, through which we can write the posterior probability distribution \( p(\bar{\theta}_k|D,M) \) of the set of parameters \( \bar{\theta}_k \) given the data \( D \) and the model \( M_k \):

\[
p(\bar{\theta}_k|D,M_k) = \frac{p(D|M_k,\bar{\theta}_k)p(\bar{\theta}_k|M_k)}{p(D|M_k)}, \tag{2.8}
\]

where \( p(D|M_k,\bar{\theta}_k) \) is the likelihood, \( p(\bar{\theta}_k|M_k) \) is the prior probability of the parameters given the model \( M_k \), and \( p(D|M_k) \) is the evidence.

The model averaged posterior distribution of the parameters \( \theta_k \) is given by the sum of the single model \( M_k \) posteriors, weighted by the model prior:

\[
p(\bar{\theta}_k|D) = \sum_k \frac{p(\bar{\theta}_k|D,M_k)p(M_k)}{\sum_k p(M_k|D)} . \tag{2.9}
\]

From BMA it also follows that the posterior distribution of a quantity \( \Delta \) is the average of the single model posteriors for that quantity, weighted by their posterior model probability:

\[
p(\Delta|D) = \sum_k p(\Delta|D,M_k)p(M_k|D) . \tag{2.10}
\]

The posterior model probabilities can be computed by:

\[
p(M_k|D) = \frac{p(D|M_k)p(M_k)}{\sum_k p(D|M_k)p(M_k)} , \tag{2.11}
\]
where
\[
p(D|M_k) = \int p(D|M_k, \bar{\theta}_k)p(\bar{\theta}_k|M_k) d\bar{\theta}_k.
\] (2.12)

In our case \( p(\bar{\theta}_k|M_k) \) is simply a delta function, as the parameters \( \bar{\theta}_k \) (i.e. the SFH parameters, metallicities, etc.) fully define our models \( M_k \).

From eq. 2.12 one can write:
\[
\langle \Delta \rangle = \sum_k \bar{\Delta}_k p(M_k) L_k,
\] (2.13)

where \( \bar{\Delta}_k \) is the mean \( \Delta \) value from the model \( M_k \). \( L_k \) is the likelihood \( p(D|M_k) \) that we will reconstruct from the \( \chi^2 \) distribution.

In our code, the mass-to-light ratio \( M_*/L \) is the quantity \( \Delta \). Its posterior mean over all the models considered is then used to estimate the stellar mass \( M_* \) of each single galaxy through:
\[
\log(M_*/M_\odot) = \langle M_*/L \rangle - 0.4(i - DM + \langle kii \rangle - 4.58),
\] (2.14)

where \( \langle M_*/L \rangle \) is the weighted mean stellar–mass–to–light–ratio in solar mass units, \( i \) is the observed \( i \) band magnitude, \( DM \) is the distance modulus, \( \langle kii \rangle \) is the weighted mean of the K-correction \( i_{\text{rest frame}} - i \) and 4.58 is the \( i \)-band absolute magnitude of the Sun. Weighted means are considered over all models.

In this thesis we use the flexible stellar population synthesis (FSPS) code by Conroy & Gunn (2010) to generate simple stellar population spectra. Those are computed assuming Padova (Girardi et al. 2000b, Marigo & Girardi 2007, Marigo et al. 2008) isochrones and Miles (Sánchez-Blázquez et al. 2006) stellar libraries with four different metallicities \((Z = 0.03, 0.019, 0.0096 \text{ and } 0.0031)\). We choose the four-parameter SFH described in Simha et al. (2014):
\[
SFR = \begin{cases} 
A(t - t_i)e^{(t - t_i)/\tau} & \text{if } t < t_i \\
SFR(t_i) + \Gamma(t - t_i) & \text{otherwise}
\end{cases}
\]
where \( t_i \) is the time at which star formation commences, \( t_i \) is the time when the SFR transitions from exponential to a linear fall off, \( \tau \) is the exponential time scale, and \( \Gamma \).
2.3. Methods

Validation of the BMA method

In order to test our method for stellar mass estimation, we use as reference a catalog that overlaps with DES observations and has been proven to provide robust stellar mass estimates. Laigle et al. (2016) used LePHARE to compute stellar masses with multiband data in 16 filters from UV to infrared over the 2 deg² COSMOS field. From this sample, matched to DES data, we cut all objects at \( z = 0 \) to eliminate stars, and at \( z > 1.5 \), as we do not expect DES to be able to estimate stellar masses beyond that value. Galaxies with \( i \)-band magnitude above 23.0 are also cut out. The remaining sample comprises galaxies
with $SNR > 10$ in DES, for which we compute stellar masses using the BMA code run with the DES photometry. The bias distribution given by the difference in log galaxy stellar mass between the two samples $\log(M_{\text{COSMOS}}) - \log(M_{\text{BMA}})$ is shown in Figure 2.3. Mean bias and scatter (that we quantify as the standard deviation of the distribution) are below the typical error on galaxy stellar masses from SED fitting ($\sim 0.2$ dex) in the redshift range $0.2 < z < 0.6$, where we expect good performance for optical surveys such as DES. At higher redshift, it is harder to constrain the optical to near-infrared (NIR) SED with the DES bands and therefore the scatter increases. Also at low redshifts ($z < 0.2$), the 4000Å break is harder to constrain, as it is blue-ward of the $g$-band effective wavelength. The scatter will also be partially due to the fact that the COSMOS stellar masses are not “true” stellar masses, and will depend on the assumptions and methodology in Laigle et al. (2016). The slight bias that seems to exist in the stellar masses we computed with the BMA algorithm and DES photometry, particularly towards higher redshift, is probably due to the degeneracies between stellar mass and dust extinction. Laigle et al. (2016) are able to constrain dust extinction better than in this work because of the information brought by the infrared data available to them.

2.3.3 ANNz2

ANNz2 (Sadeh et al. 2016) is an updated version of the neural network code ANNz (Collister & Lahav 2004). ANNz2 differs from its previous version by incorporating several additional machine learning methods beyond Artificial Neural Networks (ANNs), such as Boosted Decision Trees (BDTs) and $k$-Nearest Neighbours (KNN) algorithms. These are implemented in the TMVA package (Hoecker et al. 2007).

ANNs have been shown to have competitive performances for photo-$z$ estimation compared to other machine learning methods (Firth et al. 2003), and therefore we use ANNs in the DES photo-$z$’s production. A neural network is made up of several layers, and each layer is composed by nodes. The number of nodes and layers depends on the chosen architecture. The inputs of the first layer are the observed magnitudes, colours, or any other galaxy property that could add information for redshift estimation. The output is the photo-$z$, or any other quantity that has been trained. In the multi–layer perceptron method, which is implemented in ANNz2 in ANN method, responses from each neuron

\[3\text{https://github.com/IftachSadeh/ANNZ}\]

\[4\text{TMVA is a part of the ROOT C++ software framework (Brun & Rademakers 1997)}\]
of a layer are fed onto the following layer, and so on from input to output levels. Each response is fed with a weight, which is varied from cycle to cycle depending on the error function, which quantifies the amount of error in predicting the output when compared to the target value.

The code can be run in a mode called “randomised regression”, that allows to vary the input parameters of the chosen machine learning method. For example, when we use ANNs we usually randomly vary: the number of nodes in each layer, the number of training cycles, the usage of the so-called Bayesian regulator, that reduces the risk of over-training, the type of activation function, the type of variable transformation performed before training (such as normalisation and PCA transformation) and the initial random seed. After training is complete, the performance of each method is quantified through an optimisation process, which leads to a single nominal photo-z estimator for ANNz2. The entire collection of solutions is used in order to derive a $p(z)$, constructed in two steps. First, each solution is folded with an error distribution, which is derived using the KNN error estimation method of Oyaizu et al. 2008. The ensemble of solutions is then combined using an optimised weighting scheme. This methodology allows us to take into account both the intrinsic errors on the input parameters for a given method, and the uncertainty on the method itself. Another important feature implemented in ANNz2 is the weighting method (Lima et al. 2008). It is therefore possible to give in input a reference sample and re-weight the training set to make its relevant variables distributions more representative of the former.

Within this thesis, ANNz2 is only used in this Chapter to estimate DES SV photo-z’s (Section 2.4.1), and DES galaxies’ stellar masses (Section 2.4.2).

2.4 Applications for cosmology and galaxy evolution

2.4.1 DES Science Verification photo-z’s

In order to train ML methods and test their performance, we need a sample of galaxies with a measured spectroscopic redshifts that can be matched to DES photometry. This has been done in a comprehensive way within the DES photo-z group for SV data, so that all algorithms would be trained and tested on the same sample. The final spectroscopic set comprises of $\sim 48,000$ galaxies spread over six fields in the sky, with measurements from 20 different surveys. This catalogue has been cleaned of objects that we do not expect
Figure 2.4: Redshift distributions (arbitrarily renormalised) of the spectroscopic sample used for training, validation and testing of DES SV photo-$z$’s. The top panel shows the distribution for training and validation samples, the middle panel for the independent testing sample from the VVDS F–14 field, and the the lower panel for an additional testing sample that goes to deeper magnitudes than the other fields (not mentioned in this work). From Bonnett et al. (2016).

to be present in the DES galaxy catalogue (such as stars and AGNs), making sure that it is representative of the galaxies sample for which we want to evaluate the photo-$z$’s. A full description of the matched spectroscopic sample is presented in Appendix A of Bonnett et al. (2016). This sample is split into training, validation and testing sample. In particular, the testing sample is independent from the training and validation sets in the sense that it comes from a separate field in the sky (the VVDS F–14), and thus its line of sight structure is uncorrelated from the other fields. This feature ensures that performance metrics evaluated on this sample would reveal redshift estimates that suffer from incompleteness of the training sample or that have been overtrained. Overtraining occurs when a ML algorithm becomes sensitive to fluctuations in the training data, rather than to actual features of the observables. This results in an apparent improvement of the performance metrics computed on the training sample, but it can be identified from a poorer performance on an independent testing sample. Overtraining can also be avoided through convergence tests, which are available within the ANNZ2 code. These tests check whether the error estimator on training and validation samples have not improved over the last training cycles. The spectroscopic redshift distributions of the training, validation
and testing samples are shown in Figure 2.4.

Several template fitting and machine learning methods have been used by the DES photo-z working group on SV data. Four of them, namely ANNz2, bpz, skynet and tpz, have been used in Bonnett et al. (2016) to estimate the impact of redshift distributions on cosmological parameters, in Leistedt et al. (2016) to infer the impact of spatial systematics on redshift distributions, and in Abbott et al. (2016c) for cosmological analysis with cosmic shear. I have used ANNz2 to produce the photo-z’s used in these analysis and released at https://des.ncsa.illinois.edu/releases/sva1. The training has been performed in randomised regression mode for 100 ANNs, using as inputs the MAG_AUTO magnitudes in griz bands from the SVA1 gold catalogue. During training, the samples that we previously defined for training and validation are used. The testing sample is used to estimate metrics after the training is complete.

The weighting method mentioned in Section 2.3 has been applied before the training. The key point of this method is to give more significance to training data which is
representative of the population for which we want to compute the redshift. In Figure 2.5 we show the original magnitude distributions from DES photometry matched to the spectroscopic training sample (pink squares). The purple data points show the effect of the weighting using as a reference sample the DES SVA1 gold galaxy catalogue (black histogram). It is clear how magnitude $\sim 19$ objects would have too high significance in the training: without the weighting assignment, the final redshift distribution (and the single galaxies’ PDF) would present a spurious peak corresponding to those magnitude $\sim 19$ galaxies, which are around $z \sim 0.2$ in Figure 2.4. DES collaborators Lima et al. (2008) have comprehensively explored the effect of the weighting on the recovered $\Delta n/\Delta z$, finding that this method performs well even when the spectroscopic sample is not very representative of the photometric sample magnitudes (see for example the $g$ band magnitude distributions at $g > 25$ in Figure 2.5). Those results are based on KS tests of the recovered versus true redshift distributions and outlier fractions, when this method is compared to other traditional photo-z estimation methods on data and simulations. A correction factor is thus assigned to each galaxy depending on the input magnitudes. This is given by the number of neighbours in magnitudes-space in the training sample over the number of neighbours in the reference sample, both calculated within a set distance. Distances in magnitude space are simply Euclidean distances.

For this reason, dedicated catalogs need to be separately evaluated depending on the scientific analysis. We have produced dedicated catalogs for weak lensing and large scale structure (LSS) studies. The weak lensing catalog used for cosmic shear analyses typically has magnitude and redshift distributions comparable with the full gold samples for SV and Y1 releases. For example, the LSS Y1 sample is bright, as it has a sharp cut at $i < 21$.

We have tested the use of the inTrainFlag computed within ANNs2. We provide this flag as part of our catalogs to identify galaxies that fall into incomplete regions of the training sample in the magnitude space. The photo-z’s associated with low values of this flag are found in underrepresented regions of the magnitude space, and thus their redshift is not reliable. Metrics have been computed on data and simulations as a function of this flag, and we find that a conservative cut that satisfies the DES requirements on bias and scatter is inTrainFlag $> 0.7$. This flag, together with the weighting method, constitute our solution to incompleteness and unrepresentativeness of the training sample.

Objects that have an unobserved band, have been treated as faint objects and considered at the mean magnitude limit for each filter (namely 24.67, 24.21, 23.78, 23.10 in
2.4. Applications for cosmology and galaxy evolution

Figure 2.6: Redshift distributions of the different ANNz2 photo-z estimators (coloured data points), compared to the target distribution from the weighted SV testing sample.

Figure 2.7: Performance metrics of the ANNz2 estimators on the weighted testing sample. The metrics are, from left to right: bias, scatter (the standard deviation $\sigma$ and the 68th percentile $\sigma_{68}$ of the bias distribution) and outlier fraction. The outlier fractions are defined outside twice and three times the scatter values.

Normalised redshift distributions and performance metrics on the testing sample for the different ANNz2 redshift estimators are shown in Figures 2.6 and 2.7, respectively. **ANNZ_BEST** is the single-value solution from the ANN that performed the best out of the 100 ANNs, **ANNZ_MLM_avg** is the average of the solutions from all ANNs, **ANNZ_PDF_avg** is the single-value average of the full PDF solution, as computed from the randomised regression, and **ANNZ_PDF_max** is the PDF maximum value. Based on the performance metrics, which are lowest in bias and scatter, we decide to use **ANNZ_PDF_avg** as the photo-z nominal value.

Abbott et al. (2016c) present the first cosmological constraints from DES SV data,
Figure 2.8: Impact of the photo-z catalogue choice on the $\sigma_8$ and $\Omega_m$ constraints. The constraints on $S_8$ computed from the different catalogues shift by less than two thirds of the errorbar. From Abbott et al. (2016c).

using shear 2-point measurements over 3 redshift bins. They find $S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5} = 0.81 \pm 0.06$. Figure 2.8 shows the impact of the photo-z catalogue choice on the $\sigma_8$ and $\Omega_m$ constraints. Excellent agreement is found between the different codes, with the ML methods providing very similar results (note that they are trained on the same spectroscopic sample, and therefore they are not truly independent). BPZ is the only template fitting method presented, and it shows the largest difference compared to SKYNET (which is taken as the SV fiducial photo-z). However, in all cases the constraints on $S_8$ shift by less than two thirds of the errorbar.

2.4.2 Stellar masses with machine learning

In this subsection we present a new approach to derive galaxy stellar masses from multi-band photometric data using machine learning. It is faster by a factor of $\sim 100$ compared with standard template-fitting methods, and it allows to incorporate information from external higher quality data, therefore achieving similar, if not improved, performance. Machine learning, which in this context can be viewed as an interpolation method, has been largely adopted in galaxies’ redshift estimation, as outlined in the above, but has never been used to estimate stellar masses from photometric data.
Method

By using the Laigle et al. (2016) COSMOS-based catalogue as a training set, which includes accurate stellar mass estimates based on a large number of broadband filters (see Section 2.3.2), we train ANNz2 using DES photometry. We use LePhare as a reference template fitting code, because this is also the method adopted by Laigle et al. (2016) and this choice provides a fair performance comparison with ML.

The sample is cut in redshift, eliminating all objects at $z = 0$ to remove stars, and at $z > 1.5$, as the DES filter coverage does not typically allow to measure galaxy properties beyond this redshift. Galaxies with $i$-band magnitude above 23.0 are also removed. The remaining galaxies are matched to DES Year 1 photometry, which has $S/N > 10$ after the selection cuts described. The training and testing samples are formed of $\sim 20,000$ galaxies with observed $griz$ bands randomly selected from the matched COSMOS-DES catalog. The rest of the catalogue ($\sim 20,000$ galaxies) is used for testing.

The input variables provided to ANNz2 are DES $\text{MAG\_AUTO}$ $griz$ magnitudes, and COSMOS photo-z’s. ANNz2 is run in single (i.e. only one ML method is run, with a single set of initial parameters) regression mode with BDTs, as ANNs run on this sample show biases due to a back propagation issue: too much weight was allowed to be given to the redshift, that strongly correlates with the mass.

The template fitting evaluation was performed with LePhare and a set of 20 SPS templates from Bruzual & Charlot (2003). The templates were chosen in order to be as similar as possible to the set used in Laigle et al. (2016).

Results

The stellar masses estimated with LePhare show a mean of the bias distribution of $\Delta = -0.051 \pm 0.002$ dex and a scatter $\sigma = 0.32 \pm 0.01$ dex on the testing sample. A single random forest run with ANNz2 has $\delta = -0.006 \pm 0.001$ and $\sigma = 0.31 \pm 0.02$ dex. A comparison with the COSMOS catalogue masses (i.e. our “true” values in the testing sample) is shown in Figure 2.9. The performance is very similar, even with a lower bias from ML estimates. Given that the template fitting was performed in an almost identical fashion as in Laigle et al. (2016), we believe that the higher bias found in the LePhare results (as opposed to the ML method) is due to a lack of filters in the DES data compared to COSMOS. Machine learning techniques show a better control as they are able
to incorporate information from the COSMOS data through training. Computing times are \(\sim 100\) times quicker with ANNz2 than with LePHARE, providing an ideal method to compute stellar masses in a binned range of redshift, and obtain in a reasonable time full stellar mass PDFs. The idea behind this approach is that ML acts as an interpolation method between the different stellar population synthesis models, and can “learn” quickly prior information contained in more sophisticated photometric or spectroscopic surveys.

Further tests of this method concern the inclusion of morphological parameters in the input variables. Soo et al. (2018) show that there is room for improvements on photo-z estimation when morphological information is added to photometric data from less than 5 bands. We therefore utilise morphological and photometric information from Multi-Object Fitting (MOF) pipeline that uses the \texttt{ngmix} code\(^5\) available for the same galaxy sample used here. However, we find that the inclusion of galaxy size and light profile type (through the MOF outputs \(T^6\) and \(\text{fracDeV}^7\)) does not improve upon the performance. A

\[\text{Log}(M_\star[M_\odot])(\text{DES})\]

\[\text{Log}(M_\star[M_\odot])(\text{COSMOS})\]

Figure 2.9: Stellar masses computed with boosted decision trees using DES 4–bands photometry, compared to the COSMOS stellar masses from Laigle et al. (2016) evaluated with LePHARE and 16–filters photometry. The COSMOS stellar masses represent our “true” values in the testing sample shown here.

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\(^5\)https://github.com/esheldon/ngmix

\(^6\)The size squared of the object.

\(^7\)In the MOF composite model, the light profile is fit to a de Vaucouleurs plus exponential model. The
2.5 Conclusions

In this Chapter, we have reviewed the basic concepts behind photometric redshift estimation and galaxies’ SED modelling. The SED fitting techniques used in this thesis have been described. We have then shown some applications of the methods to DES data. In particular, we have described how the ANNz2 photo-z’s catalogue for the DES SV release has been produced, and how machine learning can be applied to DES data for stellar mass estimation. The approach presented allows to incorporate information from fraction of the light profile which follows a de Vaucouleurs profile is given in \( \text{fracDeV} \).

\( \sim 20\% \) improvement on the bias is found only thanks to the improved MOF photometry when compared to the SExtractor \texttt{MAG\_AUTO} magnitudes.

We conclude that this approach to stellar mass computation is promising, and we have computed a first catalog for DES Year 1 data using this method. Assuming BPZ photometric redshifts and MOF photometry, we recovered stellar masses over the Y1 wide field footprint of \( \sim 1,800 \text{ sq. deg.} \), shown in the mass map in Figure 2.10. Future work will use a cross-correlation of stellar mass maps with weak lensing maps to constrain the stellar–to–halo mass relation.

Figure 2.10: Top: Stellar mass map over the DES Year 1 wide field. It comprises galaxies with redshift \( 0.2 < z < 0.4 \). Bottom: Weak lensing convergence \( \kappa \) mass map by Chang et al. (2018) for sources at \( 0.6 < z < 0.9 \) (E modes). The cross-correlation of this mass map with the stellar mass map of foreground galaxies produces a signal which can be used to study the stellar–to–halo mass relation.
external higher quality data, and achieving similar, if not improved, performance compared to traditional methods. The method is also significantly quicker than others (∼100 times quicker than LePhare), which is useful when dealing with large photometric surveys such as DES, and we predict that it will allow us to produce full stellar mass PDFs in a reasonable time.

In future analyses, we plan on studying cross-correlations of stellar mass maps, computed with machine learning techniques on DES Year 3 data, with weak lensing mass maps. By predicting a convergence mass map, which can be defined by an adaptation of Utsumi et al. (2016), from our observed “stellar convergence” $\kappa_*$ map, we will fit a stellar–to–halo mass relation to weak lensing observations. This measurements will provide insights on the distribution of stellar matter relative to dark matter, and on the relative contribution of these components also outside galaxy clusters (which are discussed in Chapter 6).
The work presented in this Chapter is an extended version of Palmese et al. 2017, ApJ 849L, 34P, with some information from the GW170817 DECam discovery paper Soares–Santos et al. 2017, 848, L16 and work done as part of the DECam–GW follow up program yet to be published. The DECam–GW pipeline is shortly described in Herner et al. 2017 and has been used in the GW170814 analysis by Doctor et al., in preparation. I am an author or co-author in all of the works listed above. Some information from the earlier work on DECam GW follow ups are also presented (from Soares-Santos et al. 2016 and Cowperthwaite et al. 2016).

The first identification of the electromagnetic counterpart (LIGO Scientific Collaboration et al. 2017) of a gravitational wave (GW) signal (Abbott et al. 2017a) marks the beginning of a new era for multi-messenger astronomy. More than 3000 physicists and astronomers from all around the globe probed every aspect of the event, across the electromagnetic
spectrum and into the realms of gravity theories and particle physics. Amongst the several expected transients described in Chapter 1, the coalescence of neutron stars is expected to have strong optical and near-infrared signatures in the form of a kilonova, the ejecta from which are heated by the decay of heavy nuclei produced via $r$-processes. The optical counterpart to the BNS coalescence signal GW170817 was discovered independently by several collaborations using optical telescopes, including the Dark Energy Camera GW team (Soares-Santos et al. 2017).

In this Chapter we exploit galaxy catalogs for follow ups of gravitational wave events, focusing on the follow up of the DECam golden event GW170817. We show how deriving properties of galaxies, including redshifts, stellar masses and star formation rates, from photometric and spectroscopic surveys can boost our GW EM follow up strategy and understanding of GW sources. We start by presenting the DECam–GW follow up program in Section 3.1, focusing on the galaxy host matching of candidates which has been my main task within the follow up effort. In Section 3.3 we describe a study of NGC 4993, the host galaxy of the GW170817 GW event, the GRB170817A short gamma–ray burst (sGRB) and the AT2017gfo kilonova. We use Dark Energy Camera imaging, AAT spectra and publicly available data, relating our findings to binary neutron star (BNS) formation scenarios and merger delay timescales. NGC4993 is a nearby (40 Mpc) early–type galaxy, with $i$-band S´ersic index $n = 4.0$ and low asymmetry ($A = 0.04 \pm 0.01$). These properties are unusual for sGRB hosts, usually showing higher asymmetry. However, NGC4993 presents shell–like structures and dust lanes indicative of a recent galaxy merger, with the optical transient located close to a shell. We constrain the star formation history (SFH) of the galaxy assuming that the galaxy merger produced a star formation burst, but find little to no on–going star formation in either spatially–resolved broadband SED or spectral fitting. We use the best–fit SFH to estimate the BNS merger rate in this type of galaxy, as $R_{NSM}^{gal} = 5.7^{+0.57}_{-3.3} \times 10^{-6}$ yr$^{-1}$. If star formation is the only considered BNS formation scenario, the expected number of BNS mergers from early–type galaxies detectable with LIGO during its first two observing seasons is $0.038^{+0.004}_{-0.022}$, as opposed to $\sim 0.5$ from all galaxy types. Hypothesising that the binary system formed due to dynamical interactions during the galaxy merger, the subsequent time elapsed can constrain the delay time of the BNS coalescence. By using velocity dispersion estimates and the position of the shells, we find that the galaxy merger occurred $t_{mer} \lesssim 200$ Myr prior to the BNS coalescence. Note that in this work we may use the word “merging” for both the galaxy merging and the
3.1 Gravitational wave follow up with DECam

A subset of GW events are expected to produce an electromagnetic (EM) emission that once detected, can provide information complementary to the waveform. Observing the EM counterparts offer a number of exciting scientific opportunities for cosmology and astrophysics, as we have described in Chapter 1. It is worth stressing that follow ups of BBH events are interesting even though most accepted BBH merger models do not predict an EM counterpart, as they lack the massive accretion disks expected to produce GRBs and other observable transients (e.g. Annis & Soares-Santos 2016 and references therein). However, there exist theoretical models that could produce an EM signal (e.g. Loeb 2016, de Mink & King 2017): these are highly speculative, and assume the presence of matter around the binaries in the form of circum–binary disks, or mergers happening within another star. There are three (not mutually exclusive) reasons for non-detections: (1) the probable sky regions of previous BBH detections were not searched comprehensively, (2) the BBH emission could not be distinguished from background transients, and/or (3) emission from BBH mergers is below the detectable threshold of current instruments. The possibility of (1) and (2) implies that detectable BBH emission cannot yet be ruled out, and placing upper limits on the emission provides interesting constraints on theoretical models of BBH mergers.

With these benefits in mind, the Ligo–Virgo Collaboration (LVC) established partnerships with several collaborations around the globe, including DECam. Shortly after their first analysis of the GW signal, LVC shares with the partner collaborations a number of useful information, including the estimated distance to the source, the type of event (BBH, BNS, BH+NS mergers) and a map of the probability for the source of the event to be located in different positions of the sky. The LVC trigger information are communicated through a private network to the EM follow up partners, similarly to what is used in the gamma–ray community. The partner collaborations then decide whether to follow up the candidate, depending on factors such as the observability of high probability regions of the skymap from their telescope. Our EM follow up group consists mainly of DES members, and some external collaborators from the astronomical community, so that the program was named DECam–GW program. At present, DES is one of the primary users...
of DECam, and the DECam–GW team obtained \( \sim 4 \) nights of telescope time per year over the past two observing seasons, to be added to the DES allocation of \( \sim 105 \) nights per year. When a LVC trigger is received, the team uses dedicated observing strategy codes to decide whether to observe the event. If the decision is positive, DES observations are interrupted to start the follow up. The LVC might update their analysis of the event later on, resulting in a new skymap. If this happens while the follow up observations are still on, we modify our observing strategy accordingly.

### 3.1.1 Observing strategy

The observing strategy is mostly optimised to catch the EM emission expected from BNS merger models. These predict that the EM counterpart will fade in a matter of days to a week time from the GW trigger. It is therefore crucial to quickly identify, analyse and eventually report candidates for further photometric and/or spectroscopic follow up. Clearly, DECam represents a premier instrument in the Southern emisphere to achieve these goals, given its wide and unique field of view. A general rule is to observe candidates three times: once as soon as possible after the trigger, 2 or 3 days later and about two weeks later, in order to observe the decline in flux of potential kilonova events. The first steps in planning the observations once the trigger is received consist in (i) produce expected 10\( \sigma \) limiting magnitude maps for the following 24 hours for 90 seconds exposures, (ii) calculate source detection probabilities for those maps and (iii) select pointings to be observed based on these probabilities. This is done for time slots of \( \sim 1/2 \) hour. The source detection probabilities are computed given the limiting magnitudes from (i) and a source model. At present, we do not have a realistic model for BBH EM and we just assume that the source has an apparent magnitude of \( i = 20 \). The kilonova model used for BNS and BH+NS events is a modified version of the model by Barnes & Kasen (2013). The detection probability maps are divided into DECam pointings, and time slots of roughly half an hour containing an integer number of pointings are created. The exposures are taken in \( i \)–band for BBH follow up and in an \( i zz \) sequence for NS mergers, given that we expect kilonovae to emit in the optical–near infrared. This is done for all available time slots, and it is repeated for the following available nights.
3.1 Image processing

Once the images have been taken, they are processed through the difference imaging pipeline, initially developed for supernovae searches with DES by Herner et al. (2017). Supernova light curves are typically very similar to what we expect a kilonova to look like from our DES photometry, just bluer and brighter. It is thus natural to borrow some methods from SN searches. The difference imaging consists in subtracting from the new follow up images the “templates”, which are DECam images of the same area of the sky taken previously to the event. We search for new objects in the residual images obtained, which constitute our potential candidate transients. This pipeline is able to use as templates partially overlapping exposures, and also publicly available images taken with DECam outside of the DES allocated time. In particular, part of us in the DES-GW team are also involved in the BLanco Imaging of the Southern Sky (BLISS), a dedicated program aimed at providing templates in the whole observable southern sky (along with other science cases). BLISS has already observed 1000 deg$^2$ of the DECam observable sky in griz which had not previously been covered.

3.1.3 Post-processing

After the images have been processed, we assess the outputs and create a candidate list to analyse. An important step consists in rejecting non-astrophysical artifacts that may arise from the difference imaging, for example close to CCD edges. This is achieved by classifying the candidate transients through a machine learning method that assigns a score between 0 (high probability of being an artifact) and 1 (high probability of being a real object). So far in the analyses we have assumed a cut in the score at $\geq 0.7$, where the efficiency of this cut was measured from point sources injected into our images to be $\gtrsim 90\%$ in both $i$ and $z$ up to $z = 22$. Depending on the type of event, one may want to apply other cuts to the list of transients. The next step consists into rejecting the most likely contaminants to kilonova events: Supernovae (SN).

SN rejection and host matching

The light curve (i.e. the flux as a function of time) of a SN may look similar to a closer kilonova, given that the latter is meant to be redder and dimmer. One plausible way of rejecting supernovae in a kilonova search consists in requiring that the observed flux of
candidates has significantly declined within the first weeks from the trigger (e.g. Soares-Santos et al. 2016 require $S/N < 3$ at 24 days), given their longer lightcurve lifetime. This cut will not exclude all the SN, especially those that exploded prior to the trigger. Assuming that those SN happen in galaxies, we identify those contaminant transients by matching them to galaxies, and associating the host galaxy redshift to the SN. If the SN is too far to be detected by the GW experiment, we identify it as a SN reject it as a contaminant. This is achieved by constructing a dedicated galaxy catalog with redshifts and morphological information over the whole DECam observable sky (i.e. the whole southern sky up to a declination of 30 deg) and defining a host matching method. In our catalog we include galaxies out to redshift $z < 0.4$, as that is the furthest distance we would be able to see a SN given the DES-GW strategy for 90 second exposures and a typical $i-$band absolute magnitude at the peak of the SN lightcurve of $-19$. Host galaxies are searched for in a catalog containing Y3Q2 DES data with LePHARE photo-zs that I have computed using MAG_AUTO magnitudes and errors. These galaxies are complemented with 2MASS and SDSS galaxies available in the southern sky. Our host matching script queries the relevant DES Easyaccess database table to obtain transient coordinates which are then matched to potential host galaxies. The search is done for each candidate in the HEALPix\(^1\) pixel at its position and all the 8 adjacent pixels. Our matching script searches within a 15 arcsec radius from the transient position and ranks all sources according to

\(^1\)http://healpix.sourceforge.net
3.1. Gravitational wave follow up with DECam

Figure 3.2: Probability sky map from LIGO containing 90 and 50% of the probability for the EM counterpart location (solid lines for the updates version, dashed for the first skymap) for GW150914 (left), GW151226 (middle) and GW170817 (right). Red hexagons are the DECam pointings taken as part of the follow–up program. The yellow point in the right hand side panel indicates the position of the kilonova. From Soares-Santos et al. (2016), Cowperthwaite et al. (2016) and Soares-Santos et al. (2017) respectively.

their dimensionless separation from the transient $d_{\text{DLR}}$, which is in units of directional light radius (DLR):

$$d_{\text{DLR}} = \frac{\text{galaxy} - \text{transient angular separation (arcsec)}}{\text{DLR (arcsec)}},$$

(3.1)

where the DLR is the elliptical radius of a galaxy in the direction of the SN in units of arcseconds. The DLR is computed from some basic morphological quantities from SExtractor: $A_{\text{IMAGE}}, B_{\text{IMAGE}}$ and $\text{THETA}_{\text{IMAGE}}$. These are respectively, the profile RMS along the major and minor axis, and the position angle of the major axis.

This method has already been used for SN searches by Gupta et al. (2016). In Figure 3.1, the DLR for each galaxy is represented by the blue arrows. The maximum value allowed for the $d_{\text{DLR}}$ is 4, if no galaxy meets these requirements the candidate is flagged as hostless. If one or more galaxies satisfy this condition, they are assigned a DLR_RANK depending on their $d_{\text{DLR}}$: the lowest $d_{\text{DLR}}$ gets a rank of one, and so on up to rank 3, galaxies that are further than the third are excluded. The results are output to a text file and written to the DES database SNGALS table.

At present we have not put any cut at low redshift for the SN host matching catalog, and therefore matches output from the same code can be used to match potential GW counterparts to host galaxies by separating the matches depending on their redshift, and on the maximum redshift at which the counterpart can be as provided by LIGO.
3.1.4 Results from past observing seasons

During the first LIGO observing season we followed up the two BBH events GW150914 (Soares-Santos et al. 2016; Annis et al. 2016) and GW151226 (Cowperthwaite et al. 2016). Neither of the searches found a credible EM counterpart, as all candidates were rejected as background. This result is not surprising, given that (1) we do not expect an EM counterpart to BBH mergers and (2) the observed area was relatively small (11% and 3% of the LIGO BAYESTAR updated probability map). The large 90% probability region is clear in Figure 3.2. During the second observing run, joint detections from LIGO and Virgo were able to reduce these regions by roughly one order of magnitude, from thousands/hundreds of sq. deg. to hundreds or tens. O2 was a lot more fortunate for the DECam-GW program: we were able to follow up two golden events triggered within 3 days, GW170814 and GW170817, both having 90% probability regions fully within the DECam observable sky. GW170817 was followed up with enthusiasm, as you will read in the next Section.

3.2 GW170817

The follow up of GW170817 was surely part of the most intense and ambitious programs done in modern astronomy, involving dozens of collaborations all over the world. On August 17 2017 a GCN (Gamma–ray Coordinate Network) was sent by the Fermi-GBM about the detection of a short GRB (sGRB), GRB 170817A, at 12:41:06 UTC. Only 6 minutes after the announcement was sent out, LIGO identified a GW signal that occurred $\sim 1.7$ s before the sGRB. The combination of the data received from the three detectors restricted the sky localisation to 28 deg$^2$, and the estimated distance of the event was $\sim 40$ Mpc. This signal was consistent with that of a BNS coalescence for the first time. In particular, the observed chirp mass was $M = 1.188^{+0.004}_{-0.002} M_\odot$, with a total mass of the system between 2.73 and 3.29 $M_\odot$ and individual masses between 0.86 and 2.26 $M_\odot$. This further supports the BNS scenario against the BBH one, as BHs in BBH systems are usually found to have significantly higher masses. The scenario of a BH-NS binary cannot be ruled out, but the fact that the estimated masses are similar to realistic BNS systems supports the initial BNS hypothesis. The follow up included observations in the radio and microwaves (Hallinan et al. 2017; Alexander et al. 2017), infrared (Chornock et al. 2017; Kasliwal et al. 2017), optical/UV (Arcavi et al. 2017; Cowperthwaite et al. 2017; Cowperthwaite et al. 2017).
GW170817 Host galaxy follow up with DECam

GW170817 was followed up extensively by our DECam team, and we imaged 70 deg$^2$ in $i$ and $z$ band, corresponding to 80.7% of the final probability map. A bright optical transient was detected in our images at 11.4 hours after the GW trigger, and we found it located at 10.6$''$ from the centre of NGC 4993 at redshift $z = 0.0098$. This redshift is consistent with the distance of $40 \pm 8$ Mpc reported by LIGO, provided that $H_0 = 70 \text{km s}^{-1} \text{Mpc}^{-1}$. The apparent magnitudes of the transient at its first detection were $i \approx 17.30$ and $z \approx 17.45$, corresponding to an $i$–band absolute magnitude of $M_i = -15.7$, consistent with what expected from kilonova models. After performing the difference imaging, we found 1,500 potential transient candidates, all but one rejected as background sources after some simple selection cuts, which include rejecting SN events. Thus the candidate found in NGC 4993 is the only plausible GW counterpart, and we reject chance of coincidence at the 99.5% confidence level.

Our analysis of the GW170814 follow up images is on–going and still blinded. However, we find that our method for SN rejection through galaxy matching allows us to exclude $\sim 50\%$ of candidates with a machine learning score of $\geq 0.7$. This method has been tested on SN events simulated with SNANA (Kessler et al. 2009).

3.3 GW170817 Host galaxy follow up with DECam

While the models predicting optical and NIR emission from the coalescence of binary neutron stars are widely accepted in the astronomical community, the formation of the binary and the physics involved in merging are still a matter of debate (Lipunov et al. 1997; Faber & Rasio 2012). In this work we use this DECam data and supplement it with Hubble Space Telescope, AAT spectroscopic data and with publicly available datasets to understand the source of GW170817 in the context of its host galaxy and the local environment. In particular, we relate the BNS formation to the dynamics and stellar evolution of the host over time, asking whether the binary system was born as such, or whether dynamical interactions caused its formation. Usually it is assumed that BNSs
Figure 3.3: Possible formation channels for binary neutron stars. *Left:* pure or secular star formation scenario. The binary is formed as a system during some star formation event, and follows the usual steps of stellar evolution: the most massive of the two stars undergoes a supernova event and becomes a neutron star.

Dynamically–driven binary formation has been proposed for BBH (e.g. Rodriguez et al. 2016). By dynamically–driven, we mean any dynamical interaction that may facilitate the formation of a BNS that can merge in less than a Hubble time. In the simplest case, two single NS may form a binary system due to a close encounter. Given the typical dimensions of NS, their cross sections are not large and this is only a possibility in very dense stellar environments. Other dynamical processes may intervene: a widely separated binary system may be brought to a orbit on a shorter distance due to interactions with a third body, or an existing binary system including one NS may capture another NS. See Figure 3.3 for a schematic representation of the two different scenarios presented.

Previous studies (Carter et al. 1988) classified this galaxy as an atypical elliptical galaxy with faint concentric shells and spectral features suggesting that the galaxy has
undergone a merging event. Several analytical and numerical studies support the galaxy merger scenario for the formation of shells in galaxies (e.g. Quinn 1984; Pop et al. 2017), and show that the distribution of shells can constrain the time of the merger event. We study the evolution of this galaxy to discern between different BNS formation scenarios and estimate the rate of BNS formation in early-type galaxies, using Dark Energy Survey (DES) data to place NGC4993 in the context of the galaxy population.

### 3.3.1 Data

**Photometric data: DECam, VHS and HST**

The DECam images used in this work were taken as part of the DECam-GW follow up program between the nights of 2017 August 17 and September 1, using $ugrizY$ filters. We also use public $ugrizY$ DECam data from June 2015 to avoid contamination in the transient region. In addition, we extract $YJK$ data from the VISTA Hemisphere Survey (VHS; McMahon et al. 2013), covering the host galaxy. The images are coadded and registered to a common pixel scale (0.2636") using SWARP (Bertin et al. 2002) with 3.5 sigma clipping to remove cosmic ray artifacts. An RGB coadded image of the galaxy is presented in Figure 3.4. We build a $\chi^2$ detection image from the $r$, $i$ and $z$-band data and run SExtractor (Bertin & Arnouts 1996) in dual mode on the coadded images.

The photometry is corrected for galactic extinction. In order to compare the galaxy properties to a broader sample, we also use DES data from the first year of observations (Y1; Drlica-Wagner et al. 2017). We use \textsc{mag\_auto} magnitudes unless otherwise stated.

NGC4993 was also observed during HST Cycle 24 (PropID 14840, PI: Bellini) using ACS in F606W. The data were publicly released in April 2017 and were accessed via the Hubble Source Catalog (HSC; Whitmore et al. 2016).

**Spectroscopic data: 6dF and AAT**

The 6dF Galaxy Survey (Jones et al. 2004) final release (Jones et al. 2009) includes an optical spectrum of the centre of NGC4993 with an estimated redshift ($z = 0.009680 \pm 0.000150$).

Spectra of 14 galaxies with $v_{\text{helio}} \sim 3000$ km s$^{-1}$ and within one degree radius of NGC4993 were obtained in one target of opportunity exposure of the AAOmega spectrograph at the Anglo–Australian Telescope (AAT) on 2017 August 27. Of those, 10 spectral
Chapter 3. Host galaxies for gravitational wave follow ups and the case of GW170817

Figure 3.4: Left panel: DECam coadded image of NCG4993 in $gri$. Shell structures indicative of a recent galaxy merger are clearly visible. Middle panel: $r$-band residuals from GALFIT after subtraction of the best-fit single Sérsic light profile. Right panel: F606W-band HST ACS image with a 3 component galaxy model subtracted. Dust lanes crossing the centre of the galaxy are evident. The green lines show the position of the transient. The BNS counterpart is only present in the middle panel.
fits passed quality cuts. All the spectra used here are centred on their galaxy nucleus with a 2" aperture.

### 3.3.2 Host morphology

**CAS and Galfit**

We begin our study of NGC 4993 with an analysis of its morphological properties, employing the CAS non-parametric light quantification (Conselice 2003) and parametric Sérsic light profile fitting with GALFIT (Peng et al. 2010). Both methods utilise a mask to exclude other sources in the image and the location of the kilonova event. The CAS system is able to pick out the salient features of galaxy morphology, allowing galaxy types to be assigned and identifying objects that are likely to have undergone a recent major merger. Meanwhile, fitting the light profile additionally provides us with an alternative estimate of the total magnitude and can reveal more subtle aspects of galaxy morphology within the residuals of the model-subtracted image.

The CAS system estimates three morphological parameters, concentration $C$, asymmetry $A$, and clumpiness $S$ to classify objects. The concentration is defined as the logarithm of the ratio of the 80% to 20% curve of growth radii $r_{80}, r_{20}$:

$$C = 5 \times \log_{10}(r_{80}/r_{20})$$

(3.2)

where the curve of growth is the integrated flux inside an aperture of radius $r$ as a function of $r$. In general, elliptical galaxies tend to be more concentrated than disk galaxies and dwarf galaxies. In order to compute the asymmetry $A$ we rotate the galaxy image $I$ by 180° ($R$) and subtract it from its original image. The absolute value of these residuals is divided by the original image flux $I$, so that: $A = |I - R|/I$. The asymmetry is particularly related to the merger history. The clumpiness $S$ is given by subtracting the original image of the galaxy by a smoothed image, so that the residual map only contains the high-frequency components of the light distribution:

$$S = 10 \times \sum_{x,y=1.1}^{N-N} \frac{(I_{x,y} - I_{x,y}^\sigma) - B_{x,y}}{I_{x,y}}$$

(3.3)

where $I_{x,y}$ is the sky-subtracted galaxy flux in the pixel at $(x, y)$, $I_{x,y}^\sigma$ is the map smoothed with a filter of width $\sigma$ and $B_{x,y}$ is the background flux value in an area which is equivalent
to that of the galaxy. Elliptical galaxies are usually very smooth and therefore present a low clumpiness value, while star forming galaxies can be very patchy and present a high $S$ value. The CAS quantities are all defined within 1.5 times the Petrosian inverted radius at $r(\eta = 0.2)$, where $\eta$ is a dimensionless quantity defined in terms of the surface brightness at radius $r$: $\eta \equiv I(r)/\langle I(r) \rangle^2$. This radius was chosen because more than 99% of the light is included within $r(\eta = 0.2)$. For a detailed definition and analysis of these parameters see Bershady et al. (2000).

**GalFit** is run on the DES and VHS images to fit the galaxy with a Single Sersic profile, performing the deconvolution with a PSF model extracted with PSFEx (Bertin 2011) and using input guesses from SExtractor. As reported in (Peng et al. 2010), the adopted Sérsc function has the following form:

$$
\Sigma(r) = \Sigma_e \exp \left[-k \left(\frac{r}{r_e}\right)^{\frac{1}{n}} - 1\right],
$$

where $\Sigma_e$ is the pixel magnitude at the effective radius $r_e$. The Sérsc index $n$ quantifies the profile concentration: if $n$ is large, we have steep inner profile with a highly extended outer wing; inversely, when $n$ is small, the inner profile is shallow and presents a steep truncation at large radii. In the case of $n = 1$ we have an exponential light profile, while for $n = 4$ the it reduces to a de Vaucouleurs profile. **Galfit** provides measurements for the free parameters of the Sérsc function: central position, integrated magnitude $m_{tot}$, effective radius $r_e$ measured along the major axis, Sérsc index $n$, axis ratio $q$ and position angle $\theta$. The integrated magnitude is determined through its definition as a function of the flux integrated out of $r = \infty$ for the Sérsc profile. The fit is done in two ways: band-by-band and simultaneously across all bands using a modified version, **GalFit-m** (Vika et al. 2013). In the second case the Sérsc fitting parameters are allowed to vary with wavelength as a second-order polynomial. All parameters are left free without constraints, except for the central position in the single-band fits. This is allowed to vary by only $\pm 1$ pixel as it is well-constrained by SExtractor already.

In order to assess the stability of **GalFit** and obtain an estimate of the uncertainties on the measurements, each single-band run is performed 10,560 times, varying the inputs around their nominal values. We take the median as our final measurement and the standard deviation as the uncertainty.

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2 This is the inverse of the definition that was introduced by Petrosian (1976)
Figure 3.5: Concentration versus asymmetry for NGC4993 (in blue), compared to a sGRB hosts sample (Conselice et al., in prep.) in red, and field galaxies (black dots) with stellar mass within $\pm 0.2$ dex of NGC4993 value and redshift $z < 0.2$. The lines separate different Hubble types as shown in Conselice (2003).

Table 3.1: Outputs from GALFIT parametric Sérsic fits performed on the $ugrizY$ DECam coadd images and $YJKs$ VHS data. The fit was joint across bands, allowing the effective radius, $r_e$ (in pixels), Sérsic index, $n$, ellipticity, $\epsilon = 1 - b/a$, and position angle, $\theta$, to vary with wavelength. One pixel corresponds to $0.2636''$. The final row lists indicative errors based on the single band analysis.
Results

Following the definitions given in Conselice (2003), we find: concentration $C = 3.348 \pm 0.035$, asymmetry $A = 0.04 \pm 0.01$, and clumpiness $S = 0.05 \pm 0.05$. These values are typical for an early-type galaxy. In Figure 3.5 we compare these values to field galaxies of similar masses (within 0.2 dex of NGC4993) and redshifts ($z < 0.2$) from the GAMA survey, and to a sample of sGRB hosts (Conselice et al. in prep.) taken in F814W imaging from HST. NGC4993 stands out as peculiar with respect to other GRB hosts: such objects tend to lie on the more highly asymmetric side of late-type galaxies.

The results from the single S´ersic fit across all bands are summarised in Table 3.1 (the band-by-band fits give broadly consistent results). We find an increase in S´ersic index towards redder bands and a rotation in the position angle. This rotation of bluer versus redder bands suggests there could be two superimposed stellar populations with differing orientations. This may have arisen during the course of the galaxy’s secular evolution but could also be caused by a minor galaxy merger, as indicated by the presence of shells.

The middle panel of Figure 3.4 shows DECam r-band residuals from GalFit and the position of the transient. At least four shell structures are clearly visible. Closer inspection with HST data (right panel in Figure 3.4) reveals a possible further broad inner shell, on which the transient seems to lie, and obvious dust lanes (visible also as a negative residual in the DECam version). The r-band absolute magnitude from a 4 sq.arcsec region around the transient location in the galaxy-subtracted template image is $-10.65$. This luminosity implies a rather high stellar density in the locale of the BNS coalescence. In summary, we find compelling evidence for a recent minor galaxy merger in NCG4993, and the location of the kilonova event with respect to the shells leads us naturally to ask whether there is a causal connection between the two.

From Figure 3.5 we see that clear major galaxy mergers are unusual amongst sGRB hosts. Furthermore, the other sGRBs are at cosmological distances and thus are mostly undergoing extensive star formation or merging. If the hosts have to be related by some common features, this is an indication that NGC4993 has undergone some merging activity, but a minor merger such that the bulk morphology is still elliptical. We thus explore the possibility that the kilonova was a result of a recent galaxy merger in NGC4993.
Figure 3.6: Spectroscopic fit of the 6dF optical spectrum. The black line is the observed spectrum, the red line is the pPXF fit for the stellar component, and the orange line is the best–fit including ionized gas emission lines. The zoomed panels show $H_\beta$, OIII, NII and $H_\alpha$ lines. The green points at the bottom are the fit residuals, while the purple line is the gas-only best–fit model spectrum.

Figure 3.7: BPT diagram for NGC4993 (red star) and the other galaxies (black points) in the galaxy group with AAT spectra available. The dashed lines represent the Kewley et al. (2006) classification method for AGN, star–forming (HII) and composite (Comp) galaxies. Many of the group galaxies have very weak AGN or LINER-like emission. Error bars represent 1σ error from the propagation of fit errors on line strengths.
3.3.3 Photometric and spectroscopic SED

SED fitting methods

We use pPXF (Cappellari & Emsellem 2004; Cappellari 2017), for the spectral fitting. It enables extraction of the stellar kinematics and stellar population from absorption line spectra of galaxies, using a maximum penalized likelihood approach. We use the Miles stellar libraries, and fit over the wavelengths 4000 – 7409 Å, excluding the range 5500 – 5600 Å of the 6dF spectrum, where a strong sky line contaminates the flux.

We use LePhare (Arnouts et al. 1999, Ilbert et al. 2006) for the broadband Spectral Energy Distribution (SED) fitting. We add a 0.05 systematic uncertainty in quadrature to the magnitudes, as the SExtractor errors not take into account systematic uncertainties on magnitude estimation. The simple stellar population (SSP) templates used are Bruzual & Charlot (2003), with two metallicities (Z⊙ and 2.5Z⊙), a Chabrier (2003) Initial Mass Function (IMF) and a Milky Way (Allen et al. 2011) extinction law. The SFH chosen is lognormal:

\[ \Psi(t, t_0, \tau) = \frac{1}{t \sqrt{2\pi \tau^2}} e^{-\frac{(\ln t - \ln t_0)^2}{2\tau^2}}, \]

as it is the most representative family of models with only two parameters (Gladders et al. 2013). Here t₀ and τ are the half–mass–time and width.

Motivated by our morphological analysis, we allow for an additional burst of recent SF. This is modelled as a Gaussian centred at t_{burst} with width of 10 Myr and peaking at a fraction 0.4 – 0.1 of the peak of the log-normal SFH (as no evidence for strong late SF is found).

The same templates are used to perform spatially–resolved photometric SED fitting across DES+VHS coadded images within 10 × 10 pixels, including the galaxy dust extinction. The other sources in the field are masked out using the segmentation map output by SExtractor.

SED fitting results

Figure 3.6 shows the best fit model of the 6dF spectrum, which results in a reduced χ² of 1.22. An analysis of the mass fraction as a function of stellar age shows that part of the core galaxy stellar population has a supersolar metallicity, but the weighted mean value \( \langle [M/H] \rangle = -0.012 \pm 0.010 \) is marginally consistent with solar metallicity. The mean age
Figure 3.8: sSFR (left) and stellar mass (right) maps resulting from the pixel SED fitting of DES+VHS bands. Other objects have been masked out. $x$ and $y$ axes correspond to the map pixels. One pixel corresponds to a physical size of 0.526 kpc at the galaxy redshift.

Figure 3.9: Pixel color-magnitude diagram for the pixels covering NGC4993 from DECam $g$ and $r$ single epoch exposures taken previously to the BNS event. The core of the galaxy is shown in red, while the cyan points represent the 1.5" around the location of the BNS event (10.6" from the center).
is $11.298 \pm 0.054$ Gyr, and the mass-to-light ratio is $5.23 \pm 0.15$ in $r$-band.

The stellar model fit reveals the existence of weak ionized gas emission lines. However, the line ratios from the fit suggest they are produced by a harder ionizing source than star-formation, formally lying in the AGN region of the Baldwin, Phillips & Teerivich (BPT; Baldwin et al. 1981) diagram. Blanchard et al. (2017) argue that there is a weak AGN present in the core of the galaxy on the basis of radio and X-ray emission, and so we conclude there to be no evidence of recent star-formation from the 6dF spectrum, irrespective of the highly uncertain $\OIII/H_\beta$ ratio. A comparison of galaxies in the group using AAT spectra and classification by Kewley et al. (2006) is shown in Figure 3.7.

Given the evidence of dust presence in the HST study, we estimate the dust content using the Balmer decrement (Berman 1936) observed from the spectrum. The reddening is $E(B - V) = 0.12 \pm 0.50$ in the case of $I(H_\alpha)/I(H_\beta) = 3.1$, which is expected in the case of AGN activity. We therefore restrict our dust models to have reddening values $0.1, 0.2, 0.3, 0.4, 0.5$ in the photometric fits.

The photometric best-fitting template has a solar metallicity, a quickly declining log-normal SFH with $t_0 = 3$ Gyr and $\tau = 0.1$. A low reddening $E(B - V) = 0.1$ is preferred, and the stellar mass is $(2.95 \pm 0.65) \times 10^{10} M_\odot$. The inclusion of a late SFH burst is disfavored by the fitting apart from intermediate apertures.

Previous work found that the presence of dust lanes may bias the galaxy stellar mass from unresolved galaxy SED fits to lower values (Sorba & Sawicki 2015). The total stellar mass from fitting over the SExtractor segmentation map of NGC493 is $(3.8 \pm 0.20) \times 10^{10} M_\odot$, more than 1σ higher than the unresolved SED fitting. The specific SFR (sSFR) and stellar mass maps from our pixel SED fits are shown in Figure 3.8, where the shell structure is clearly visible, suggesting that the sSFR is slightly more accentuated in the stellar halo compared to the inner parts. Younger ages (by $\sim 2$ Gyr) are also preferred in the outer regions, though we still do not find evidence for a star formation burst at late times, and explain our results by the stripping of stellar populations from the lower-mass galaxy in a minor dry merger. A dust model with $E(B - V) = 0.1$ is preferred in the inner few kpc, while $E(B - V) = 0$ is found outside. Despite the presence of dust lanes, an analysis of the HST photometry and a comparison with extinction models suggests that the effect of dust is not extreme, with reddening values that are consistent with 0.1 in the core. We therefore believe that the dust obscuration does not play a significant role in our SFR estimates.
Pixel Color Diagrams

In Figure 3.9 we show a color-magnitude diagram for all the pixels within the field of view of the DECam data near the galaxy. The image has been cleaned of stars and other contamination, thus all points come from the galaxy itself. The position of the GW source, 10.6″ offset from the center, is the cyan colored pixels, while the center of the galaxy is shown in the red points. This galaxy is well represented by a pixel “main sequence” that is bluer at fainter levels, which is typical of early–type galaxy color gradients (e.g., Lanyon-Foster et al. 2007). We conclude that there is no significant difference between the transient position and other outer light, although it is bluer than the core region. This further supports the scenario in which the BNS formation is not related to some particular recent star formation event in this region.

3.3.4 Implications for the binary neutron star formation and coalescence

BNS formation and delay time under the hypothesis of galaxy merger

In the most accepted shell formation scenarios the shells are stellar debris coming from the less massive, stripped galaxy, and the arcs form at the apocenter of the orbits of the infalling material (Quinn 1984). The kinematics of the shells allow to connect their position, the gravitational potential of the galaxy and the time elapsed since the galaxy merger (Dupraz & Combes 1986; Ebrová et al. 2012).

Based on our results, we believe that NGC4993 experienced a dry minor galaxy merger with still visible signs. The shells are expected to be washed out within a time that depends on the velocity dispersion at their position. We estimate the shell survival time in two ways, based on the velocity dispersion of the galaxy as well as the velocity dispersion of the shell itself. From the 6dF spectrum the line-of-sight central velocity dispersion is $\sigma_v = (160.0 \pm 9.1)$ km s$^{-1}$. We estimate its value at the position of the transient. The velocity dispersion of early type galaxies drops from its central peak value at larger radii, and observations show that the maximum drop to the outer parts of ellipticals near the effective radius is $\sim 40\%$ of the central value (Emsellem et al. 2004). Based on the distance of the shell from the centre, $R \approx 4$ kpc, we estimate that the dynamical time at this radius is $t_{\text{dyn}} \equiv R/\sigma_v \approx 60$ Myr (the line-of-sight velocity is relevant here, given the shell’s geometry, but e.g. if we assume a 3D isotropic velocity dispersion it would reduce the dynamical time by $\sqrt{3}$).
So far we have no measurement of the shell’s velocity dispersion, but estimates from the literature suggest for similar shells in other galaxies $\sigma_v \approx 20 \text{ km s}^{-1}$ (Quinn 1984). This would give a dynamical time scale of $t_{\text{dyn}} \approx 192 \text{ Myr}$. Detailed simulations of shells in other galaxies suggest that survival time could be even larger than 1 Gyr, depending on the assumed scenario (Pop et al. 2017).

The survival time of the shell could be used as an upper limit for the time the minor merger took place, i.e $t_{\text{dyn}} \geq t_{\text{merg}}$, so we estimate $t_{\text{merg}} \lesssim 200 \text{ Myr}$.

If the BNS was formed as such in a shell, then we would have expected to see evidence for recent star formation, but we find no indication of this. In the absence of star formation it is plausible that the BNS coalescence was triggered by a dynamical process, e.g. NS-NS capture or the destabilisation of a pre-existing wide-separation binary. These processes will be quite sensitive to the stellar density which, given the Sérsic index and the luminosity from the residual image found in section 3.3.2, is high in the centre of NGC4993 and around the transient position. If this dynamical hypothesis is true, then the delay time $\Delta t_{\text{NSM}}$ between the BNS formation and coalescence is $\lesssim 200 \text{ Myr}$. Figure 3.10 shows a schematic timeline of the events described for NGC 4993.
3.3. GW170817 Host galaxy follow up with DECam

Galaxy environment

If the binary formation is related to dynamical processes in galaxy merging as we are investigating here, then this is most likely to happen in galaxy groups and low mass clusters. According to the 2MASS catalog (Tully 2015), NGC4993 resides in a group, of which we analyse the remaining 7 galaxies. A spectral analysis shows that NGC4993 is not the only galaxy showing AGN activity (see Figure 3.7), but it is peculiar in terms of age, metallicity and mass-to-light ratio. It shows an older stellar population (the mean age of the other 13 galaxies is $\log(Age) = 9.56 \pm 0.17$), lower metallicity (mean: $M/H = -0.31 \pm 0.11$), and higher $M/L_r$ (mean: $2.41 \pm 0.45$) than the average. The group has a projected virial radius of $R_{vir} = 0.36$ Mpc and a line-of-sight velocity dispersion $\sigma_v = 143$ km s$^{-1}$ (Tully 2015). The crossing time is therefore $t_{cr} \sim R_v/(\sqrt{2.5}\sigma_v) \sim 1.6$ Gyr.

If galaxy mergers are correlated to BNS coalescence, future GW studies could possibly concentrate on galaxy groups (but note that these are crowded regions and therefore matching candidates to a host could be difficult). In order to have precise measurements of $H_0$, one needs to identify the host galaxy redshift clearly. When the match is clear, the properties of the type of host galaxy found could help future studies to select the right host galaxy or create galaxy catalogs of likely hosts for GW EM follow-up. Similar galaxy catalogs could also be useful for “untriggered” kilonova searches (Doctor et al. 2017): kilonovae can in principle be detected by photometric and/or spectroscopic surveys also when a GW signal is not detected (for example, while LIGO is turned off, or for events which are too far to be detected by the interferometers). Large photometric surveys such as DES, LSST or WFIRST are expected to observe kilonova events at redshifts beyond the sensitivity of GW experiments, where the angular separation between galaxies decreases (Scolnic et al. 2017), and optimised galaxy catalogs will be necessary to identify the correct host.

BNS merging constraints

We derive a constraint on neutron stars merging rate at time $t$ by using:

$$R_{NSM}(t) = \alpha R_{NS}(t'),$$

(3.6)
where $\alpha$ is the fraction of neutron stars which are in binaries, $t' = t - \Delta t_{NSM}$ (with $\Delta t_{NSM}$ being the delay time of the neutron star merger) and the fraction of mass of formed stars that are NS is:

$$R_{NS}(t') = \int dM_\star \Phi(M_\star) \Psi(t_\star) \Theta_{NS}(M_\star),$$  \hspace{1cm} (3.7)

with $\Phi(M_\star)$ being the IMF, $\Psi(t_\star)$ is our best fit SFH, $\Theta_{NS}(M_\star)$ is 1 for star mass ranges of $8 M_\odot < M < 20 M_\odot$, zero otherwise. We drop the metallicity dependence in $\Theta_{NS}$ because we only consider a solar metallicity for the galaxy, as a result of our spectroscopic fit. $t_\star$ is the time when the progenitor of the NS was formed, therefore satisfying $t' = t_\star + t_{life}$, with $t_{life}$ being the lifetime of the progenitor before becoming a NS. We assume a $t_{life} = 0.02$ Gyr, but our calculation is insensitive to this choice as the typical lifetime of these massive stars ($\sim 0.01 - 0.03$ Gyr) is much shorter than the timescale over which the SFH found for NGC4993 is changing at late times. We assume a Chabrier IMF, but this choice is not relevant as we are only exploring the high mass end of the IMF. Assuming $\alpha = 0.002$ and the distribution of $\Delta t_{NSM}$ from Vangioni et al. (2016) (their Figure 3 for solar metallicity), and our best fit SFH from Eq. 3.5 with $t_0 = 3$Gyr and $\tau = 0.3$, we get a NS formation rate of $R_{NS}^{gal} = 3.6^{+28}_{-3.6} \times 10^{-5}$ yr$^{-1}$ and a BNS merger rate of $R_{NSM}^{gal} = 5.7^{+0.57}_{-3.3} \times 10^{-6}$ yr$^{-1}$ for the whole galaxy. Errors reflect the uncertainty on the SFH, which dominates our errors: they represent the two central quartiles of the rates distribution computed with the SFHs of the pixel SED fitting over the galaxy.

Given the sensitivity of the BNS merger event rate to the recent SFR of a galaxy, it is somewhat surprising that GW170817 occurred in an old, early type galaxy. We therefore ask what is the probability of observing such an event in any early–type galaxy within the LIGO–detectable volume. To make this estimate we integrate the stellar mass function of early–type galaxies from Weigel et al. (2016) and scale the per–solar–mass rate from Eq. 3.6 to the mass contained within the LIGO detectable volume (radius 80 Mpc). We find $R_{NSM}^{early} = 23^{+14}_{-14}$ yr$^{-1}$ Gpc$^{-3}$ resulting in $0.038^{+0.004}_{-0.022}$ expected events. This calculation assumes that the SFH of NGC4993 is representative of local early–type galaxies. In fact much of the mass will be contained in more massive, and on average older and less star–forming, galaxies. We contrast this with a similar calculation for all galaxy types, using the cosmic SFR density from Gladders et al. (2013), finding $R_{NSM}^{all} \approx 270$ yr$^{-1}$ Gpc$^{-3}$ and $\sim 0.5$ expected events.
This result shows that it is unlikely that we observed one such BNS merger with LIGO over the combined nine months of operations in an early-type galaxy. The assumptions in the calculation include the fraction of NS that form in binaries ($\alpha = 0.002$) and the delay time distribution, both coming from binary star models (where the progenitors of the BNS were already a bound system) and satisfying Milky Way constraints. If the BNS formation mechanism is via dynamical interaction, our result could point to a higher value of $\alpha$ or a shorter $\Delta t_{NSM}$ for systems that recently underwent a galaxy merger, more so for those that have high stellar density (such as early-type galaxies). It is therefore of interest to know the fraction of galaxies similar to NGC4993 that show similar signs of a galaxy merger in the form of visible shells. We select galaxies from the first year of DES data with size, surface brightness and Sérsic index within 10% of the best fit values for NGC4993. We find 1100 such galaxies, and visually inspect them to identify shell galaxies. A subsample of those is shown in Figure 3.11. Only 15% of these objects display shells, and so NGC4993 is unusual amongst early-type galaxies.

On the other hand, Blanchard et al. (2017) find a median delay time of $11^{+0.7}_{-1.4}$ Gyr under the assumption that the binary was formed through secular SF, and that no interactions disturbed the binary since it was formed. This is derived from the measured SFH, which is
similar to what we find, and from which they find that 50% of the stellar mass of NGC4993 was formed $11^{+0.7}_{-1.4}$ Gyr ago. This scenario is possible and cannot be excluded, although our study shows that it is unlikely.

Our results are far from conclusive evidence for a merger origin of BNS events. However, the coincidence of evidence for a recent merger in a galaxy for which a BNS event was otherwise improbable is compelling.

### 3.4 Conclusions

In this Chapter we have shown how galaxy properties are important not only for GW electromagnetic follow up strategies, but also to study the formation and evolution of the GW sources. In particular, we can use the SED fitting results that we get from the methods described in the previous Chapter to:

- Match to galaxies the transients found from GW follow up searches. The goal of this search is twofold. First, by identifying a GW source host with a photo-$z$ or spectroscopic redshift, we can relate it to the distance provided by LIGO and use the GW event as a standard siren and measure cosmological parameters. Secondly, we can identify and reject Supernovae that contaminate our candidate list and restrict our analysis to a smaller sample.

- Study binary systems formation and evolution. In the case of GW170817, the star formation and the properties of the host galaxy showed that the fact that this event happened in NGC4993 was unlikely based on current BNS models. These models, based on pure star formation, should be revisited in the future. Other works followed our line of thought and reached similar conclusions (Belczynski et al. 2018; Ebrová & Bílek 2018).

- Constrain the delay time of the GW sources, either through estimating a time for dynamical interactions in the case of dynamically-driven formation of the system (as in Palmese et al. 2017), or through a study of the star formation history (as in Blanchard et al. 2017).

Furthermore, galaxy catalogs such as the one described in Section 3.1.3 of this Chapter, and used in the DES–GW post-processing pipeline, can also be useful to point small FoV telescopes after a GW trigger towards galaxies. Providing the properties of those galaxies,
can also help with selecting likely candidates. For example, one could assume that these
events are most likely to happen where most of the stellar mass is, or in the most luminous
or star–forming galaxies. However, only further GW and EM detections will provide some
statistics and will allow us to identify the galaxy properties of the most likely hosts.
Chapter 4

Stellar mass versus dark matter in galaxy clusters: RXJ2248

“I have forced myself to contradict myself in order to avoid conforming to my own taste.”

Marcel Duchamp

The work described in this chapter is part of Palmese et al., 2016, MNRAS, 463, 1486.

In this part of the thesis (Chapters 4, 5 and 6) we utilise galaxy properties, in particular the stellar mass, to study galaxy clusters, their mass content and their evolution.

4.1 Introduction

In the last decade, large photometric galaxy surveys, such as SDSS, have provided us with a massive amount of data that have proven to be extremely useful for studies of cosmology. On the other hand, smaller area but deeper surveys like the Hubble Space Telescope (HST) based Cluster Lensing And Supernova Survey (CLASH) (Postman et al. 2012), allowed us to characterise single objects with unprecedented precision. The importance of finding synergies between these surveys relates to several aspects of observation (e.g. target selection, photometric calibration) and data analysis (photometric redshifts,
Table 4.1: Main properties of the cluster RXC J2248-4431. The quoted luminosity is in the rest frame 0.1-2.4 keV band.

<table>
<thead>
<tr>
<th>$\alpha_J^{2000}$</th>
<th>$\delta_J^{2000}$</th>
<th>Redshift</th>
<th>Luminosity (erg s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>22:48:44.29</td>
<td>-44:31:48.4</td>
<td>0.348</td>
<td>$3.08 \times 10^{45}$</td>
</tr>
</tbody>
</table>

physical properties of galaxies). This is particularly relevant for overlapping ground–based and space–based surveys: the higher quality that can be obtained from space can enable calibration and tests for the data collected by ground–based telescopes.

In this Chapter, we study the cluster of galaxies RXC J2248.7–4431 (RXJ2248 hereinafter). We make use of the synergies between DES and CLASH, and test in this way the performance of the early DES data at a catalog level (i.e. without making use of the images for the results). Photometric redshift (photo-z) and stellar mass results from CLASH are also used as a validation set for DES stellar mass estimates.

The aim of this work is twofold: the first goal is to compare between DES’s wide area breadth and CLASH’s small area precision for the cluster RXJ2248. In fact, checks using HST data had not been done before to test the DES data, although the similar optical filters and the additional UV and IR HST bands make CLASH an optimal candidate for validation and quantifying uncertainties of photometry, photo-z’s and stellar masses. The second is to illustrate how an analysis of the stellar mass distribution of this massive cluster over the wider Dark Energy Camera (DECam) field of view can be done.

In Section 4.2, we start by describing the two surveys considered. The cluster is described in Section 4.3. The comparison of DES and CLASH, in terms of photometric redshifts and star/galaxy separation, is presented in Section 4.4. Section 4.5 contains the second part of this work, where we present the stellar mass results obtained from CLASH and DES, and compare the DES stellar masses to the total mass from the DES weak lensing analysis by Melchior et al. (2016). In the following, we assume a concordance $\Lambda$CDM cosmological model with $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$ and $h = 0.7$. In this cosmology, 1$'$ corresponds to a physical transverse length of 295 kpc at the cluster redshift $z = 0.3475$.

4.2 Data

The data used for the analyses developed for this work come from DES and CLASH.

The fact that DECam has a $\sim 3$ deg$^2$ field of view gives us the opportunity of studying the large scale structure of galaxy clusters with only one pointing.
4.2. Data

Figure 4.1: A portion of $1' \times 1'$ image centered in RA 22:48:48.003 and DEC -44:31:38.52 in the CLASH F625W band (top) and the DES $r$ band (bottom).

<table>
<thead>
<tr>
<th>Survey/Instrument</th>
<th>Authors</th>
<th>FoV</th>
<th>Filters</th>
<th>Mag limits</th>
<th>Spectra</th>
<th>Objects</th>
</tr>
</thead>
<tbody>
<tr>
<td>NTT+ G12</td>
<td>5' × 5'</td>
<td>$V, R$</td>
<td>–</td>
<td>116</td>
<td>711</td>
<td></td>
</tr>
<tr>
<td>GMOS G13 33' × 33'</td>
<td>16 in 2000–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>CLASH P12 2' × 2' (WFC3)</td>
<td>17000 Å</td>
<td>~ 25-27 (10σ)</td>
<td>–</td>
<td>3471</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M14 33' × 33'</td>
<td>$UBVRIZ$</td>
<td>26.4, 26.7, 24.4 ($V, R, I$ 5σ)</td>
<td>–</td>
<td>–</td>
<td></td>
<td></td>
</tr>
<tr>
<td>WFI G13 3' × 3'</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td></td>
<td></td>
</tr>
<tr>
<td>DES M16 2.2 deg$^2$</td>
<td>$grizY$</td>
<td>24.45, 24.30, 23.50, 22.90, 21.70 (10σ)</td>
<td>–</td>
<td>374 294</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 4.2: Some experimental specifications of the surveys that have observed RXJ2248, with the corresponding paper in which those data have been used. The work presented in those papers is shortly summarised in Section 4.3. G12, P12, M14, G13 and M16 stand for Gómez et al. (2012), Postman et al. (2012), Monna et al. (2014), Gruen et al. (2013), Melchior et al. (2016) respectively. The magnitude limits reported for DES are the mean 10σ galaxy magnitudes.
The cluster RXJ2248 was observed during the SV season, with typical exposure times of 90 seconds for the griz bands and 45 seconds for the Y band. It was re-observed later in 2013 to benefit from improvements to telescope performance and general image quality. The objects used in this Chapter are part of the SVA1 gold catalogue.

We use AB magnitudes throughout this thesis, and \texttt{MAG\_AUTO} measurements given by \texttt{SExtractor}, as these proved to be robust and were thus used in several DES SV papers (e.g. Bonnett et al. 2016; Crocce et al. 2015). The objects selected for the analysis have a signal to noise $S/N > 10$ in the $i$ band.

The other survey considered here is CLASH (Postman et al. 2012), a 524-orbit HST multi-cycle treasury program that has observed 25 massive clusters, having a range of virial masses between $5 \times 10^{14} M_\odot$ to $30 \times 10^{14} M_\odot$ and an average redshift of $\bar{z} = 0.4$. The wavelength range covers the UV, the visible and the IR (2000 – 17000 Å) through 17 bands using the Advanced Camera for Surveys (ACS) and the Wide Field Camera 3 (WFC 3).

The CLASH mosaics were produced using the “MosaicDrizzle” pipeline (see Koekemoer et al. 2002, Koekemoer et al. 2011). The CLASH catalogue creation pipeline makes use of \texttt{SExtractor}: the software is run in dual image mode, where a detection image is created from a weighted sum of the ACS/WFC and WFC3/IR images. The WFC3/UVIS images are not used in the construction of the detection image but the UVIS data are still used to compute source photometry. The photometry given in the public catalogue (http://www.stsci.edu/~postman/CLASH), which is also the one used in this work, was measured in isophotal apertures, as they have been shown to produce reliable colours (Benitez et al. 2004). ACS/WFC3 reach a depth of 26.8, 26.4, 26.2, 26.0 and 26.6 (10σ galaxy AB magnitudes for circular apertures of 0.4 arcsec in diameter, Postman et al. 2012) in the F475W, F625W, F775W, F850LP and F105W filters, respectively.

Below, we compare the information obtained with 5 DES filters and with 17 HST filters.

### 4.3 The Cluster RXC J2248.7–4431

In this section we present what is known about this cluster from previous works. The cluster of galaxies RXC J2248.7–4431, where RXC stands for ROSAT X-ray Cluster, is also known as Abell S1063 or MACS 2248–4431. It is a very luminous cluster, having an
4.3. The Cluster RXC J2248.7–4431

Figure 4.2: Throughput of the DES filters (solid lines) and HST similar filters (dashed lines).

X-ray bolometric luminosity of \((6.95 \pm 0.1) \times 10^{45} \text{ erg s}^{-1}\) in the energy range \(0.1 - 100\) keV (Maughan et al. 2008). Its properties are listed in Table 4.1. It was first catalogued by Abell et al. (1989), who counted 74 galaxies. Thanks to the ROSAT-ESO Flux Limited X-ray (REFLEX) Galaxy Cluster survey, Böhringer et al. (2004) measured a spectroscopic redshift \(z = 0.3475\), which has been adopted in the recent literature and has also been confirmed in Gómez et al. (2012), who quoted a mean redshift of \(z = 0.3461^{+0.0010}_{-0.0011}\) for 81 members.

Gómez et al. (2012) were the first to study in detail RXJ2248, even though it is the second most luminous cluster in the REFLEX survey (having a reported luminosity of \(\sim 3.08 \times 10^{45} \text{ erg s}^{-1}\) in the rest frame \(0.1 - 2.4\) keV band).

In Gómez et al. (2012), the cluster is presented as one of the hottest X-ray clusters known at that time. The high X-ray temperature, together with the high velocity dispersion, suggest a very massive cluster \((M_{200c} > 2.5 \times 10^{15} M_\odot)\) and/or a merger system. The merger model is supported by a small offset between the galaxy distribution and the peak of X-ray isophotes, and a non-Gaussian galaxy velocity distribution. Gómez et al. (2012) also reported that the velocity distribution is better represented by the velocity dispersion produced during a merger than by the velocity distribution of a relaxed cluster.

Gruen et al. (2013) used Wide-Field Imager (WFI) data to perform a weak lensing analysis of the cluster. They parametrised the cluster density with a NFW profile (Navarro et al. 1996) and obtained a mass \(M_{200m} = 3.31^{+0.96}_{-0.68} \times 10^{15} M_\odot\) (or \(M_{200c} = 2.28^{+0.66}_{-0.47} \times 10^{15} M_\odot\)). They also identified a second galaxy cluster in the field of view at redshift \(\sim 0.6\), with an estimated mass of \(M_{200m} = 4.0^{+3.7}_{-2.6} \times 10^{14} M_\odot\).
Melchior et al. (2016) studied the weak lensing masses and galaxy distributions of four massive clusters observed during the DES SV period, including RXJ2248. They found $M_{200c} = 1.75^{+0.43}_{-0.37} \times 10^{15} M_\odot$, which is in agreement with previous mass estimates. For RXJ2248, they also identified filamentary structures of the luminous red-sequence galaxies found with the RedMAPPer (Rykoff et al. 2014) algorithm.

Umetsu et al. (2016) combined HST and wide field imaging (from the Subaru telescope or the ESO/WFI) observations to reconstruct the surface mass density profiles of 20 CLASH clusters. Their analysis jointly uses strong lensing as well as weak lensing with shear and magnification, and for RXJ2248 they found $M_{200c} = 1.878 \pm 0.672 \times 10^{15} M_\odot$.

### 4.4 Comparison of DES and CLASH

In this section, we assess detectability, photometry, and stellar masses of DES galaxies, treating matched CLASH galaxies as truth table.\(^1\) In order to make the comparison, we seek to identify similar filters in both data sets. Figure 4.2 shows that the closest HST analogs to DES $griz$ are F475W, F625W, F775W and F850lp. We will refer to the corresponding HST and DES bands as $g$, $r$, $i$ and $z$ for simplicity of notation. In the following, we will also use the DES $Y$ band, that does not have a similar HST filter. When we refer to 5 CLASH filters, it means we are including the F105W filter, that is broader than the DES $Y$.

In the DES catalogue of the RXJ2248 area, there are 374,294 sources in a roughly circular area of approximately 3 deg\(^2\). The deeper, higher resolution CLASH catalogue includes 3,471 sources in a much smaller area ($\sim 5' \times 4'$).

We perform a spatial matching (using a matching radius of 1.5\(''\)) between the DES and CLASH catalogues and we find 609 matched sources. Thus the DES recovered only 18% of the sources in the CLASH catalogue. The high percentage of sources missed in DES is due to various problems, one of them being that the $griz$ 10\(\sigma\) depths differ by $\gtrsim 2$ magnitudes between the two datasets. This accounts for most of the undetected sources.

---

\(^1\)A comparison of weak lensing measurements between DES and CLASH was not performed because they predominantly reveal differences in the shear calibration. The majority of galaxies with shape measurement in both catalogs are very faint for DES, resulting in large and noisy calibration factors (see Section 4.2.1 in Melchior et al. 2016). In addition, the high density of galaxies in the central region of this cluster creates many more close galaxy pairs or even blends in ground-based DES images than when viewed with HST, rendering shape measurement even more challenging. A detailed analysis of those relevant effects is beyond the scope of this work.
4.4. Comparison of DES and CLASH

in DES: when we simulate fake faint galaxies with BALROG\(^2\) (Suchyta et al. 2016) on the DES image of RXJ2248, we find that the completeness in \textit{riz} bands (which are those used to run the detection) drops below 20\% between magnitude 24 and 25, justifying the incompleteness found when comparing to the even deeper CLASH survey. We also expected one of the problems to be blending, especially close to the bright cluster core. We run some completeness tests using a DES enhanced deblending catalogue (Zhang et al. 2014) that would increase the percentage of recovered sources to 20\%, but found that blending is not a major reason of incompleteness. Also, CLASH object detection is run on ACS+IR images, while DES detection only involves optical bands and it may miss redder sources. A visual comparison of DES and CLASH images is shown in Figure 4.1.

A comparison of measured isophotal magnitudes at the catalogue level between the matched galaxies in the two datasets here considered shows a mean shift \(|\Delta m| \leq 0.13\) in all bands, where the offsets due to the different filters compared have been taken into account. This is true when a signal to noise cut \(S/N > 10\) is performed on the matched galaxies, and objects with saturated pixels and corrupted DES data are removed.

4.4.1 Magnitude comparison

Considering only those matched sources with a signal to noise ratio \(S/N > 10\) in the DES \(i\)-band, excluding stars and objects with SExtractor FLAGS > 3 (in order to exclude objects with saturated pixels or corrupted data, but include objects that were initially blended) we are left with 327 sources observed in the \(g\) and \(r\) bands, and 331 in the \(i\) and \(z\) bands. The differences \(\Delta m = m_{\text{DES}} - m_{\text{CLASH}}\) are plotted in Figure 4.3, as well as the DES magnitudes as a function of the CLASH ones for the matched sources. The magnitudes plotted are SExtractor isophotal magnitudes \textsc{Mag_ISO} for both DES and CLASH. \(\Delta m\) in the \textit{griz} bands has been corrected for the magnitude shifts due to the differences between these DES and HST filters. The offsets have been computed using two “extreme case” SED templates (one elliptical, one irregular) at the cluster redshift. We have not taken into consideration the \(Y\) band offset as the HST and DES filters are too different, but we still report the comparison for completeness.

Figure 4.3 shows an offset in the DES magnitudes, especially in the \textit{gri} bands, which may be due to different choices of threshold or background when running SExtractor.

\(^2\)A software pipeline for embedding simulations into astronomical images. See: https://github.com/emhuff/Balrog.
Figure 4.3: DES magnitudes compared to CLASH magnitudes, with bottom plots of $\Delta m = m_{\text{CLASH}} - m_{\text{DES}}$ in the $g, r, i$ and $z$ bands for the matched sources that satisfy $S/N > 10$ and filtering the sources with $\text{FLAGS} > 3$. CLASH errorbars are not plotted for visualisation purposes, while those on the DES magnitudes represent the $1\sigma$ error. The dashed black lines represent the ideal case $m_{\text{CLASH}} = m_{\text{DES}}$. 
4.4. Comparison of DES and CLASH

<table>
<thead>
<tr>
<th>CLASS_STAR</th>
<th>$g$</th>
<th>$r$</th>
<th>$i$</th>
<th>$z$</th>
<th>SPREAD_MODEL</th>
<th>$g$</th>
<th>$r$</th>
<th>$i$</th>
<th>$z$</th>
</tr>
</thead>
<tbody>
<tr>
<td>G(DES)</td>
<td>551</td>
<td>538</td>
<td>535</td>
<td>522</td>
<td>G(DES)</td>
<td>388</td>
<td>463</td>
<td>428</td>
<td>405</td>
</tr>
<tr>
<td>G(CLASH)</td>
<td>553</td>
<td>553</td>
<td>553</td>
<td>553</td>
<td>G(CLASH)</td>
<td>553</td>
<td>553</td>
<td>553</td>
<td>553</td>
</tr>
<tr>
<td>S(DES)</td>
<td>58</td>
<td>71</td>
<td>74</td>
<td>87</td>
<td>S(DES)</td>
<td>221</td>
<td>146</td>
<td>181</td>
<td>204</td>
</tr>
<tr>
<td>S(CLASH)</td>
<td>56</td>
<td>56</td>
<td>56</td>
<td>56</td>
<td>S(CLASH)</td>
<td>56</td>
<td>56</td>
<td>56</td>
<td>56</td>
</tr>
</tbody>
</table>

Table 4.3: Number of galaxies $G$ and stars $S$ found in DES and CLASH, when considering $\text{CLASS\_STAR} < 0.8$ (top table) and $\text{SPREAD\_MODEL} > 0.003$ (bottom table) for galaxies in DES.

Nevertheless the linear trend is clear, bringing to Pearson coefficients between 0.91 and 0.98 in all bands. The higher scatter that we could expect in the $Y$ band (as the corresponding CLASH filter is the F105W, which is much more spread towards the infrared than the DES $Y$ filter) is actually compensated for by higher DES photometric errors. The mean difference in magnitude $\Delta m$ between the two datasets is 0.13, 0.04, -0.07, -0.07 and 0.08 in the $grizY$ bands respectively.

4.4.2 Star/galaxy separation

For the purpose of studying the star/galaxy separation, we adopt the same notation used in Soumagnac et al. (2015). We study the galaxy completeness $c_g$, defined as the ratio of the number of true galaxies classified as galaxies to the total number of true galaxies (including then also the number of true galaxies classified as stars $M_G$):

$$c_g = \frac{N_G}{N_G + M_G},$$

where here $N_G$ is given by the galaxies in the DES catalogue, and the number of true galaxies is given by the object classified as such in CLASH.

Moreover the galaxy purity $p_g$ is defined as

$$p_g = \frac{N_G}{N_G + M_S},$$

where $M_S$ is the number of stars classified as galaxies.

We consider as true galaxies the sources that have a SExtractor stellarity index $\text{CLASS\_STAR}< 0.08$ in the CLASH catalogue, otherwise they are stars. This cut has been proven to perform well in other CLASH works (e.g. Jouvel et al. 2014). We try to understand if the star/galaxy performance is compatible between the two datasets.
We first consider the CLASS_STAR parameter given in the DES catalogue. We find that a cut between 0.7 and 0.9 for the CLASS_STAR_I gives purity and completeness above the 90%. The number of galaxies and stars in the two catalogues can be found in Table 4.3.

We also test the performance of star/galaxy separation with the SPREAD_MODEL parameter (defined in Desai et al. 2012 and tested in Bouy et al. 2013). SPREAD_MODEL is a morphological star/galaxy separation parameter given by SExtractor which acts as a linear discriminant between the best fitting local PSF model and a slightly “fuzzier” version made from the same PSF model, convolved with a circular exponential model. A threshold is set to 0.003 by the DESDM pipeline to separate stars (PSF like, having absolute values below 0.003) from galaxies (non-PSF like, with values higher than 0.003). As a result, 77.4% of the galaxies are catalogued in DES as such, and the purity is 97.3%. A plot for the purity and the completeness for varying SPREAD_MODEL_I cuts is shown in Figure 4.4. We list the number of galaxies and stars in the two catalogues in Table 4.3. It can be seen from Figure 4.4 that cut at lower values (∼0.001 – 0.002) would give a higher completeness without affecting the purity significantly. Moreover, in this case it may be better using the SPREAD_MODEL in the r band, which is deeper than the i one, and this can also be seen in Figure 4.4, where it is clear that, for the same cut, the completeness is higher. We also find that using the CLASS_STAR parameters with the mentioned cut is more efficient than adopting the SPREAD_MODEL_I with the cut at 0.003.
4.4. Comparison of DES and CLASH

4.4.3 Photo-z

Considering only those matched sources with a signal to noise ratio $S/N > 10$ in the DES $i$-band, excluding stars (in this case we exclude all objects with `CLASS_STAR_I` > 0.8) and objects with `FLAGS` ≠ 0 (in order to exclude objects with saturated pixels or corrupted data, and originally blended sources) we are left with 155 sources. This is the subset of galaxies that we will use for the photo-z and stellar mass comparison.

In order to estimate the photo-z’s, we used LePHARE, which we have described in Chapter 2. While its photo-z performance with DES data has been tested (Sánchez et al. 2014), stellar masses tests have not been performed with the same data so far. We therefore need to further check the DES photo-z and stellar mass estimation with LePHARE first. This is where the HST data are particularly useful in this work, as we need to check DES against a more precise photometric survey covering the wavelengths from optical to IR.

Results

We run LePHARE on both CLASH (with 5, 8 and all 17 filters) and DES (5 filters) catalogues, fitting the 31 synthetic SEDs templates given by the COSMOS (see Ilbert et al. 2009) libraries. We use four galaxy extinction values ranging from 0.05 to 0.3 using a Calzetti et al. (2000) extinction law for DES. For CLASH, two more extinction values are added (0.4 and 0.5), as the wider wavelength range covered by HST allows to constrain a wider range of extinction laws.

The results are plotted in the left panel of Figure 4.5 for the 155 matched sources when 5 filters are considered for CLASH. Of all the sources considered, 85% have a photo-z which is compatible with the CLASH photo-z within the DES requirement $|z_p - z_s| < \sigma(1+z_s)$, where $\sigma = 0.12$. We notice an offset in the CLASH redshift when 17 filters are used (see right panel of Figure 4.5), while 77% of the sources still satisfies the DES requirement. This most likely stems from the inclusion of near-UV filters to get an accurate redshift from the Balmer break for galaxies below a redshift of 0.4 (see e.g. Eisenstein et al. 2001). In fact, this offset starts to be seen also when adding only three UV bands (namely F336W, F390W and F435W) to the grizY filters (see middle panel in Figure 4.5). A problem around redshift 0.4 for DES galaxies had already been seen in Sánchez et al. (2014) (see their Figure 5) and Bonnett et al. (2016). In particular, Bonnett et al. (2016) also pointed

$^3$Where $z_p$ and $z_s$ are the photometric and spectroscopic redshifts, so here we consider the CLASH photo-z as the “spectroscopic” one.
Chapter 4. Stellar mass versus dark matter in galaxy clusters: RXJ2248

Figure 4.5: Comparison of the DES versus CLASH photo-z’s for the sources matched between the two catalogues. photo-z’s were obtained using LePhare. Left: only the 5 HST filters similar to the grizY filters in DES have been used to compute CLASH photo-z’s. Middle: 3 of the HST UV filters have been added to the 5 HST optical filters for the CLASH photo-z estimation. Right: all the 17 available CLASH filters have been used to estimate the photo-z’s. The red dashed line represents $z_{DES} = z_{CLASH}$, and the grey area the expected DES accuracy of $|z_{DES} - z_{CLASH}| < \sigma(1 + z_{CLASH})$, where $\sigma = 0.12$.

out a lack of matching SEDs for galaxies around redshift 0.4 with template fitting methods (see their Figure 8).

Zero points\(^4\) have not been adopted in the DES photo-z estimation, as we saw that their introduction causes systematic effects. Zero points are calculated using field galaxies, so we believe we would need spectroscopy in the cluster field to be helpful at photo-z calibrations for this study.

\[4\] Zero–points define the shift in the observed magnitudes due to various systematics.

4.4.4 Stellar Masses

Stellar masses are key observables in the study of galaxy evolutionary models. Unfortunately, they cannot be directly measured, but require multicolour photometry to be fitted with stellar population models, therefore making a series of assumptions. One of these is the galaxy redshift if spectroscopy is not available: in the view of our goal of computing the stellar mass profile of the RXJ2248 cluster, we have to bear in mind that galaxy redshift accuracy is essential not only to ensure the correct template match in the template fitting method here used and the distance to the galaxy, but also to determine the cluster membership. We will therefore see how the redshift assumptions affect the stellar mass estimation and elaborate a reasonable technique to correctly estimate the stellar mass profile.
Method

We use the same sample of matched galaxies with $S/N > 10$ used in Section 4.4.3 and their redshift estimations in order to compute the stellar masses for both DES and CLASH using LePHARE. In the first place, the redshifts of the galaxies are fixed to those photo-z’s previously computed (i.e. to DES photo-z’s for DES stellar masses, and to CLASH photo-z’s for CLASH stellar masses). In the second case, we fix the galaxy redshifts at the cluster redshift for both DES and CLASH, and the LePHARE DES photo-z’s are only used to select a subsample of cluster members satisfying $|z_{phot} - z_{cl}| \leq 0.12$. For this subsample both DES and CLASH stellar masses are estimated.

We chose to use LePHARE, together with the Bruzual & Charlot (2003) templates, as this combination has been shown to be robust in the estimation of physical parameters of galaxies (Ilbert et al. 2010).

We derive our stellar mass estimates by fitting synthetic SEDs templates while keeping the redshift fixed as described previously in the two cases. The SED templates are based on the stellar population synthesis (SPS) package developed by Bruzual & Charlot 2003 (BC03) assuming a Chabrier (2003) initial mass function (IMF). Our initial set of templates includes 9 models using one metallicity ($Z = 1Z_\odot$) and nine exponentially decreasing star formation rates $\propto \exp(-t/\tau)$ where $t$ is the time and $\tau$ takes the values $\tau = 0.1, 0.3, 1, 2, 3, 5, 10, 15, 30$ Gyr. The final template set is then generated over 57 starburst ages ranging from 0.01 to 13.5 Gyr, and four extinction values ranging from 0.05 to 0.3 using a Calzetti et al. (2000) extinction law. For CLASH, two more extinction values are added (0.4 and 0.5).

The uncertainties on our stellar masses estimates ($MASS\_BEST$ from LePHARE) are given by the 68% confidence limits on the SED fit.

Photo-z consistency test

In this Section we test whether the fact that we assumed a photo-z that was computed with a certain set of templates to then compute the stellar mass with a larger set of templates is consistent. With photometric surveys data, it is a common to perform estimation of the photometric redshift and SED fitting in two steps, which involve fixing the redshift of a galaxy at the best fit value obtained in the first step. Although this may not be the most elegant way of solving the problem of the lack of spectroscopic information, it has
been proven to lead to only a small bias in the SED fitting parameters, when compared to results given by the simultaneous estimation of redshift and stellar mass (see Acquaviva et al. 2015). Moreover, here we can take advantage of the prior information that this is a cluster.

In order to test the consistency of our choice, we want to show that photo-z’s are not drastically dependent on the choice of templates. Therefore, we compare the photo-z’s given by Le Phare when using the COSMOS templates and the BC03 ones. A comparison is shown in Figure 4.6 for all the galaxies in the DES field of view. We retrieve that 71% of the galaxies have $|\Delta z| = |z_{BC03} - z_{COSMOS}| < 0.12$.

**Results**

In Figure 4.7, we show the comparison between DES and CLASH stellar mass estimates for the first case, where the redshifts are fixed to the LePHARE estimates. The linear correlation between the two estimates is clear, but there is an offset of mean value $\sim 0.16$ dex. This should be considered in light of two aspects:

1. the offset in the photo-z’s that we addressed in Section 4.4.3;
2. the uncertainties in the DES stellar masses may be underestimated as those are the 68% confidence limits on the SED fit and do not take into account systematic error contribution.

In Figure 4.8 we show the results for the second case, where we select the galaxies with a DES photo-z close to the spectroscopic cluster redshift $z_{cl}$, satisfying $z_{cl} - 0.12 < z_{phot} <$
4.4. Comparison of DES and CLASH

Figure 4.7: DES stellar masses versus CLASH stellar masses computed using LePhare. In the stellar mass estimation, each source is assumed to be at the redshift given as output by LePhare, as described in Section 4.4.3. The dashed line line represents \( M_{\text{DES}}^* = M_{\text{CLASH}}^* \). In the bottom panel \( \Delta \log(M^*) = \log(M_{\text{DES}}^*) - \log(M_{\text{CLASH}}^*) \) is presented. All available filters (i.e. 5 for DES and 17 for CLASH) have been used in the estimation process. Uncertainties represent the 68% Confidence Level.

\( z_{cl} + 0.12 \). The redshift of these sources is fixed at \( z_{cl} \) in the stellar mass estimation, and the reason for this choice is twofold:

1. to minimise circularity associated with using Le Phare to both measure redshifts and stellar masses;

2. to take into account the shift in the redshift estimates pointed out in Section 4.4.3 (and therefore put at the correct cluster redshift the cluster members whose phot-\( z \) appeared to be at \( z_{phot} \sim 0.4 \)).

Of course this choice results in considering some sources as being at \( z_{cl} \) even though they are not, and we shall take this into account in the following.

The correlation between the estimated stellar masses significantly increases if also the CLASH sources are set to be at the cluster redshift, as seen in a comparison of Figure 4.7 with Figure 4.8, where we find that stellar masses from DES can be estimated within 25\% of CLASH values. This shows that the offset seen in the former is due to the offset in the redshifts given in input, rather than other systematics. Therefore, the wavelengths covered by the DES broadband filters are capable of providing a good estimation of stellar mass if the photometric redshift is sufficiently precise.
Figure 4.8: DES stellar masses versus CLASH stellar masses computed using LePhare. Here only sources around the cluster redshift are considered (i.e. sources with a DES photo-z that satisfies $|z - z_{cl}| \leq 0.12$, where $z_{cl} = 0.3475$ is the cluster redshift). In the DES and CLASH stellar mass estimation, these galaxies are all assumed to be at $z_{cl}$. The dashed line line represents $M^{DES}_{\star} = M^{CLASH}_{\star}$. In the bottom panel $\Delta \text{Log}(M_{\star}) = \text{Log}(M^{DES}_{\star}) - \text{Log}(M^{CLASH}_{\star})$ is presented. The offset seen in Figure 4.7 seems to disappear in this plot, showing that this effect was due to the photo-z offset. All available filters (i.e. 5 for DES and 17 for CLASH) have been used in the estimation process. Uncertainties represent the 68% Confidence Level.

In Figure 4.9 we show the spatial distribution of the total stellar mass spatial distributions for both DES and CLASH in the CLASH field ($\sim 4.8' \times 4.2'$), represented with a resolution of $0.12'/\text{pixel}$ and smoothed with a Gaussian of $\sigma = 0.144$ arcmin. The stellar masses of galaxies are summed over in each pixel. Obviously the two samples show very good agreement in terms of the spatial distribution of stellar mass. The Pearson coefficient for the pixel by pixel stellar mass values of the two non-smoothed maps is 0.93. The difference map without any smoothing has a mean of 0.02 and $\sigma = 0.12$.

### 4.5 Dark Matter and Stellar Masses

In this section we study the stellar mass radial profile of the cluster and relate it to that of dark matter that has been obtained though DES weak lensing studies in Melchior et al. (2016). As shown in Section 4.4.4, stellar mass estimation can be biased if the redshift assumed is biased too, but here we want to adopt a consistent methodology that takes advantage of the fact that we are looking at a cluster with a known redshift. This
Figure 4.9: DES and CLASH total stellar mass maps computed using LePhare for the galaxies matched between the two catalogues. The stellar masses plotted are the same as those shown in the bottom panel of Figure 4.8 (i.e. all the galaxies with a DES photo-z that satisfies $|z - z_{cl}| \leq 0.12$, where $z_{cl}$ is the cluster redshift, have a redshift fixed to $z_{cl}$ in the SED fitting). The map is centred on the BCG, but its stellar mass is not visible as it was originally blended and therefore did not pass the quality flag cut applied in Section 4.4.4. The resolution is $0.12^{\prime}$/pixel and the map is smoothed with a Gaussian of $\sigma = 0.144$ arcmin. At the cluster redshift, $1^{\prime}$ corresponds to 294 kpc in the assumed cosmology.

The technique is outlined in the first part of this section, followed by a study of the different mass radial profiles obtained. To allow a straightforward comparison with the weak lensing reconstructed mass, we compute total stellar mass and surface density on a projected 2-dimensional plane, i.e.:

$$M_\star(R) = \sum_i m_i^\star, \quad \Sigma_\star(R) = \sum_i \frac{m_i^\star}{A_{\text{annulus}}},$$

(4.3)

where the sums are intended over the galaxies within annuli of projected radius $R$. Similar definitions apply for the cumulative distributions $M_\star(<R)$ and $\Sigma_\star(<R)$, computed within circles of radius $R$. The centre of the image is taken to be that of the BCG. At last, we present a comparison between the stellar and total DES mass maps.

### 4.5.1 Galaxy samples and stellar mass estimates

Our goal is to compare the reconstructed mass from weak lensing to the total stellar mass of the cluster members. In order to do so, we split the galaxies into two populations. The
following steps are performed:

- We select the red members using the RedMaPPer SV catalogue (Rykoff et al. 2016b), which identifies cluster members with high precision (Rozo et al. 2014). Their stellar masses are computed using the same parameters presented in Section 4.4.4 (but fixing the redshift at \( z_{\text{cl}} \)).

- The RedMaPPer galaxies profile has been corrected by a factor representing the contribution coming from faint sources at luminosities smaller than the limit of the sample (0.2\( L^* \)). This is done by integrating the luminosity with a Schechter function, i.e. we computed the fraction:

\[
F_L = \frac{\int_0^{0.2L^*} L\phi(L)dL}{\int_{0}^{\infty} L\phi(L)dL},
\]  

(4.4)

where \( \phi(L) = \phi_*(\frac{L}{L^*})^\alpha e^{-L/L^*} \) with \( \alpha = -1 \) (as done in Rykoff et al. 2014 for the SDSS sample, that has properties similar to DES). We find that the galaxies below the luminosity limit contribute to a fraction \( F_L = 0.18 \) of the total luminosity, and therefore, assuming a constant \( M_*/L \) ratio for the red galaxy population, they contribute to the same percentage of stellar mass.

- The contribution to the total stellar mass of each red member is weighted by its membership probability (reported in the RedMaPPer catalogue).

- In order to study the mass profile at radii higher than \( r_{200c} \), we decide not to neglect the contribution coming from the bluer population. First, we exclude all objects with saturated pixels or corrupted data, but include galaxies that were initially blended (such as the BCG). Then we select the rest of the galaxies in the field of view that have magnitudes \( m_i \) in the \( i \) band satisfying \( m_i^{\text{BCG}} < m_i < m_i^{\text{lim}} \). In this way we exclude any source which is brighter than the BCG and cut at \( m_i^{\text{lim}} = 21 \) mag in order to ensure the completeness of the sample. After having performed a SED fitting as in the previous step, we filter out all galaxies that do not give a good fit (cutting on reduced \( \chi^2 < 2 \)) when the redshift is fixed at the cluster value.

### 4.5.2 Masking and background correction

We estimate the survey area lost due to masked regions and blending of faint galaxies with large cluster members near the core. We calculate corrections for both effects as follows.
• **Healpix** (Górski et al. 2005) maps of depth and masking fractions are produced for DES with **Mangle** (Swanson et al. 2008). From these, we calculate mean depth and fractions of masked area in our set of annuli. The depth is approximately constant out to ≈ 50 arcmin from the BCG, which defines the outer limit of the area used for our background estimation scheme. Masking fractions are below 5 per cent for all annuli and applied to the binned stellar mass estimates from both galaxy samples.

• For the blue galaxy sample, some objects are lost due to blending with cluster member galaxies. Without correction, this would bias our stellar mass estimates of blue galaxies near the cluster centre low. We estimate the area lost in each annulus as the isophotal area above the **SExtractor** detection threshold, ISOAREA. This yields a ≈ 7 per cent correction in the innermost arcminute, which drops quickly towards larger radii. For the blue galaxy sample, this correction and the masking fraction are applied in an additive fashion.

The contribution coming from galaxies that do not actually sit at the cluster redshift is removed from the blue galaxies sample by performing a background subtraction: we estimate the projected surface density of the stellar mass $\Sigma_*(R)$ at large radii ($30 - 50$ arcmin, which means outside ≈ $4r_{200}$), where the stellar mass profile tends to become flat. The value found is $\Sigma_* = 1.36 \times 10^{10} M_\odot/\text{arcmin}^2$ and this is subtracted on the smaller scales, with an uncertainty given by a Poissonian error. The remaining stellar mass contribution is then added to that of the red galaxies.

**4.5.3 Stellar mass profile**

We look at the radial distribution of stellar mass, taking into account both the red cluster members present in the **RedMaPPer** catalogue, and the blue members, as explained in the previous section. The splitting into red and blue galaxies is justified by the possibility of improving the SED fitting by using different priors for the two populations, and considering the systematics differently. In fact, it is well known that stellar masses estimated for quiescent galaxies are more reliable than for star-forming ones, partially because the colour–$M_*/L$ (from which $M_*$ is derived) relation are more uncertain for very blue colours (see e.g. Conroy 2013 and Banerji et al. 2013).

\[^5r_{200c} = 2200 \text{ kpc from the NFW fit of Melchior et al. (2016), which means } r_{200c} \simeq 7.46^\prime \text{ at the cluster redshift}\]
Figure 4.10: Cumulative radial distributions of total stellar mass for the DES red (red points), blue (blue points) and all galaxies (purple points) in the cluster, together with the total, non-parametric mass profile reconstructed from DES weak lensing (Melchior et al. 2016, green points). The purple solid line is our NFW fit to the DES stellar mass profile, while the blue solid line is the NFW best fit from DES weak lensing. The black points represent the CLASH total stellar mass profile computed in this work, with our NFW fit (black solid line). The red solid line is the Umetsu et al. (2016) NFW best-fit for CLASH from a strong lensing, weak lensing and magnification joint analysis. This profile is restricted to the NFW fitting range $R < 2\,\text{Mpc} \, h^{-1}$ chosen in Umetsu et al. (2016), which is larger than the HST field of view as other datasets were used in a joint analysis. The radius $R$ is projected, and $r_{200c} = 2.2$ Mpc. Errorbars show the 68% confidence level.
4.5. Dark Matter and Stellar Masses

The total stellar mass cumulative profiles $M_\star(< R)$ for the red and blue galaxies are shown in Figure 4.10. Within the innermost 5 arcmin, the contribution of the red cluster members to the total stellar mass is dominant ($\gtrsim 80\%$) with respect to the bluer galaxies, while at larger radii, namely outside $r_{200c}$, the second population considered gives a $20-50\%$ contribution to the total stellar mass. In Figure 4.10 we also plot the stellar mass profile from CLASH, where the galaxy cluster members were selected cutting on the CLASH photometric redshift with $|z_{phot} - z_{cl}| < 0.12$.

4.5.4 Comparison to total mass from Weak Lensing

The weak lensing mass profile is computed through the aperture mass densitometry (see Clowe et al. 1998) using $M_{tot}(< R) = \pi R^2 \zeta(< R) \Sigma_{cp}(z_l, z_s)$, where $\zeta(< R) = \bar{\kappa}(< R) - \bar{\kappa}(r_1 < r < r_2)$ is the difference between the mean convergence within a circular aperture of radius $R$ and the mean convergence between $r_1$ and $r_2$ (annulus radii that are fixed for all the apertures in the measurement), $z_l$ and $z_s$ are the redshift of lens and sources. The convergence $\kappa$ is defined as the projected surface mass density $\Sigma$, in units of the critical surface mass density $\Sigma_c$:

$$\kappa = \frac{\Sigma}{\Sigma_c}, \quad \Sigma_c = \frac{c^2}{4\pi G} \frac{D_s}{D_d D_{ds}}$$

(4.5)

where $D$ stands for angular diameter distance and the subscripts $s, d, ds$ indicate the distance from the observer to the source, from the observer to the lens, and from the lens to the source respectively. In particular, Melchior et al. (2016) used $r_1 = 30$ arcmin and $r_2 = 45$ arcmin. This explains our choice of estimating the stellar mass surface density background in the range 30 to 50 arcmin, where its profile is also essentially flat. In Figure 4.10 we also present the NFW mass profile derived by using the best fit parameters as found in Melchior et al. (2016) for this cluster. Given the similarity between the WL and stellar mass profiles, we try to fit the stellar mass one with a NFW projected mass profile, as the one derived in e.g. Oaxaca Wright & Brainerd (1999):
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\[
M(< x) = \begin{cases} 
\frac{3\delta c M_{200c}}{200 c_{200}} \left[ \frac{2}{\sqrt{1-x}} \text{arctanh}\sqrt{\frac{1-x}{1+x}} + \ln\left(\frac{x}{2}\right) \right] & (\text{if } x < 1) \\
\frac{3\delta c M_{200c}}{200 c_{200}} \left[ 1 + \ln\left(\frac{1}{2}\right) \right] & (\text{if } x = 1) \\
\frac{3\delta c M_{200c}}{200 c_{200}} \left[ \frac{2}{\sqrt{x^2-1}} \text{arctan}\sqrt{\frac{x-1}{1+x}} + \ln\left(\frac{x}{2}\right) \right] & (\text{if } x > 1) 
\end{cases}
\] (4.6)

where \( x = R/r_s \), \( c_{200} = r_{200c}/r_s \) is the concentration parameter and

\[
\delta c = \frac{200}{3} \ln(1 + c_{200}) - \frac{c_{200}^3}{c_{200}/(1 + c_{200})}. 
\] (4.7)

Our non-linear least squares fit uses the Levenberg-Marquardt algorithm and gives the following parameters for DES stellar mass profile: \( M_{200c}^\star = (5.38 \pm 0.11) \times 10^{12} M_\odot \), \( c_{200}^\star = 2.4 \pm 0.13 \) with a reduced \( \chi^2 = 0.6 \). While fitting a dark matter halo profile with an NFW is justified by dark matter simulations, we are not aware of any work predicting that the stellar mass profile of clusters follows an NFW too. However, we know that galaxies trace dark matter (so their distribution in clusters also tends to follow an NFW profile, as shown in e.g. Popesso et al. 2007), and that their stellar mass correlates with the halo mass, with some scatter. It is thus reasonable to use this as an empirical profile, as it also gives a good fit to the data.

From the DES stellar mass profile and the aperture mass densitometry total matter profile, we derive the stellar mass fraction \( f_\star(< R) = M_\star(< R)/M_{\text{tot}}(< R) \), which is represented by the purple points in Figure 4.11. Within \( r_{200c} \) radius, we find \( f_\star^{\text{DES}}(< r_{200c}) = (6.8 \pm 1.7) \times 10^{-3} \), compatible within \( 1\sigma \) in the outer regions with the result from Bahcall & Kulier (2014): \( f_\star \simeq (1.0 \pm 0.4) \times 10^{-2} \) above \( \sim 300 h^{-1} \) kpc. In their paper, Bahcall & Kulier (2014) examine the stellar fraction profile by stacking > \( 10^5 \) SDSS groups and clusters, divided into 3 richness subsamples.\(^6\) Inside \( r_{200c} \) we recover a lower stellar mass fraction compared to their work. The discrepancy can be explained in light of the different analyses carried out in Bahcall & Kulier (2014):

- Bahcall & Kulier (2014) stack clusters with different properties and at different redshifts.

---

\(^6\)They define the richness \( N_{200} \) as the number of galaxies in the red sequence with rest-frame \( i \)-band luminosity \( L_i > 0.4L^\star \) located within a radius \( r_{200}^{\text{gal}} \) from the BCG (i.e. within the radius where the local galaxy overdensity is 200).
4.5. Dark Matter and Stellar Masses

Figure 4.11: Cumulative radial distribution of the fraction of stellar mass of the galaxies in the cluster as computed in this work over the total mass from lensing studies. For the DES $f_\star$, the total mass comes from the non-parametric reconstruction of the weak lensing shear profile done in Melchior et al. 2016 (purple points), or from their NFW best fit (green squares). For CLASH, $M_{tot}$ is a result of the Umetsu et al. (2016) NFW best-fit for CLASH from a strong lensing, weak lensing and magnification joint analysis (red triangles). The mean DES stellar mass fraction from non-parametric weak lensing mass profile is $f_\star = (7.3 \pm 1.7) \times 10^{-3}$, and is represented by the dashed line. The radius $R$ is projected, and rescaled with $r_{200c} = 2.2$ Mpc. Errorbars show the 68% confidence level.

- They included the contribution of the diffuse intracluster light (ICL), which increases $f_\star$ by a factor 1.15 within $r_{200c}$.

- The luminosity profiles and weak lensing mass profiles have been de-projected to obtain 3D profiles in their work. On the other hand, considering the projected $f_\star$ means that we are including the contribution of the cluster outskirts along the line of sight when we look at cluster core. In these regions, the stellar mass fraction is lower, and this tends to reduce 2D $f_\star$ at small radii with respect the 3D behaviour.

On the other hand, the average stellar mass of the Universe, estimated to be $f_{\star,\text{cosmic}} = (9 \pm 1) \times 10^{-3}$ (as derived in Bahcall & Kulier 2014) is recovered outside $r_{200c}$, as we would expect even for a projected profile.

Overall, no particular radial trend is found, in agreement with Bahcall & Kulier (2014) and also with Andreon (2015), who studied the stellar-to-total mass ratio of three CLASH clusters at $z \sim 0.45$. Nevertheless, a radially varying profile might be hidden by the large errors. In order to reduce the latter, dominated by the weak lensing reconstructed mass,
and have a precise estimation of the stellar mass fraction, we will need to apply the same reasoning to a large sample of DES clusters.

If we take the NFW mass profile with the lensing best-fit parameters as total mass in $f_\star$, we get the green points in Figure 4.11 for DES, and the red ones for CLASH. Towards the centre of the cluster these profiles are higher than the one previously discussed. This is due to the fact that in this case $M_{\text{tot}}$, as can be seen in eq. (4.6), goes to zero for $R \to 0$, while the BCG stellar mass contributes to $M_\star$ up to very small radii. Moreover, the halo/cusp problem (see e.g. de Blok 2010) is a known problem of the NFW profile, that will therefore produce different results from a non-parametric mass profile from weak lensing. Use of the same dark matter halo parameterisation brings the two datasets into agreement at the $1\sigma$ level.

### 4.5.5 DES Stellar Masses and Weak Lensing Mass Maps

In this section, we explore the correlation between the stellar mass maps and the DES weak lensing mass map by Melchior et al. (2016). They adopted the aperture-mass technique from Schneider (1996). The “aperture mass” $M_{\text{ap}}$ is an estimate of the convergence $\kappa$, presented above and proportional to the projected mass density, within a circular aperture. It is defined as a weighted integral over the convergence within the aperture $\vartheta$:

$$M_{\text{ap}}(\vartheta) = \int_0^\vartheta d^2\theta U(\theta)\kappa(\vec{\theta}) ,$$

(4.8)

where a filter $Q$ can be chosen in terms of the filter $U$ so that this expression can be related to the tangential shear $\gamma_t$ with respect to the aperture centre:

$$M_{\text{ap}}(\vartheta) = \int_0^\vartheta d^2\theta Q(\theta)\gamma_t(\vec{\theta}) .$$

(4.9)

If one chooses $U$ to look like a cluster profile, then the aperture mass will act like a bandpass filter applied to the convergence map, and it will provide useful information about the mass distribution within the cluster. Eq. (4.9) needs to be expressed in terms of an observational estimator of the tangential shear, such as the tangential ellipticity $\epsilon_t(\vartheta_j)$ of a galaxy image $j$. Schneider (1996) show that Eq. (4.9) can be rewritten as:

$$M_{\text{ap}}(\vartheta) = \sum_j Q(|\vartheta - \vartheta_j|)\epsilon_t(\vartheta_j) .$$

(4.10)
Figure 4.12: DES total stellar mass distribution (coloured density plot) compared to the mass map \( M_{ap}/\sigma_{ap} \) (from DES WL) and the sum of the galaxies’ ellipticity \( \epsilon_i(\vartheta_j) \) inside the circular aperture \( \vartheta \). Schneider (1996) also show that the variance of the aperture mass is given by:

\[
\sigma_{M_{ap}}^2 = \frac{\sigma^2}{2} \sum_j Q^2(|\vartheta - \vartheta_j|),
\]

where the sum is over all the galaxies’ ellipticity \( \epsilon_i(\vartheta_j) \) inside the circular aperture \( \vartheta \).

where \( \sigma^2 \) is the variance of the intrinsic ellipticity distribution.

In Figure 4.12 we show the DES aperture mass map \( M_{ap}/\sigma_{ap} \) (black contours) and our stellar mass map (coloured density map) in \( 30' \times 30' \) around the BCG position. Both maps, have a pixel scale of \( 0.4997'/\text{pixel} \) and have been smoothed with a Gaussian of \( \sigma = 1' \).

An elongated structure spanning for \( \sim 4 \) Mpc around the BCG is clearly present in both maps, as well as a few clumps lying inside and outside the \( r_{200c} \) radius. Note that the mass structures that can be seen in the total mass map may lie outside the cluster but still cause the lensing, as they are along the line of sight, while the DES galaxies considered here, are only those at the cluster redshift. This fact partially explains why the peaks and minima in the stellar mass and aperture mass maps may be not always coincident. Also, the peak of the stellar mass distribution coincides with the BCG position, while the weak lensing map shows a small offset of the peak from the BCG: Gruen et al. (2013) already
addressed this effect to the expected shape noise studied by Dietrich et al. (2012).

The correlation that can be seen by eye between $M_{\text{ap}}/\sigma_{\text{ap}}$ and $\log M_\star$, is quantified by a Pearson coefficient of $r = 0.30$ when cross-correlating the maps pixel by pixel. Again, the correlation expected between stellar mass and total matter (quantified in this case by the aperture mass and convergence) in a cluster is diminished by the fact that the gravitational lensing gives an integrated information about the mass along the line of sight.

4.6 Conclusions

We compared the catalogues derived from DES and CLASH observations of the galaxy cluster RXC J2248.7–4431, treating CLASH as a validation set for DES. Photometric redshifts and stellar masses for both datasets were computed using LePhare, and we found that stellar masses can be estimated with good precision with DES, despite the lower number of bands available. Gravitational lensing results from both DES and CLASH were used to compare stellar and total mass maps, as well as the mass profiles and stellar mass fraction.

We conclude that:

1. HST data can be used as a validation set for DES data and results. We found that in this case, using the CLASS_STAR parameters with the mentioned cut is more efficient than adopting the SPREAD_MODEL_I with the cut at 0.003.

2. DES photo-$z$’s are compatible with the 17 HST filters photo-$z$’s within the DES requirements. The $z \sim 0.1$ offset observed in the DES photo-$z$’s, is due to a colour-redshift degeneracy that cannot be broken without UV bands at redshifts below 0.4. We found that such offset would percolate into the stellar mass estimates and bias the results by $\sim 0.16$ dex. In order to perform stellar mass studies, we therefore overcame the problem of the redshift estimation for single cluster members by devising a technique as follows. This method treats separately the red galaxies, as found by RedMAPPer, and the blue galaxies. The redshift information can either be the spectroscopic redshift of the cluster, if available, or the RedMAPPer cluster photometric redshift (as RedMAPPer photo-$z$’s are estimated with high precision). In order to estimate the blue galaxies contribution to the stellar mass, we perform a background subtraction which is only possible thanks to the DECam wide field of view.
3. We then estimated total stellar mass and stellar mass fraction profiles for both DES and CLASH, reaching large radii with DES. Within the projected $r_{200c}$ radius, we find a fraction of stellar mass over total mass (derived from weak lensing) $f_\star(<r_{200c}) = (6.8 \pm 1.7) \times 10^{-3}$ with DES, which is compatible with other recent measurements from an independent dataset (Bahcall & Kulier 2014).

4. On cosmological scales the ratio of baryon to total matter densities is $\Omega_b/\Omega_m \approx 16\%$ (e.g. Planck Collaboration et al. 2015). In the cluster core we find that the ratio of stellar mass to total matter is $\sim 0.7\%$. This means that if the cluster distribution is representative, then only 4% of the baryons are locked into stars (compatible within 2$\sigma$ with Fukugita & Peebles 2004).

5. The stellar mass fraction profiles we derive from DES and CLASH are compatible within 1$\sigma$, provided that the same parametrisation is used for the total matter halo profile.

At the time of writing, DES observations have not been completed yet, but clusters catalog have been finalised for Year 1 data. We therefore take the work presented in this Chapter as a pilot analysis for more than 70,000 clusters from the Y1 redMaPPer catalog. In the next Chapters, we show how this huge cluster sample allows to put more stringent constraints on the stellar–to–halo connection.
Chapter 5

Stellar mass as a cluster mass proxy

“It is the unknown we fear when we look upon death and darkness, nothing more.”

J. K. Rowling – Harry Potter and the Half-Blood Prince

The work described in this chapter is part of Palmese et al., 2018 “Stellar mass as a galaxy cluster mass proxy and stellar–to–halo connection in the Dark Energy Survey redMaPPer clusters”, currently in the DES collaboration review process, and the companion papers Welch, Annis, Lin, Palmese, Soares–Santos et al., in prep., and Pereira, Soares-Santos, Makler, Annis, Lin, Palmese et al., 2018, MNRAS 474, 1361P.

5.1 Introduction

Galaxy clusters are fundamental cosmological probes for large galaxy surveys such as the Dark Energy Survey. The estimation of cosmological parameters from clusters abundance is allowed by the dependence of the halo mass function on cosmology (Press & Schechter 1974; Sheth & Tormen 2002; Tinker et al. 2008), but this requires estimates of cluster total masses from the observables of our galaxy survey. In practice, we seek cluster mass
observables (or mass proxies) that tightly correlate with halo mass. In other words they exhibit a low scatter in halo mass at fixed mass proxy (and vice versa).

Several cluster finders are based on the cluster red-sequence (e.g. Koester et al. 2007; Hao et al. 2010; Oguri 2014; Rykoff et al. 2014). Amongst those, redMaPPer has been extensively studied, and its mass proxy $\lambda$, calibrated over several works, as already pointed in Chapter 1. The richness is defined as the sum over the membership probabilities of all galaxies within the projected radius $R_\lambda$. This radius was calibrated against X-ray luminosity measurements $L_X$ in order to minimise the scatter in $L_X - \lambda$. Rykoff et al. (2012) set this variable to $R_\lambda = 1.0(\lambda/100)^{0.2} \text{ Mpc}/h$. On the other hand, there exists broad evidence that the content of clusters includes a non-negligible fraction of bluer, star-forming galaxies that do not follow the red sequence colour-magnitude relation, in particular towards increasing redshift (Oemler 1974; Butcher & Oemler 1978; Butcher & Oemler 1984; Donahue et al. 2002). This effect is known as the Butcher–Oemler effect. Whether the inclusion of the blue cloud can improve cluster mass estimates for cosmology is a matter of debate (e.g. Rozo et al. 2011) and depends on the survey characteristics. At higher redshifts, the blue fraction becomes significant (it can reach $\sim 30\%$ above redshift $\sim 0.3$; Zu & Mandelbaum 2016) and the red sequence is not as distinguishable in colour-magnitude space as at lower redshift. In these regimes, the inclusion of the bluer members may play a significant role in cluster abundance studies of DES and other on-going and future photometric surveys (the Large Synoptic Sky Survey, Euclid) that push towards higher redshifts, $z = 1$ and beyond. One clear advantage of including blue galaxies in cluster catalogs is in studying cluster properties and their evolution with redshift, in particular the Butcher–Oemler effect and quenching mechanisms. Moreover, cluster finders able to identify also cluster members that do not belong to the red sequence (Miller et al. 2005; Soares-Santos et al. 2011) already exist. We are particularly interested in building a mass proxy to implement in the Voronoi–Tessellation (VT) cluster finder, developed by DES collaborators in Soares-Santos et al. (2011). The VT algorithm builds a 2-dimensional tessellation in photometric redshift shells and flags galaxies that lie in high density cells as cluster members. The density threshold is taken from estimates of the 2-point correlation function. The original mass proxy delivered by VT was $N_{VT}$, the number of members identified. In a work based on DES SV data (Saro et al. 2015), the scatter in the $N_{VT}$–mass relation was shown to be too large for any cosmological analysis. For these reasons, we develop a low-scatter mass proxy for cluster finders that are not
red-sequence based.

Previous works (for example Andreon 2012) have exploited stellar masses as a possible cluster mass proxy. We here extend this study by using a larger sample of X-ray clusters for calibration and by complementing the stellar mass estimates with a membership probability scheme. We call this mass proxy “$\mu_\star$”. It is defined as the sum of the stellar mass of cluster galaxies weighted by their membership probability, as we will see in Eq. (5.1). A feasibility study for stellar mass computation with DES data has been presented in Chapter 4, where we found that stellar masses of clusters members can be recovered within 25% of HST-CLASH values. We therefore apply our method to a well-established cluster catalog, the DES Year 1 (Y1) redMaPPer catalog. Nevertheless, this mass proxy can easily be used with other, non-red-sequence based, cluster finders.

This Section is structured as follows. In Section 5.2 we describe the DES Y1 galaxy catalog, the Y1 redMaPPer catalog and the X-ray clusters catalog used. In Section 5.3 we describe the method used to compute cluster stellar masses, the completeness of the sample, and the membership probability assignment scheme. Finally in Sections 5.4 and 5.5 we calibrate our mass proxy against X-ray and weak lensing measurements.

5.2 Data

5.2.1 DES Year 1 and Year 3 data

The data used in this Chapter come from the first year of observations (September 2013 – February 2014, Diehl et al. 2014).

The cluster catalog used here is the cosmology Y1 redMaPPer catalog v6.4.17 with richness $\lambda > 5$, which consists of more than 76,000 clusters. The redshift estimate for each cluster is obtained by maximising the probability that the observed colour–distribution of likely members matches the self–calibrated red sequence model of redMaPPer. The cosmology catalogue is built such that it is volume limited and therefore simplifies our analysis with respect to selection effects. The 2D density plot of richness and redshift of this sample is shown in Figure 5.1. Note that the volume is defined locally, so that it will depend on depth and masking at different positions, thus the decrease at $z > 0.6$. The centre position (given by the galaxy with the highest central probability $p_{cen}$) and the cluster redshift are the only outputs used from this catalog. The galaxies associated with each
Figure 5.1: Distribution in richness $\lambda$ and redshift for the volume–limited sample of DES Year 1 redMaPPer clusters used in this work.

Cluster are taken from the Y1A1 gold catalog. We select objects with \texttt{MODEST\_CLASS}=1 in order to exclude sources that are likely not to be galaxies.

While the cluster catalog is based on Y1 data, the photometry comes from the deeper Year 3 data.

In order to compute the membership probabilities (as described in Section 5.3.1), we use photo-$z$s from the template-based BPZ algorithm. The catalog used in this work uses the same procedure as outlined in Hoyle et al. (2017). Briefly, six basic templates taken from Coleman et al. (1980) and Kinney et al. (1996) were corrected for redshift evolution and any residual calibration errors. Corrections were performed via finding the best-fit template for a subset of the PRIMUS spectroscopic data set (Cool et al. 2013) and computing median offsets between the observed photometry and template predictions within each template type, in a sliding redshift interval, $\Delta z = 0.06$. The magnitude and galaxy type redshift prior was then calibrated using the COSMOS+UltraVISTA photometric redshift catalogue of Laigle et al. (2016). This photo-$z$ catalog was produced by the DES photo-$z$ working group, and has been extensively tested and optimised to provide accurate redshift estimates. For this reason, we decide to trust those photo-$z$’s, rather than computing our own with BMA.

We use the mean of the probability distribution function (PDF) and an estimate of the
width of the PDF, as the full PDF was not available at the time of writing. The member galaxy properties are instead computed assuming the much more precise cluster redshift.

### 5.2.2 X-ray catalogs

The $\mu_\star$-X-ray mass observable relations are computed using *XMM* and *Chandra* data. The DES Y1 redMaPPer cluster catalog is used to find galaxy clusters on the X-ray databases at the same positions. Consequently, the samples are not X-ray selected, but at the same time X-ray temperature and luminosity measurements are not available for all of the redMaPPer clusters.

The X-ray Multi–Mirror Mission (*XMM*; Jansen & Laine 1997) is a European Space Agency space mission launched in 1999. The *XMM* Cluster Survey (*XCS*) consists in a search for galaxy clusters in archival *XMM-Newton* observations. In order to derive the cluster X-ray temperature and luminosity, we use the *XCS* Post Processing Pipeline (*XCS3P*) as described in Manolopoulou et al. (in prep), and briefly describe the methodology here. Cluster spectra are extracted and fit using the *xspec* (Arnaud 1996) package, performed in the 0.3-7.9 keV band with an absorbed MeKαL model. The cluster spectra are extracted within $r_{500c}$, which is estimated through an iterative procedure. An initial temperature is estimated using the XAPA source detection region (Lloyd-Davies et al. 2011), and $r_{500c}$ estimated from the $r_{500c}$-$kT$ relation of Arnaud et al. (2005). This process is then iterated until $r_{500c}$ converged to within 10%. Furthermore, during each iteration, a calculation of coefficient of variation (Koopmans et al. 1964) of $T_X$ is performed, defined as the ratio of the standard deviation ($\sigma$) to the mean ($\mu$), given by $C_v = \sigma(T_X)/\mu(T_X)$. In this work, we adopt a value of $C_v < 0.25$ as an indicator of a reliable measurement of the iterative temperature. For our final temperature–mass proxy relation analysis we select a high signal-to-noise subsample by excluding clusters with relative temperature error $\sigma_T > 30\%$ and redMaPPer richness error $\sigma_\lambda > 15\%$. The final sample is composed of 74 clusters in the DES Y1 wide field.

The *Chandra X-ray Observatory* is a NASA telescope launched in 1999. In order to obtain X-ray temperatures and luminosities for archival *Chandra* data, we use the Mass Analysis Tool for *Chandra* (MATCHa) pipeline, described in detail in Hollowood et al. (2018). Briefly, this pipeline finds, downloads, and cleans archival *Chandra* data for each of its input cluster candidates. It then iteratively finds a galaxy cluster centre (until converged within 15 kpc), and iteratively fits X-ray temperatures and luminosities within
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500 kiloparsec, \( r_{2500c} \), and \( r_{500c} \) apertures. As with XCS3P, MATCHa performs its fitting using xspec, with an absorbed MeKaL model. Unlike XCS3P, MATCHa performs its fits within the 0.5–2.0 keV band. For consistency with the XCS selection, we apply the same signal-to-noise–ratio (SNR) cut to this sample. We choose to use temperatures within \( r_{2500c} \) for this sample because they are more accurate for nearby clusters, where the \( r_{500c} \) apertures become too big compared to the Chandra chip. Our final Chandra sample is composed of 69 clusters in the DES Y1 wide field.

5.3 Method

The BMA method in clusters

Rykoff et al. (2016a) showed that the redMaPPer photometric redshifts for DES are excellent, with errors of the order \( \sigma_z/(1 + z) \sim 0.01 \) up to \( z \sim 0.9 \). This allows us to safely assume the cluster redshift for the cluster members and to avoid exploring the photo-z dependence of stellar masses, as was done in another DES study by Capozzi et al. (2017). Despite the fact that in the present work we can safely assume that the cluster redshift is a good estimate of the real galaxy redshift, all the other assumptions made on the galaxy templates (e.g. metallicity, star formation histories) remain unconstrained. We therefore choose not to ignore the uncertainty on model selection and use the BMA code presented.
in Chapter 2 to estimate stellar masses and other properties of the single galaxies, from which we derive the total cluster stellar masses. We test our results against the Millennium simulation semi-analytic model from De Lucia & Blaizot (2007)\(^1\), and show the results for the sum of stellar mass in clusters, in Figure 5.2. We run the BMA algorithm using the simulated magnitudes for the *griz* SDSS filters, which are very similar to the DES ones. In this case the scatter of the bias distribution is even lower ($\lesssim 0.1$ dex) than what we found in the comparison with the COSMOS results, showing that our method works well against other SED fitting methods and simulations.

**Completeness of the stellar mass sample**

The galaxy sample described in Section 5.2 is cut at $M_r < -19.8$, where $M_r$ is the $r$-band absolute magnitude. Absolute magnitudes were estimated using K-corrections computed from galaxy templates generated by kcorrect v4.2 (Blanton & Roweis 2007). We took each galaxy’s redshift to be the same as its photo–$z$, found the closest kcorrect template on a grid of redshift and colours ($g-r$, $r-i$, and $i-z$), and used that template’s K-correction from observed $i$-band to rest-frame $r$-band to calculate $M_r$. An absolute magnitude cut $M_r$ brighter than $-19.8$ was then applied to the galaxy catalog before computing membership probabilities. This cut ensures that our galaxy sample is volume limited across the redshift range considered. In Figure 5.3 we show the observed $r$-band magnitudes that the galaxies in our sample would have if they had an absolute magnitude $M_r = -19.8$ as a function of redshift. These are computed using the $k$-corrections and distance modulus output by our BMA code for the galaxies with a membership probability $> 15\%$ (corresponding to the median of the membership probability distribution), in order to be representative of a realistic cluster galaxy population. We show that the $90^{\text{th}}$ percentile of the distribution in redshift bins is below the $95\%$ completeness limit of the DES Y1A1 gold catalog (22.9 in $i$–band) over the redshift range covered by the redMaPPer cosmology catalog. We compare to the Y1 magnitude limit as our galaxy catalog contains objects detected in Y1, even if they are matched to the deeper Y3 photometry. We can conclude that with the chosen cut we are $\gtrsim 90\%$ complete.

In order to estimate the completeness in stellar mass, we look at the mass $M_\text{lim}^\star$ each galaxy would have, at its redshift, if its absolute magnitude were equal to $M_r^\text{lim} = -19.8$. This can be achieved by converting the mass-to-light ratio fitted by BMA through

\(^1\)http://gavo.mpa-garching.mpg.de/Millennium/Help?page=databases/millimil/delucia2006a
Figure 5.3: Analysis of the completeness of the galaxy sample. Top panel: observed $i$-band magnitudes that the galaxies in our sample would have if they had the absolute magnitude used as our limit ($M_{r}^\text{lim} = -19.8$). The shadowed region represents the DES Y1 95% completeness limit from Drlica-Wagner et al. (2017). Bottom panel: limiting mass $M_{\ast}^\text{lim}$ that each galaxy would have, at its redshift, if its absolute magnitude were equal to $M_{r}^\text{lim} = -19.8$. The limiting mass is below $10^{10} M_\odot$ at all redshifts; we therefore cut our sample at this stellar mass. The shadowed region represents this cut. The dashed lines are the 50th and 90th percentile of the distributions.
\[ \log(M_r^{lim}) = \log(M_r) + 0.4(M_r - M_r^{lim}) \]

where \( M_r \) and \( M_* \) are the galaxy estimated absolute magnitude and stellar mass. From Figure 5.3 it is clear that, if all the galaxies were at \( M_r^{lim} \) or fainter, \( \gtrsim 90\% \) of them would have a stellar mass \( \lesssim 10^{10} M_\odot \). We therefore are \( \gtrsim 90\% \) complete above \( M_* = 10^{10} M_\odot \) over the whole redshift range. The scatter in mass at each redshift is given by the scatter in \( M/L \) of the different models. We therefore cut our stellar mass sample at \( M_* > 10^{10} M_\odot \).

### 5.3.1 From galaxy stellar masses to \( \mu_* \)

The cluster mass proxy \( \mu_* \) is computed by weighing the stellar mass of each galaxy in the cluster by its membership probability \( p_{\text{mem},i} \):

\[
\mu_* = 10^{-10} M_\odot^{-1} \sum_i p_{\text{mem},i} M_{*,i},
\]

where the factor \( 10^{-10} \) simply gives to the mass proxy an order of magnitude similar to that of the number of observed cluster galaxies. The sum is over all the galaxies from the DES Y1A1 gold catalog having \( M_r < -19 \) and within 3 Mpc from the centre of the cluster as given by the redMaPPer Y1 catalog. The errors on \( \mu_* \) were computed using jackknife resampling. Intuitively, this method allows us to estimate the variance on our estimator by considering a galaxy cut from the cluster at each time.

**Membership probability assignment**

The membership probability for a galaxy in a cluster is given by

\[
p_{\text{mem}} = p_R p_z,
\]

where the components represent the probability of the galaxy being a member given its redshift \( p_z \) and its projected distance from the cluster centre \( p_R \). The radial probability \( p_R \) is assigned by assuming a projected Navarro–Frenk–White (NFW; Navarro et al. 1996) profile, with \( R_{200c} \) computed by counting galaxies within 3 Mpc and finding the halo profile by assuming an Halo Occupation Distribution model. Useful information is also contained in the colour probability. In order to assign these probabilities to each galaxy in a cluster, we therefore need to complete the following steps:
1. **Assign redshift probabilities.** By assuming that each galaxy redshift follows a Gaussian probability density function (PDF) with the mean being the observed photometric redshift $z$ and the standard deviation being the uncertainty in the photometric redshift $\delta z$, we define the probability as the integral of the redshift PDF over a window around the redshift of the cluster $z_0$:

$$p_z = \int_{z_{\text{min}}}^{z_{\text{max}}} \frac{1}{\sqrt{2\pi}(\delta z')} e^{-\frac{(z' - z_0)^2}{2(\delta z')^2}} dz'. \quad (5.3)$$

In general, photo-$z$ PDFs are not Gaussian. However, full PDFs are not available for Y3 data, so this is our best estimate. In order to account for changing photometric redshift uncertainties at different redshifts, we evolve the size of the window with redshift based on the median photometric redshift uncertainty $\langle \delta z \rangle$ of galaxies in our sample at a given redshift. The bounds of our integral $z_{\text{min}}$ and $z_{\text{max}}$ are defined to evolve as

$$z_{\text{min}} = z_0 - \langle \delta z \rangle$$
$$z_{\text{max}} = z_0 + \langle \delta z \rangle \quad (5.4)$$

This redshift probability gives galaxies of approximately the same redshift as the cluster centre a greater weight than galaxies at vastly different redshifts.

2. **Count galaxies.** We count all galaxies along the line of sight within circular apertures with radii $0.1 \leq r \leq 3.0$ Mpc, weighted by $p_z$. This effectively selects galaxies near the cluster redshift while avoiding a sharp, arbitrary cutoff in redshift. The redshift weighted galaxy number counts as a function of radius are divided by the surface area at each radius. This converts our number counts into a surface density, which is background-subtracted.

3. **Background subtraction.** Background or foreground galaxies are likely to enter into our number counts. To remove this contribution, we measure a local background galaxy density in the environment around each cluster. Similarly to the previous step, this contribution is estimated by summing the photo-$z$ probability weighted galaxy counts in an annulus around the cluster. We choose the internal radius of this annulus to be 4 Mpc in order to be far enough away from the cluster virial radius. The outer radius was chosen to be 6 Mpc to provide a sizable area to smooth
out small fluctuations in density. The derived profile is transformed into a surface density and subtracted from the cluster surface density.

4. **Estimate cluster radius.** This step is performed by assuming the HOD model of Tinker et al. (2011). We interpolate the background subtracted cluster mass density within our apertures to find where the density equals 200 times the critical density, thus giving our value of $R_{200c}$. This is needed to assign radial probabilities.

5. **Assign radial probabilities.** Radial probabilities take into account the size of the cluster, and thus are needed to avoid assigning high probabilities to galaxies that live at the edges of clusters. Our radial probability assume a projected NFW mass profile, of the form (Wright & Brainerd 2000):

$$
\Sigma(R) = \begin{cases} 
\frac{2 \rho_s R_s}{r^2 - 1} \left[ 1 - \frac{2}{\sqrt{r^2 - 1}} \arctan \sqrt{\frac{r-1}{r+1}} \right] & r > 1 \\
\frac{2 \rho_s R_s}{3} & r = 1 \\
\frac{2 \rho_s R_s}{r^2 - 1} \left[ 1 - \frac{2}{\sqrt{1-r^2}} \operatorname{arctanh} \sqrt{\frac{1-r}{1+r}} \right] & r < 1 
\end{cases} \tag{5.5}
$$

where $r = R/R_s$, and $R_s = R_{200c}/c$ is the scale radius, with $c$ being the concentration parameter set to $c = 3$.

The radial probability is computed from Eq. (5.5) as:

$$p_R = \frac{k \Sigma(R)}{k \Sigma(R) + \Sigma_{bg}}, \tag{5.6}$$

where $k$ is a constant given by the background subtracted surface number density $n_{tot} - n_{bg}$ and $\Sigma_{bg}$ is the background surface density. The redMaPPer membership probability scheme has already included a similar approach in the so-called “radial filter” described in Rozo et al. (2009b).

6. **Assign colour probability.** Colour probabilities $p_c$ are estimated through a purely empirical method, the Gaussian Mixture Model (GMM). This method has been previously adopted by Hao et al. (2009), who have showed that the bimodal colour distribution of galaxies in clusters is well fit by two Gaussian for SDSS clusters.\(^2\)

The fit is performed using a modified version of scikit-learn Python package

\(^2\)DECam griz filters are extremely similar to the SDSS ones, thus a similar fit works for DES data too.
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Figure 5.4: Colour distribution in $g - r$ of a cluster at $z = 0.14$ from the Y1 redMaPPer sample, given as an example. The histogram is made by counting all galaxies within 3 Mpc of the cluster center, weighted by their membership probability and after background subtraction. The red and blue Gaussians represent the best fit of the red sequence and blue cloud from the Gaussian Mixture Model after background subtraction. (Pedregosa et al. 2011). In this work, we fit two Gaussians to the colour distribution of the galaxies in each cluster, weighted by their radial and redshift probabilities. The Gaussians fit the colour distribution of the red sequence and blue cloud of cluster galaxies well. Figure 5.4 shows the two Gaussians for a randomly selected cluster from the Year 1 redMaPPer sample. A Gaussian PDF for the probability that a galaxy would have colour $x$ given it is in a colour distribution of mean colour $\mu$ and variance $\sigma^2$ can be written as:

$$p(x|\mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}.$$  \hspace{1cm} (5.7)

We define a colour probability density that a galaxy with colour $x$ is a member of a cluster with red and blue Gaussian colour distribution given by $\mu_r, \sigma_r$ and $\mu_b, \sigma_b$ from the GMM fit as:

$$u \Pi(x) = w_r p(x|\mu_r, \sigma_r^2) + w_b p(x|\mu_b, \sigma_b^2),$$  \hspace{1cm} (5.8)

where $w_r$ and $w_b$ are the area of the Gaussians and satisfy $w_r + w_b = 1$. Finally, we
compute the probability that the galaxy is in the cluster given its colour:

\[ p_c = \frac{\kappa \Pi(x)}{\kappa \Pi(x) + N_{bg}(x)}, \]

(5.9)

where \( \kappa \) is the background-subtracted number of galaxies. We can also define the probability of being in the red sequence:

\[ P(RS|x) = \frac{\kappa \Pi_{RS}(x)}{\kappa \Pi_{RS}(x) + N_{bg}(x)}, \]

(5.10)

where

\[ \Pi_{RS}(x) = w_r p(x|\mu_r, \sigma_r^2). \]

(5.11)

These probabilities are computed for the available colours \( g - r \), \( r - i \), and \( i - z \).

The colour probabilities are needed to assign a lower \( p_{\text{mem}} \) to galaxies that are likely part of the foreground/background. As we have already mentioned, clusters are known to follow a bimodal colour distribution, and in particular a tight red sequence with a small colour scatter. By providing this extra information, we are able to assign a higher membership probability to galaxies which are more likely to be members based on the colours actually observed in clusters.

## 5.4 Calibrating \( \mu_* \) against X-ray mass observables

### 5.4.1 The \( T_X - \mu_* \) relation

Following previous works (e.g. Rozo et al. 2009a; Rozo et al. 2011; Mulroy et al. 2014), we perform a Bayesian linear regression of the scaling relation between the logarithm of the X-ray mass proxy (in this case the temperature \( T_X \)) and the logarithm of our photometric mass proxy, including an intrinsic scatter \( \sigma_{\text{Log}T_X|\mu_*} \) of the temperature at fixed \( \mu_* \). A Bayesian linear regression assumes Bayes’ theorem in its formalism, and we choose this method because it easily allows the inclusion of an intrinsic scatter. The formalism is presented in Section 6.3 for a more generic case, where we will need to include an extra variable in the fit which is not permitted in publicly available routines. Namely, we fit:

\[ \langle \text{Log} T_X|\mu_* \rangle = \alpha + \beta \text{Log}(\frac{\mu_*}{\mu_*}), \]

(5.12)
where $\mu_* = 1000$ is roughly the mean $\mu_*$ of the sample. We use the publicly available Python version of Kelly 2007 and separately fit the X-ray temperatures presented in Section 5.2.2 for the XMM and Chandra samples. We perform separate fits for the two samples as combining different temperature measurements is not straightforward and we are not interested in fitting a generic $T_X - \mu_*$ relation but rather to test our methodology against other well established mass proxies. The results of the regression are reported in Table 5.1 and shown in Figure 5.5. The slope found for the Chandra temperatures is shallower ($\beta = 0.295^{+0.070}_{-0.071}$) because the dynamical range explored by $T_X$ is not as wide as in the XMM sample and some cluster temperatures have a very low signal-to-noise in the low $T_X$ and low $\mu_*$ end regimes (thus they are cut by our SNR selection). Farahi et al. (in prep.) also find a shallower slope in the $T_X - \lambda$ relation for the Chandra sample matched to Y1 redMapper clusters. The mass proxy seems to correlate better with the XMM temperatures, resulting in a slope of $\beta = 0.483 \pm 0.053$.

The weak lensing mass–$\mu_*$ relation studied in Pereira et al. (2018) and presented in Section 5.5 is a preliminary analysis of our new mass proxy based on SDSS redMaPPer clusters, made before DES Y1 cluster catalogues were available. In that work, we find a steeper slope $(1.74 \pm 0.62$ at $0.1 < z < 0.33$) than the analysis presented here. We believe that the correlation of stellar mass with total cluster mass is higher than with the X-ray temperatures because the X-ray measurement only probes the inner part of the cluster gravitational potential (within $R_{500c}$ and $R_{2500c}$ for the XMM and Chandra data respectively), while the weak lensing probes larger radii.

We perform the same linear regression of Eq. (5.12) with the X-ray luminosities in units of $10^{44}\text{erg/s}$ in place of the temperatures. Results are reported in Table 5.1. We find a larger scatter for this relation, which is expected as the temperature directly probes the potential well of the halo, while the luminosity depends primarily on the density of the Intra–cluster Medium (ICM). This causes baryon effects to be included to a higher order and the scatter with halo mass to increase.

### 5.4.2 Intrinsic scatter

We find an intrinsic scatter of $\sigma_{\log T_X | \mu_*} = 0.152^{+0.017}_{-0.015}$ for the XMM sample, which is only $\sim 2\sigma$ above the value that we get if we reproduce the same analysis with the redMaPPer richness: $\sigma_{\log T_X | \lambda} = 0.121^{+0.014}_{-0.013}$. This is a promising result in light of the fact that the redMapper mass proxy has been refined and optimised over several works (Rozo et al.
5.4. Calibrating $\mu_*$ against X-ray mass observables

| Sample–observable | # of clusters | $\alpha$ | $\beta$ | $\sigma_{\log(T/L_X|\mu_*)}$ |
|-------------------|---------------|---------|--------|-----------------------------|
| XCS–$T_X$         | 74            | 0.580$^{+0.021}_{-0.021}$ | 0.483$^{+0.064}_{-0.065}$ | 0.152$^{+0.015}_{-0.015}$ |
| XCS–$L_X$         | 74            | 0.392$^{+0.064}_{-0.065}$ | 1.54$^{+0.17}_{-0.17}$ | 0.514$^{+0.031}_{-0.047}$ |
| Chandra–$T_X$     | 69            | 0.784$^{+0.022}_{-0.022}$ | 0.295$^{+0.070}_{-0.071}$ | 0.139$^{+0.015}_{-0.014}$ |
| Chandra–$L_X$     | 69            | 0.644$^{+0.062}_{-0.062}$ | 0.84$^{+0.053}_{-0.20}$ | 0.436$^{+0.040}_{-0.037}$ |

Table 5.1: Fits of the scaling relation following Eq.(5.12) for X-ray temperatures and luminosities. Values represent the median of the parameters posterior distribution, and the errors are the 16th and 84th percentiles. Temperatures are in units of keV and luminosities in $10^{44}$ ergs$^{-1}$.

Figure 5.5: Bayesian linear regression of X-ray temperature and $\mu_*$ for the XCS high signal-to-noise sample (top panel) and the Chandra sample (bottom panel). The grey points are our sample data points, the blue points are the mean temperature and mass proxy values in $\mu_*$ bins. The red lines are a random sample from the posterior distribution of slope and intercept, and the blue band represents 1$\sigma$ around the mean value of the intercept plus the intrinsic scatter.
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Figure 5.6: Bayesian linear regression of X-ray luminosity and $\mu_*$ for the XCS high signal-to-noise sample (top panel) and the Chandra sample (bottom panel). The grey points are our sample data points. The red lines are a random sample from the posterior distribution of slope and intercept, and the blue band represents $1\sigma$ around the mean value of the intercept plus the intrinsic scatter.
5.4. Calibrating \( \mu_* \) against X-ray mass observables

and that the sample was selected using richness cuts \( (\sigma_\lambda < 15\%, \lambda > 5) \). No cuts have been performed based on \( \mu_* \). The scatter on \( T_X \) from the Chandra sample is similar \( (\sigma_{\log T_X|\lambda} = 0.139_{-0.014}^{+0.015}) \) and it is also less than \( 2\sigma \) above the redMaPPer richness estimate \( (0.118_{-0.014}^{+0.014}) \).

The value found for the XMM scatter corresponds to a 41\% scatter \( (10^0 - 1) \): even though it is not straightforward to compare results computed with different methods and using different samples, several works find that the intrinsic scatter is \( \sigma_{\log M_h|X} = 10 - 70\% \) for a mass proxy \( X \) (see Table 3 of Mulroy et al. 2014 for a comparison). This result shows that our mass proxy is competitive with other methods of cluster mass estimation. Note that the scatter computed here is different from what we would find for the total cluster mass at fixed \( \mu_* \). In fact, as suggested in the previous subsection, not only do current X-ray temperature measurements probe a restricted cluster scale, but they are also influenced by gas and baryon physics. In other words, there is a non-negligible intrinsic scatter between total cluster mass and X-ray mass observables \( (\sigma_{\log L_X|M_h} \sim 0.17 \) in Vikhlinin et al. 2009).

We perform a number of tests to understand if the membership probabilities are taken into account in an optimal way. We find that including the blue cloud galaxies does not bring a significant increase in the scatter: the inclusion of the second term in the right-hand side of Eq. (5.8), compared to having the red sequence term only or redMaPPer members only, brings an additional scatter which is an order of magnitude lower than the error. This is consistent with what we would expect for this sample, as it has been matched to a red-sequence cluster finder. Rozo et al. (2011) found that the blue galaxies significantly increase the scatter of their sample, but the fact that this is not true in our case allows us to keep this contribution which may become relevant at low richness and high redshift regimes, which should be tested using a non-red sequence based cluster finder and matched against other mass observables. It is beyond the scope of this work to test this hypothesis. Rozo et al. (2011) also show that differences between the true and predicted scatter of the mass proxy–mass relation are irrelevant for a DES–like survey as long as these differences are about 5\% or less (i.e., \( \Delta \sigma < 0.05 \)), which further supports our choice.

We find that the inclusion of the radial probability works well in terms of the choice of an arbitrary radial cut between \( 0.7 \) and \( 3h^{-1} \) Mpc: in fact, the intrinsic scatter of the temperature-mass relation is independent of this choice. On the other hand, we tested the use of the red galaxies only without including the radial probability contribution. In this
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Case, we find similar trends to previous work (e.g. Andreon 2015): optimal choices for the aperture do exist when no membership probability is considered. We find that the scatter can increase by up to $\sim 15\%$ within the inner 1.5 Mpc, and outside that range mostly noise is added.

We tested the inclusion of colour probabilities $p_c$ in the full membership probabilities by modifying Eq. (5.2) into $p_{\text{mem}} = p_R p_c p_c$. We also tried to combine the colour membership probabilities from different colours in different redshift ranges. This is justified by the fact that most of the colour information in a galaxy SED is contained in the 4000 Å break, that shifts between the bands with redshift. We therefore use $g-r$ for the range $z < 0.35$, $r-i$ in $0.35 < z < 0.75$ and $i-z$ at $z > 0.75$. We find that these tests did not have a significant impact on the mean scaling relation fit and intrinsic scatter, so it is reasonable to include the simpler version of the full probabilities as given in Eq. (5.2).

The fact that our scaling relation scatter and slope are insensitive to the choices made in these tests shows that the membership probabilities are robust and that cluster size and colours (that enter in $p_{\text{mem}}$ though the redshift probability estimation) are taken into account well.

Finally, we estimate the scatter of halo mass at fixed mass proxy, which is a quantity of interest in cosmological studies. In fact, the halo mass scatter about the mean mass–observable relation is one of the main systematics that need to be taken into account. We follow Rozo & Rykoff (2014) and estimate this quantity through:

$$\sigma^2_{M|\mu_*} = \sigma^2_{T|\mu_*} \frac{\beta^2}{\sigma^2_{M|T}} - \sigma^2_{M|T} ,$$  \hspace{1cm} (5.13)

where variables are in natural logarithm (in order to use results from the literature), the scatter in mass at fixed $T_X$ has a fiducial value of 15% and the slope of the $M - T_X$ relation is $\beta = 1.5$. We find that $\sigma_{\text{Log}M|\text{Log}\mu_*} \sim 0.19$, while $\sigma_{\text{Log}M|\text{Log}\lambda} \sim 0.12$ for the XMM sample. Rozo & Rykoff (2014) also find $\sigma_{\text{Log}M|\text{Log}\lambda} \sim 0.11$ when comparing redMaPPer SDSS measurements to XCS temperatures. Note that this is only a qualitative estimate of the scatter on halo mass, and the results presented are only used to investigate the performance of our mass proxy. A careful modelling of the cluster selection effects, an estimate of the correlation coefficient for $\mu_* - T_X$ to be included in Eq. (5.13), simulations and Fisher matrix forecasts would be needed in order to evaluate the actual impact of $\mu_*$ on cosmological parameters. DES collaborators Farahi et al., in prep., are already working
5.5. Weak lensing calibration

Figure 5.7: Weak lensing mass calibration of $\mu_*$ from Pereira et al. (2018). The shaded regions represent 2$\sigma$ confidence intervals. Miscentering corrections have been applied to the mass estimates. In the mass–$\mu_*$ relation we adopt the median of $\mu_*$ as the mass proxy pivot, which is, in order for the three panels: $\mu_0^\star = 5.16 \times 10^{12} M_\odot$ (redMaPPer low redshift sample), $\mu_0^\star = 7.30 \times 10^{12} M_\odot$ (VT low redshift sample), $\mu_0^\star = 6.30 \times 10^{12} M_\odot$ (VT high redshift sample). In this work, we decided to leave $\mu_*$ in units of $M_\odot$, so the factor $10^{-10} M_\odot^{-1}$ from Eq. (5.1) is not taken into account.

on a similar modelling for $\lambda$. Based on their results, the error on the scatter on halo mass at fixed richness is large enough to make $\sigma_{\log M | \log \lambda}$ and $\sigma_{\log M | \log \mu_*}$ consistent within 1$\sigma$.

In the future, we plan on studying these effects for $\mu_*$ as well.

5.5 Weak lensing calibration

In Pereira et al. (2018) we use two cluster samples from the SDSS Stripe 82 data to calibrate $\mu_*$ and $\lambda$ against weak lensing measurements: 230 redMaPPer clusters at redshift $0.1 \leq z < 0.33$ and 136 VT clusters at $0.1 \leq z < 0.6$. The source galaxy catalog used comes from the CS82 survey (Erben et al. 2017), with shape measurements and photometric redshifts from matched SDSS co-add (Annis et al. 2014) and UKIDSS YJHK (Lawrence et al. 2007) photometry. Clusters are stacked in $\mu_*$ bins to measure a mass-observable power law relation of the form:

$$\langle M_{200c} | \mu_* \rangle = M_0 \left( \frac{\mu_*}{\mu_*^0} \right)^{\alpha}. \quad (5.14)$$

Mass proxy bins have been chosen in order to have a similar number of clusters in each bin. For redMaPPer clusters we obtain $M_0 = (1.77 \pm 0.36) \times 10^{14} h^{-1} M_\odot$, $\alpha = 1.74 \pm 0.62$, while for VT clusters: $M_0 = (4.31 \pm 0.89) \times 10^{14} h^{-1} M_\odot$, $\alpha = 0.59 \pm 0.54$ and $M_0 = (3.67 \pm 0.56) \times 10^{14} h^{-1} M_\odot$, $\alpha = 0.68 \pm 0.49$ for the low and high redshift bins, respectively. This fits are shown in Figure 5.7. The results found for the redMaPPer richness with
this method \( M_0 = (2.46 \pm 0.44) \times 10^{14} h^{-1} M_\odot; \alpha = 1.18 \pm 0.38 \) are consistent with the literature (Simet et al. 2017; Melchior et al. 2017; Oguri 2014), showing that this method can be applied to any cluster-finding algorithm, including VT. The on-going work consists in replicating this analysis using DES Year 3 data, which comprises of a larger and deeper sample than SDSS.

5.6 Conclusions

In this Chapter we presented a stellar mass based mass proxy that can be applied to photometric surveys. Our main results can be summarised as follows:

- The outputs of our BMA code presented in Chapter 2 are used to estimate our mass proxy \( \mu_* \) for DES Year 1 data. We study the scatter of this mass proxy compared to X-ray mass observables: we find \( \sigma_{\log T_X|\mu_*} = 0.152^{+0.017}_{-0.015} \) and \( 0.138^{+0.015}_{-0.014} \) for the XMM and Chandra temperatures respectively. These values are consistent within 2\( \sigma \) with the results from the redMaPPer richness \( \lambda \). Given that \( \lambda \) has been extensively studied and optimised to reach the lowest levels in scatter, we conclude that also \( \mu_* \) is a promising low-scatter mass proxy.

- It is a sensible choice to develop a new mass proxy using a well known sample of clusters, and also to compare results with a well-established mass proxy in order to validate the method used. In this spirit, \( \mu_* \) has been calibrated with weak lensing measurements for redMaPPer and VT clusters from SDSS and CS82 data. The analysis has been performed also with the redMaPPer richness, where results are consistent with others from the literature, showing that it is robust. The slope found in the mass proxy–halo mass relation for redMaPPer clusters is similar for \( \lambda \) and \( \mu_* \). This indicates that the correlation of our mass proxy with halo mass is just as good as for the redMaPPer proxy. However, this comparison is only valid where \( \lambda \) is available, i.e. in SDSS clusters which only go out to redshift 0.3. It is in our interests to explore comparisons with red-sequence cluster finder out to larger redshifts, where the red sequence width increases. The same analysis is currently being performed for DES Year 3 data, where clusters are probed out to \( z \lesssim 1 \). Our mass proxy has not been optimised or studied as much as the redMaPPer richness, and thus it is not as ready as \( \lambda \) for cosmological analyses yet. However, it is physically
motivated and provides stellar mass estimates which are not an output of redMaPPer clusters.

• Future work will include the development of a new version of the VT cluster finder, that integrates this mass proxy into the pipeline (Bugard et al., in prep.), and a production of a cluster catalog for DES data. We also plan to perform an “end–to–end” analysis to quantify the impact of this mass proxy on cosmological parameters.
Chapter 5. Stellar mass as a cluster mass proxy
Chapter 6

Cluster evolution results from DES Year 1 redMaPPer clusters

It is our choices, Harry, that show what we truly are, far more than our abilities.

J. K. Rowling

The work described in this chapter is part of Palmese et al., 2018 “Stellar mass as a galaxy cluster mass proxy and stellar–to–halo connection in the Dark Energy Survey redMaPPer clusters”, currently in the DES collaboration review process, and the companion paper Welch, Annis, Lin, Palmese, Soares–Santos et al., 2018. The Intra–cluster light section features work from Zhang, Yanny, Palmese et al., 2018 and Gruen, Zhang, Palmese et al., 2018, both in the DES review process.

6.1 Introduction

The method presented in the previous Chapter enables studies of the whole galaxy content of redMaPPer clusters. The cluster red sequence is the main feature used to identify galaxy clusters in optical data and produce samples that are used to measure cosmological parameters (Gladders & Yee 2005; Gladders et al. 2007; Koester et al. 2007; Rozo et al. 2010; Rykoff et al. 2014, 2016a), but our understanding of the underlying physical processes leading to the formation and evolution of this feature is limited. For example, simulations of
the stellar content of galaxy cluster members hardly reproduce the colour evolution of red sequence members (see Roediger et al. 2017 and references therein). Red sequence cluster finders therefore use the red sequence as an empirically developed method. However, in order to make the most precise cosmological measurements using red sequence-selected clusters, we must investigate and quantify the impact of the red sequence assumptions in the systematic uncertainties. The membership assignment scheme that we have presented allows us to study the photometric properties of cluster members, in particular measure the red sequence slope and width.

Using the quantities derived in the previous Chapter, we can also measure the **stellar–to–halo mass relation (SHMR)**. Measuring such a relation is key to understanding the efficiency of assembling baryons into stars, which does not appear to be an efficient process: less than 10% of baryons are converted into stars (e.g. Gallazzi et al. 2008). Theoretical semi-analytical models and simulations (see Somerville & Davé 2015 for a review), make use of feedback processes from AGN and supernovae to switch star formation off and reproduce the observations, in particular at clusters scales. Therefore the efficiency with which halos convert the matter they contain into stars is a crucial ingredient in our understanding of galaxy formation and evolution, particularly the discrepancies currently existing between simulations and observations and also between different observational analyses.

Several methods have been used to observationally study the link between stellar mass and halo mass. The most important are:

- **Halo Occupation Distribution (HOD)**; Seljak 2000; Peacock & Smith 2000) models allow us to connect the observed galaxies to the underlying dark matter. The basic assumption of the HOD model is that the probability that a halo hosts a galaxy with certain properties only depends on the halo mass. Several studies using the HOD (Zu & Mandelbaum 2015, Zu & Mandelbaum 2016, Zu & Mandelbaum 2017) have extended the model to study effects such as quenching and environmental dependence with SDSS data.

- **Abundance matching** (AM) assumes that stellar masses or luminosities of galaxies are tightly correlated to the masses of dark matter halos (Wechsler et al. 1998; Colín et al. 1999; Kravtsov & Klypin 1999). The main assumption behind these methods
6.1. Introduction

is simple: the most massive galaxy lives in the most massive halo, the second most massive galaxy lives in the second most massive halo, and so on. Most recent AM prescriptions also include some scatter between the galaxy and halo abundances, and consider the presence of both halos and subhalos, each containing a galaxy (e.g. Kravtsov et al. 2004). Defining the scatter and the galaxy/halo properties to be linked, are the challenging steps when defining an abundance matching method. For example, subhalos accreted into a halo are rapidly stripped of material in their outskirts, while galaxies are stripped later on (Nagai & Kravtsov 2005). Therefore, one may want to match a property of the halo at its accretion to a galaxy property at later times (e.g. Conroy et al. 2006). AM methods can be “non–parametric”, and predict a SHMR given a stellar mass function (SMF) or luminosity function (LF), a halo mass function (HMF), and a scatter prescription between the two distributions (e.g. Kravtsov et al. 2018). Otherwise, AM can be “parametric”, in the sense that the SHMR is parametrised and constrained by the observed abundance data (e.g. Moster et al. 2010).

- Alternatively, one can measure directly the SHMR from galaxies and clusters by constraining their stellar and total mass content for each object. However, we are only able to measure the total mass of single objects through gravitational lensing using photometric surveys such as DES, and that is feasible only with galaxy clusters (except a few strong lenses cases). This direct measurement can thus only be done within clusters with DES.

The majority of previous measurements on the SHMR were mainly limited to direct measurements of stellar mass and total mass (from lensing or X-ray mass scaling relation) on a small sample of clusters and groups (in the order of ~ 1 – 100, e.g. Kravtsov et al. 2018), or to the use of HOD or abundance matching methods on large but low redshift (z ≤ 0.3) samples (such as Zu & Mandelbaum 2015), or within small fields (e.g. Coupon et al. 2015, Shan et al. 2017). In this work we extend these measurements to the huge cluster sample from DES Y1 data, spanning redshifts out to z ~ 0.7. For a comprehensive review on the galaxy-halo connection, see Wechsler & Tinker (2018).

The galaxy content of clusters can also be examined through the galaxy stellar mass function, and is used to connect galaxies with the underlying dark matter through the
methods mentioned above. Its shape and evolution provide insights into galaxy formation and evolution processes, and their connection with the galaxy environment. Extensive work has been done to constrain the SMF for galaxies with different colour, morphology and environment (Bundy et al. 2006; Baldry et al. 2008; Pozzetti et al. 2010; Vulcani et al. 2012; Mortlock et al. 2015; Weigel et al. 2016; Etherington et al. 2017; Capozzi et al. 2017). Usually the SMF and LF are well fitted by a single or double Schechter function (Schechter 1976). It is of particular interest to focus on clusters, where other than the star formation history, a number of external stresses (e.g. galaxy harassment, strangulation, merging, tidal forces) impact on the stellar mass function of the cluster members over cosmic time. Most works find that the luminosity or stellar mass function of these galaxies is consistent with a passive evolution since $z \sim 1$ (e.g. Kodama & Bower 2003; Andreon 2006), suggesting that star formation and mass assembly are accelerated in such dense environments and have been completed by $z \sim 1$. Zhang et al. (2017) find a hint for evolution of the faint end LF between $z \sim 1$ and $z \sim 0.1$, such that the low mass red sequence galaxies are more abundant than brighter ones at lower redshift, indicating different formation times. Other works find similar results (e.g. De Lucia et al. 2007; Lin et al. 2017). However, there is no consensus yet on the LF evolution, especially given the different methods and samples used, and the difficulties in detecting and measuring photometry of faint galaxies in crowded environments. Additional measurements of SMF over wide redshift ranges may help in further understanding the discrepancies.

An important ingredient of stellar mass measurements in clusters is also the so-called **Intra–cluster light (ICL)**. The central galaxy of clusters tends to be surrounded by an extended light envelope (Zwicky 1951, 1952; Matthews et al. 1964; Morgan & Lesh 1965). Studies indicate that this light envelope extends to hundreds of kpcs and sometimes encloses several galaxies, especially if the cluster is experiencing a merging process (see reviews in Mihos 2004; Lauer et al. 2014). Given its diffuse nature and the fact that it may enclose multiple galaxies, it seems more reasonable to consider this envelope as a component of galaxy clusters rather than as a part of single galaxies. This diffuse light envelope is thus frequently referred to as ICL. Despite the difference between central galaxy and ICL, they are almost impossible to observationally distinguish because the outskirts of centrals naturally blend into ICL. Outside the outskirts of centrals, the ICL is extremely faint, which poses significant challenges for separating it from centrals, and
for further characterising its distribution and properties. Studying the statistical distribution of ICL in an ensemble of clusters is one approach toward easing systematic effects from ground based observations. An approach towards this direction, called “stacking”, consists in combining the images of several galaxy clusters by aligning the centres of the clusters and measuring ICL in the combined image. This method is used in Zhang et al. (2018) to detect ICL in DES clusters and its results are used to study the properties of ICL and its plausible formation scenarios. It is likely that ICL forms through multiple channels, but the relative contributions are still being explored. Depending on the formation mechanism, simulated ICL exhibits different colour and spatial distributions, and the total amount of ICL stellar mass varies, which provides clues for testing ICL formation hypotheses with observations.

In this Chapter we present measurements of the red sequence, SHMR and stellar mass functions in clusters out to \( z \sim 0.7 \) from \( \sim 1,839 \text{deg}^2 \) of the sky taken during the first year of DES observations, and study some ICL properties. This Chapter is divided into eight sections. In Section 6.2 we present cluster properties that naturally come out of our membership probability scheme, in particular for the red sequence galaxies. Section 6.3 contains measurements of the SHMR for centrals, satellites and total galaxy population. In Section 6.4 we present measurements of the stellar mass function for centrals and for all galaxies in clusters, while in Section 6.5 we study the mass growth of the centrals over redshift and discuss the identification of those and Brightest Cluster Galaxies (BCGs) from our sample. Section 6.6 is dedicated to the effect of the galaxy Initial Mass Function (IMF) on the SHMR and SMF. In Section 6.7 we study measurements of the intra–cluster light in terms of its colour and stellar mass. Section 6.8 contains discussion and conclusions.

### 6.2 Photometric properties of clusters

In the previous Chapter, we have introduced the membership probabilities method used. In particular, the colour probabilities allow measurements of the red sequence properties. A quantity of interest is the red sequence slope in colour–magnitude space, which we measure by performing a weighted linear fit of observed \( r \) versus \( g - r \), \( i \) versus \( r - i \) and \( z \) versus \( i - z \). The weights in the three cases are given by the membership probability multiplied by the red sequence probability defined in Eq. (5.10), as computed from the
Figure 6.1: Colour–magnitude diagram for a cluster at $z = 0.14$ from the Y1 redMaPPer sample, given as an example (same as Figure 5.4). The red points are weighted by $p_{\text{mem}} \times p_{\text{red}}$, and the blue points by $p_{\text{mem}} \times p_{\text{blue}}$ (where $p_{\text{blue}}$ is defined similarly to the red sequence membership in Eq. (5.10)). The red line is the best fit to the red points from the GMM method.

colours $g - r$, $r - i$ and $i - z$ respectively. An example of this fit is shown in Figure 6.1 for the $g - r$ colour.

Other quantities of interest in cluster studies are the mean colour and the scatter around it of the red sequence galaxies. These are measured by our GMM fit as the mean and the width of the Gaussian distribution associated with the red sequence. The observed scatter $\sigma_{\text{obs}}$ will be given by the contribution of the intrinsic scatter in colour of the galaxies in the cluster and of the photometric error in the colour $\sigma_{\text{phot}}$. Assuming these two errors are independent, they can be summed in quadrature, and the intrinsic scatter we are interested in is given by:

$$\sigma_{\text{int}} = \sqrt{\sigma_{\text{obs}}^2 - \sigma_{\text{phot}}^2}. \quad (6.1)$$

The typical photometric error for each cluster can be measured as the mean measured colour error from its members. We consider only members with $p_{\text{mem}} > 20\%$ to avoid including a high number of interlopers. In Figure 6.2 we show red sequence mean colour $\mu_{\text{red}}$, intrinsic scatter $\sigma_{\text{red}}$ and slope $m_{\text{red}}$ from the three considered colours as a function of redshift. These results can be compared to the results from Rykoff et al. (2014) in $g - r$ for SDSS clusters. This comparison only consists in a qualitative check for our
6.2. Photometric properties of clusters

Figure 6.2: Red sequence mean colour $\mu_{\text{red}}$, intrinsic scatter $\sigma_{\text{red}}$ and slope $m_{\text{red}}$ as a function of redshift for $\sim 80,000$ clusters from the DES Y1 redMaPPer cosmology sample (purple density plot). Each cluster has tens to hundreds of members. The magenta lines are the estimates from redMaPPer using SDSS data (from Rykoff et al. 2014), which are only volume limited out to $z \sim 0.35$. These are shown for a qualitative comparison.

Method, and is only valid out to $z = 0.35$, which is the redshift out to which their sample is volume limited. The mean colours tend to become redder at higher redshifts, as expected for observed colours. The intrinsic scatter increases, while also becoming a noisier measurements due to the fact that the photometric errors become more substantial, in particular in $g - r$, as most of these red sequence galaxies are very faint in $g$–band.

The fact that the intrinsic width of the red sequence increases with redshift, shows that red sequence–based cluster finders may face more difficulties in identifying clusters at higher $z$, and that including the blue cloud into mass proxies may be useful. The slope is negative and quite shallow, as seen in previous studies (e.g. Mei et al. 2009, Rykoff et al. 2014). On–going work is focused on measuring the mentioned quantities, along with the blue fraction, from rest–frame galaxy colours. These measurements will allow physical interpretations of the evolution of the studied properties, which is not possible with the observed colours only. The results shown in Figure 6.2 for the observed colours
still provide a solid consistency check for our membership probability assignment scheme.

6.3 Stellar-to-halo mass

While the weak lensing calibration of the mass scaling relation for $\mu_*$ is carried out in a companion paper for SDSS clusters (Pereira et al. 2018), here we use an independent mass estimate through the richness-mass relation which has been extensively studied for redMaPPer clusters in Melchior et al. (2016). This allows us to transform the redMaPPer richness $\lambda$ into a halo mass $M_{200m}$ for all the Y1 redMaPPer clusters and estimate the stellar–to–halo–mass relation for DES clusters.

For the full Y1 redMaPPer sample we focus on a statistical measurement of the stellar to halo mass relation. This means that while binning our sample in halo mass and redshift, we assume that the intrinsic scatter of stellar mass around a certain halo mass would reduce to a stochastic scatter around the mean SHMR value. The validity of this assumption has already been pointed in other works (Zu & Mandelbaum 2015; Guo et al. 2014). We therefore choose a method that allows us to fit an intrinsic scatter and to take into account errors on stellar mass, halo mass and redshifts.

We fit the SHMR with a linear model in $\log(M_*/\tilde{M}_*)$, $\log(M_{200c}/\tilde{M}_{200c})$, $\log(1+z)/(1+\bar{z})$ in the form:

$$\log\left(\frac{M_*}{\tilde{M}_*}\right) = \alpha \log\left(\frac{M_{200c}}{\tilde{M}_{200c}}\right) + \beta \log \left(\frac{1+z}{1+\bar{z}}\right) + \gamma ,$$

where $\tilde{M}_*$, $\log(\tilde{M}_{200c}) = 13.79$ and $\bar{z} = 0.46$ are the median values of the full sample. $\tilde{M}_*$ is changed from case to case. This empirical relation is a fair assumption at cluster scales, as also motivated by simulations, and it is often used in the literature (Brough et al. 2008; Moster et al. 2010; Pillepich et al. 2017). We add a Gaussian scatter $\sigma_0$ on $\log(M_*/\tilde{M}_*)$ independent of halo mass, which enters in our analysis as an additional term to the covariance matrices of the data. We further assume that the measurements of the data $D_i$ for each cluster $i$, namely $M_{*,i}$, $M_{200c,i}$ and $z_i$, are independent, and that the errors on the data are Gaussian. Under these assumptions, we calculate the posterior distribution of the parameters $\alpha$, $\beta$, $\gamma$, $\sigma_0$ in Eq. (6.2) given the data $D$ for each cluster.
\[ p(\alpha, \beta, \gamma, \sigma_0|D) = \prod_i p(\alpha, \beta, \gamma, \sigma_0|D_i) \]
\[ \propto \prod_i \iiint dx_i \ dy_i \ dz'_i \ p(\alpha, \beta, \gamma, \sigma_0, x_i, y_i, z'_i|D_i) \]
\[ \propto \prod_i \iiint dx_i \ dy_i \ dz'_i \ p(\alpha, \beta, \gamma, \sigma_0, x_i, y_i, z'_i) \times p(D_i|\alpha, \beta, \gamma, \sigma_0, x_i, y_i, z'_i), \quad (6.3) \]

where \( x_i \equiv \log \left( \frac{M_{\ast,i}}{M_r} \right) \), \( y_i \equiv \log \left( \frac{M_{\text{200c},i}}{M_{\text{200c}}} \right) \), \( z'_i \equiv \log \left( \frac{1+z}{1+z_0} \right) \) and we have applied Bayes’ theorem. Going forward:

\[ p(\alpha, \beta, \gamma, \sigma_0|D) \propto \prod_i \iiint dx_i \ dy_i \ dz'_i \ p(x_i|\alpha, \beta, \gamma, \sigma_0, y_i, z'_i) p(\alpha, \beta, \gamma, \sigma_0, y_i, z'_i) \]
\[ \times p(D_i|\alpha, \beta, \gamma, \sigma_0, x_i, y_i, z'_i), \quad (6.4) \]

where the first term is a 1D Gaussians \( \mathcal{N}^{1D}(\mu; \sigma^2) \) of mean \( \mu = x_i - \alpha y_i - \beta z'_i - \gamma \) and variance \( \sigma^2_0 \), and the last component is the likelihood of each cluster \( i \), a 3D Gaussian in this case:

\[ p(\alpha, \beta, \gamma, \sigma_0|D) \propto \prod_i p(\alpha, \beta, \gamma, \sigma_0) \iiint dx_i \ dy_i \ dz'_i \ N^{1D}(x_i - \alpha y_i - \beta z'_i - \gamma; \sigma^2_0) \]
\[ \times \mathcal{N}^{3D}([x_i - \bar{x}_i; y_i - \bar{y}_i; z'_i - \bar{z}'_i]; \Lambda) \]
\[ \times p(\alpha, \beta, \gamma, \sigma_0) \prod_i N^{1D}(\bar{x}_i - \alpha \bar{y}_i - \beta \bar{z}'_i - \gamma; \sigma^2_0 + \Lambda_x + \alpha^2 \Lambda_y + \beta^2 \Lambda_z), \quad (6.5) \]

where \( \Lambda \) is the covariance matrix of the \( i \)-th cluster, which is diagonal under our assumptions. We assume uniform truncated priors in \( p(\alpha, \beta, \gamma, \sigma_0) \) for all of the four fitting parameters, in particular \( 0 < \alpha < 2, -2 < \beta < 2, -10 < \gamma < 10 \) and \( 0 < \sigma_0 < 1 \).

### 6.3.1 Central stellar mass to halo mass

We select as the central the galaxy with highest \( P_{\text{cen}} \) centering probability from the redMaPPer catalog, and consider as satellites all of the remaining galaxies. We fit the stellar mass of centrals, \( M_{\ast,\text{cen}} \), as a function of \( M_{\text{200c}} \) and estimate the parameters in Eq. (6.2) and (6.5). The results are presented in Table 6.1 (where we report the median of the posterior distribution and 68% confidence level uncertainties) and Figure 6.3. The scatter
Figure 6.3: Top: Stellar–to–halo mass relation for central galaxies (left panel), and posterior distributions of the parameters in Eq. (6.2) (right panel). Bottom: Total stellar–to–halo mass relation (left panel), and posterior distributions of the parameters in Eq. (6.2) (right panel). The data points represent the mean stellar mass values and the standard error of the mean of the distribution in halo mass bins. Binned data are only shown to guide the eye, and have not been used in the analyses. The black lines are 100 random samples from our $\alpha$ and $\beta$ posterior distributions, and the light shaded broad region represents our scatter. The lines from the literature represent their best fit. The shaded region around the Kravtsov et al. (2018) best fit is their $1\sigma$ uncertainty on slope and intercept. The shaded region around the IllustrisTNG best fit is the Pillepich et al. (2017) scatter estimate for 32 kpc apertures around galaxies. All the data and fits presented assume a Chabrier IMF.
at fixed halo mass is substantial (\(\sim 0.3\) in logarithmic scale) but a trend with halo mass is clearly found, with a slope of \(\alpha = 0.4052 \pm 0.0048\). In Figure 6.3 we show the results for redMaPPer clusters in the red density plot, while the black solid lines are 100 random samples from the \(\alpha\) and \(\beta\) posterior distributions obtained with the Bayesian linear regression on that data. For visualisation purposes, we plot mean stellar mass values in halo mass bins in three redshift bins \((z < 0.25, 0.25 < z < 0.4, 0.4 < z < 0.7)\). These results are compared to others from the literature that use a range of different methods. For a more consistent comparison, we show results that assume a Chabrier IMF. Kravtsov et al. (2018) use SDSS photometry and X-ray data for single clusters at \(z < 0.1\) and compare with abundance matching predictions, while Zu & Mandelbaum (2015) and Coupon et al. (2015) implement HOD methods on SDSS and CFHTLS data respectively. Zhang et al. (2016) present a study of BCGs from DES Science Verification data for X-ray selected clusters, and we show their results for 32 kpc apertures around the BCG at the mean redshift of our sample \(z = 0.45\). Pillepich et al. (2017) use the latest Illustris simulations to measure the stellar mass content of groups and clusters.

Kravtsov et al. (2018) perform a detailed analysis to derive extended luminosity profiles around BCGs, and fit those with multiple Sérsic profiles. The model profile is then extrapolated to infinity to derive total magnitudes. They find that \textsc{cmode}l magnitudes computed with the standard SDSS pipeline underestimate the total BCG luminosity by a factor \(\sim 2 - 4\). The MOF magnitudes used in this work are computed similarly to the SDSS \textsc{cmode}l magnitudes: a composite model made of a bulge plus a disk component is fit to the profile and extrapolated to infinity. In order to compare our results to Kravtsov et al. (2018) we downweight their best fit by 0.45 dex in stellar mass. This is their SHMR estimate presented in Figure 6.3, which is consistent with our result at all halo masses, but with a slightly shallower slope. They find a slope of \(0.39 \pm 0.17\) and \(0.33 \pm 0.11\) when they include the clusters from Gonzalez et al. (2013) (and this is the result we show), which is within \(1\sigma\) from our best–fit. The de–corrected normalisation is consistent with ours, although they focus on clusters at \(z < 0.1\) and our data points from the lowest redshift bin are \(\sim 0.1\) dex below the rest of the cluster sample. This discrepancy is comparable to the uncertainty on stellar masses and could be due to the difference in the photometry and the qualitative correction we have applied.

The analysis from Zu & Mandelbaum (2015) is also valid at low redshifts \((z < 0.3)\) and it looks qualitatively in agreement with our lowest redshift bins measurements. The
slope from Zhang et al. (2018) of 0.37 ± 0.10 is within 1σ of what we find, while the normalisation depends on the aperture chosen and a comparison is not straightforward: we use magnitudes from MOF, that are not computed within a fixed aperture but vary from object to object.

The Coupon et al. (2015) estimate has the shallowest slope of all the results discussed here, which makes their results deviate from ours at higher halo masses. Their redshift range is overlapping with ours from \( z > 0.5 \), but going up to \( z \sim 1 \) with a mean around 0.8. It is possible that galaxy evolution affects the stellar mass of galaxies at redshifts that we are considering in this work, but the weak redshift evolution that we observe seems to go towards higher values of stellar mass at higher \( z \). We argue that the difference in normalisation may be due to the different framework used to estimate the stellar masses. In particular, they utilise a wider range of galaxy dust models, which they may constrain better thanks to the \( K_s \) band information. Also, they do not consider models with supersolar metallicity, which may be relevant when fitting BCGs and luminous red galaxies in clusters.

Results from the latest IllustrisTNG simulations (Pillepich et al. 2017) deviate from our result and other observational data at high halo mass. In Figure 6.3 we plot their best fit SHMR for centrals when the stellar mass is computed within a 30 kpc aperture. They de-correct Kravtsov et al. (2018) result to match that aperture and find their best fit to be higher than Kravtsov et al. (2018). They find that the SHMR is very sensitive to the change of aperture considered, which could also explain our disagreement. In particular, for brighter (and thus greater stellar mass) objects we may be systematically underestimating the total luminosity of the central galaxy (as also pointed in Kravtsov et al. 2018), as we are only considering a model that fits well to the inner luminosity profile, and not the extended stellar halo. Also, in brighter environments, there is a chance that the subtracted background is overestimated. This would explain our shallower slope in the SHMR. On the other hand, we find a high scatter (\( \sim 0.3 \) dex) in stellar mass that still makes our results consistent at the high mass end.

Our scatter is larger than typically found in other works (0.22 dex in Zu & Mandelbaum 2015 and Coupon et al. 2015, 0.17 dex in Kravtsov et al. 2018). Uncertainties on the photometry, stellar masses, total masses and so on can well affect the value of the intrinsic scatter. Given the differences between the methods and samples adopted, we believe that it is reasonable to find different values. However, our sample spans a wider combination
6.3. Stellar-to-halo mass

Figure 6.4: Stellar mass of the central over the total stellar mass for the Y1 redMaPPer clusters (red density plot). The data points represent the median stellar mass fraction values at different halo masses and the errorbars indicate the standard error of the mean of the fraction distribution in each halo mass bin. The central contributes roughly 40-20% of the total stellar mass. The line is from Pillepich et al. (2017) results at $z = 0$ and with 30 kpc apertures.

of area and redshift range than other works, making contributions to the intrinsic scatter from sample variance and galaxy or cluster evolution more substantial. Amongst the works discussed in this section, the analysis from Kravtsov et al. (2018) is the closest to ours. They consider a much smaller ($\sim$ tens of clusters) sample of clusters over a redshift range $z < 0.1$, thus it is not surprising that our scatter is $\sim 0.12$ dex larger than theirs.

The redshift dependence of the SHMR seen in the $\beta$ parameter is positive, and this can be understood in light of the results presented in Section 6.5.1.

6.3.2 Total stellar to halo mass

Satellite galaxies become a significant contribution to the stellar content of the halo at higher halo masses. In fact, the total mass of clusters can be accounted for by the contribution of the satellite sub-halos, while the central halo contribution decreases. This can be seen in terms of stellar mass in Figure 6.4. The central contributes roughly 40-20% of the total stellar mass at all halo masses, decreasing with halo mass. We do not find any significant redshift dependence of this behaviour, but we recover a significant scatter at lower masses (as also found in Pillepich et al. 2017, where it is $\lesssim 0.2$ dex below
Table 6.1: Fits of the SHMR from Eq. (6.2) for centrals and all galaxies. Values represent the median of the parameters posterior distribution, and the errors are at 68% confidence level. Redshift and halo mass pivot values are respectively $z = 0.46$ and $\log(M_{200}^c) = 13.79$.

<table>
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<th>Subject</th>
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<td></td>
</tr>
<tr>
<td>$\log(M^\sigma)$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
6.3. **Stellar-to-halo mass**

Figure 6.5: Stellar mass fraction (total stellar mass of each cluster over its halo mass) as a function of halo mass. The data points represent the mean stellar mass fraction values at different halo masses and the error bars indicate the standard error of the mean. The dashed line is the prediction of Kravtsov et al. (2018) using abundance matching with scatter in the SHMR and a Chabrier IMF. The stellar masses have been corrected to galaxies within $R_{200c}$ only for the comparison.

$$\log(M_{200c}/M_\odot) \sim 14$$.

Fit results for the total SHMR with the power law presented in Eq. (6.2) are listed in Table 6.1 and shown in Figure 6.3. Our errors on the power law parameters are very small, in the order of $\sim 0.5 - 7\%$, because of the large number statistics used. We find that the total SHMR follows a steeper and less scattered power law than centrals only, as also found in previous works (e.g. Pillepich et al. 2017). The slope is significantly steeper than what is found in other observational works, such as Andreon (2012) $0.37 \pm 0.07$, and Kravtsov et al. (2018) $0.59 \pm 0.08$, while the central SHMR slope is still consistent with Kravtsov et al. (2018) within $1\sigma$. One reason for the discrepancy is that they consider a fixed $M_*/L$ ratio to compute the stellar masses of all galaxies. Secondly, we have a deeper dataset and MOF photometry that performs well in crowded environments such as clusters, and membership probabilities that take into account the galaxy properties. These factors will change the contribution that the satellite galaxies give to the total stellar mass of clusters. Our result is closer to what is found in the latest IllustrisTNG simulations: 0.84 when including centrals, intra-cluster light (ICL) and satellites, reaching 1.14 for satellites only. This value is also less than $1\sigma$ away from our result. The inclusion of centrals is what lowers the slope, an effect which is mitigated in our case by the inclusion of membership
Chapter 6. Cluster evolution results from DES Year 1 redMaPPer clusters

probabilities, given that we do not have a truth table of members. In fact, centrals will also have $p_{\text{mem}} < 1$ by construction.

Our analysis shows that the total SHMR has a weaker dependence on redshift than for centrals, with the value of $\beta$ being closer to 0. However the inversion in sign of $\beta$ is due to the probabilities that are used to weight the stellar masses, and this is an unavoidable effect due to our survey specifics. In fact, the stellar mass of the redshift bin containing galaxies around $z \sim 0.4$ is larger than the others. The number density of DES galaxies shows in fact a peak around that redshift: more galaxies are assigned to a similar photo-$z$ there compared to other redshifts, and therefore they will have a larger contribution from the $p_z$ component in the membership probabilities. At the same time more constraining power will come from the higher redshifts with lower stellar masses, because there are more clusters there in our volume limited sample. We therefore believe that the observed redshift dependence of the total SHMR is mostly due to the photometric redshifts rather than to any physical evolution.

The amount of scatter in stellar mass at fixed halo mass is also an important ingredient for halo or sub-halo abundance matching (AM) methods, and Kravtsov et al. (2018) showed how the scatter can impact the SHMR measurements. Our $1\sigma$ scatter in the logarithmic stellar mass at fixed halo mass is $0.2492 \pm 0.0010$. For AM a scatter of $\sim 0.1 - 0.3$ is usually assumed. The intrinsic scatter found in the other works discussed here (e.g. Pillepich et al. 2017, Leauthaud et al. 2012b and Kravtsov et al. 2018) is usually $0.1 - 0.25$ dex. As discussed for the centrals, we believe that the difference in scatter is due to the different samples and methods used. We note that our result is consistent with the analysis by Leauthaud et al. 2012b ($\sim 0.2 - 0.25$ dex over $0 < z < 1$), who performed a joint analysis of galaxy–galaxy weak lensing, galaxy spatial clustering, and galaxy number densities with COSMOS data. We refer to future work to introduce a redshift and halo mass dependent intrinsic scatter.

We find a scatter in halo mass at fixed stellar mass of $\sigma_{\log(M_{200c})|M_*} \sim 0.17$. Our result is similar to what Andreon (2012) finds for the scatter at fixed stellar mass (0.21-0.32 dex). This value can also be compared to what we find in the halo mass–$\mu_*$ from the X-ray temperature calibration, $\sim 0.18$, and they are very close despite the fact that they have been derived very differently. However, to truly compare the scatter on a physical level, one would need to understand the correlation between the parameters and the selection effects introduced by the X-ray selection. Even though the X-ray measurements are done
at the redMaPPer cluster positions, a cut in the temperature SNR is essential to avoid taking into account spurious detections. This selection introduces a redshift and mass dependent cut on the sample (a Malmquist bias).

We find that the total stellar mass fraction $f_\star = M_{\star}^{\text{tot}} / M_{200c}$ is $\sim 0.011$, and it is flat over the range of halo masses studied. This value is comparable to the stellar mass fraction found in Chapter 4 and to the already mentioned results by Bahcall & Kulier (2014). Our results are shown in Figure 6.5, where we normalise by the baryon-to-matter mass ratio from cosmological constraints $\Omega_b/\Omega_m \simeq 0.16$ (Planck Collaboration et al. 2016b) for a better understanding of the fraction of baryons locked into stars: roughly 7% of cluster baryons are transformed into stars. The stellar masses have been corrected to galaxies within $R_{200c}$ for the comparison, as our analysis brings the total stellar mass of clusters out to 3 Mpc (although contributions outside $\sim 1.5$ Mpc are negligible because of the radial membership probabilities), which is roughly 30% higher than the mass within 1 Mpc. The radial probability gives most of the weight to the galaxies within $R_{200c}$, and extensive studies have been performed on mock data so that $\Sigma_{p_{\text{mem}}} \sim N_{\text{members}}$. We therefore believe that our total stellar mass is a good estimator of the whole cluster stellar mass besides the ICL.

Despite some possible difference in the stellar mass measurements that could be due to the mass-to-light ratio assumed, of the different cluster selection, our results confirm what is found in Kravtsov et al. (2018): the suppression of star formation efficiency at larger halo masses is not as strong as previously expected (e.g. Behroozi et al. 2013), and that is due to the contribution of satellites that makes this efficiency a milder function of halo mass compared to centrals alone. Also Pillepich et al. (2017) find that the $f_\star$ dependence on halo mass is shallower at the high mass end, dropping only by a factor of $\sim 2$ with respect to Milky Way halo masses. Coupon et al. (2015) find that the total stellar mass fraction is close to flat at cluster scales, slightly increasing at the high mass end. A roughly flat stellar mass fraction at cluster masses is also explained in Leauthaud et al. (2012b), who find once again results close to ours. They claim that flatness is due to galaxy merging in the absence of significant star formation. Above the peak in $f_\star$ at Milky Way halo masses, halos can only grow because of merging with halos of lower stellar mass fraction, therefore lowering the total $f_\star$. Towards higher halo masses, this means that the stellar mass fraction will be enhanced by the mergers, inverting the trend again. This behaviour will repeat towards increasing halo masses, causing the flattering.
As for the total SHMR, we do not find evidence of redshift evolution in the stellar mass fraction. Chiu et al. (2016) and Chiu et al. (2017) also find that the stellar mass fraction in X-ray and SZ selected clusters depends only weakly on redshift, implying that the stellar content at a given halo mass changes very little since $z \sim 0.7$. Similar results are found in simulations, as in Pillepich et al. (2017): the overall cluster stellar mass build-up happens at a similar pace as the dark matter halo assembly, resulting in very little change from redshift 1. Chiu et al. (2017) also point out that in the hierarchical formation scenario, this means that at these redshifts the halos mainly accrete from structures outside the virialised halo that have a stellar mass fraction close to the cosmic mean.

Previous works found no or little dependence (Vulcani et al. 2013; Etherington et al. 2017) of the faint end galaxy stellar mass function on environment. We choose to employ the SMF from Capozzi et al. (2017), that was estimated for the whole DES SV COM-MODORE galaxy catalog. They use a double Schechter function (Schechter 1976) the lowest redshift bin ($z < 0.2$), and a single Schechter function in the higher bins. By integrating the GSMF best fits, we find that our total stellar mass would be $23 - 24\%$ higher if we were to include all galaxies below the $10^{10} \, M_\odot$ limit chosen, although this would have to be weighted by the membership probabilities for consistency.

In Zhang et al. (2018) we find that the central plus ICL contribution in low redshift ($0.2 < z < 0.3$) Y1 redMaPPer clusters is $\sim 40\%$ of the total stellar mass computed as in this work, meaning that the ICL contribution to the total stellar mass can be up to $\sim 30\%$, bringing the stellar mass fraction up by a factor up to 1.3. Note that this factor would include also the contribution coming from undetected members, so it would at least partially take into account the low mass end of the SMF mentioned in the previous paragraph.

### 6.4 Stellar mass functions

#### 6.4.1 Central stellar mass function

Several works (e.g. Lauer et al. 2014) find that the luminosity function of BCGs follows a log-normal distribution. Given that we expect a similar $M_*/L$ for these galaxies, it is reasonable to expect that also the SMF of centrals follows a similar behaviour, as also found in Yang et al. (2009) for SDSS galaxy groups. In order to compute the SMF, we divide the stellar mass distribution by the comoving volume over the Year 1 footprint and
6.4. Stellar mass functions

Centrals

<table>
<thead>
<tr>
<th>IMF</th>
<th>( \langle z \rangle \sim 0.2 )</th>
<th>( \langle z \rangle \sim 0.4 )</th>
<th>( \langle z \rangle \sim 0.6 )</th>
<th>Whole</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chabrier</td>
<td>( (5.791 \pm 0.098) \times 10^{-4} )</td>
<td>( (4.876 \pm 0.083) \times 10^{-4} )</td>
<td>( (3.042 \pm 0.038) \times 10^{-4} )</td>
<td>( (4.828 \pm 0.037) \times 10^{-4} )</td>
</tr>
<tr>
<td>Salpeter</td>
<td>( (8.67 \pm 0.016) \times 10^{-4} )</td>
<td>( (7.33 \pm 0.10) \times 10^{-4} )</td>
<td>( (4.54 \pm 0.69) \times 10^{-4} )</td>
<td>( (7.249 \pm 0.074) \times 10^{-4} )</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>IMF</th>
<th>( \phi^* ) [Mpc(^{-3})]</th>
<th>( \log M^* )</th>
<th>( \alpha )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chabrier</td>
<td>( (1.68 \pm 0.16) \times 10^{-4} )</td>
<td>11.510 \pm 0.026</td>
<td>-1.267 \pm 0.0038</td>
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<td>( (1.841 \pm 0.088) \times 10^{-4} )</td>
<td>11.460 \pm 0.013</td>
<td>-1.185 \pm 0.022</td>
</tr>
<tr>
<td></td>
<td>( (1.228 \pm 0.083) \times 10^{-4} )</td>
<td>11.395 \pm 0.019</td>
<td>-1.108 \pm 0.034</td>
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<td>Whole</td>
<td>( (2.02 \pm 0.11) \times 10^{-4} )</td>
<td>11.401 \pm 0.019</td>
<td>-1.119 \pm 0.025</td>
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<tr>
<td>Salpeter</td>
<td>( (2.099 \pm 0.036) \times 10^{-4} )</td>
<td>11.713 \pm 0.057</td>
<td>-1.1845 \pm 0.0066</td>
</tr>
<tr>
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<td>( (2.28 \pm 0.15) \times 10^{-4} )</td>
<td>11.659 \pm 0.022</td>
<td>-1.074 \pm 0.028</td>
</tr>
<tr>
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<td>( (1.57 \pm 0.16) \times 10^{-4} )</td>
<td>11.574 \pm 0.035</td>
<td>-0.955 \pm 0.051</td>
</tr>
<tr>
<td>Whole</td>
<td>( (2.47 \pm 0.20) \times 10^{-4} )</td>
<td>11.593 \pm 0.032</td>
<td>-1.010 \pm 0.035</td>
</tr>
</tbody>
</table>

Table 6.2: Best–fit results of the SMF for centrals and all galaxies in the clusters in redshift bins and for the whole redMaPPer catalog. The redshifts reported are the mean values. The parameters are presented in Eq. (6.6) and Eq.(6.7). Fits are performed over the stellar mass range (\( \log(M_{\text{cen}}/M_\odot) \)) between 10.5 (10.3) and 12.5 for the centrals (total) SMF. These values are 0.2 dex higher for the Salpeter IMF case.

by the bin width in stellar mass (0.15 dex). We estimate errors by making 200 bootstrap resamplings. Given the huge size of the cluster sample used, these errors are 2-3 orders of magnitude smaller than the SMF values. In Figure 6.6 we show our results from a least–\( \chi^2 \) fit in redshift bins for a log–normal function in the form:

\[
\phi_{\text{cen}}(M) = \frac{A}{\sqrt{2\pi}\sigma_c} \exp \left[ -\frac{(\log M - \log M_{\text{cen}})^2}{2\sigma_c^2} \right],
\]

where \( \log M_{\text{cen}} \) is by definition the expectation value for the logarithm of the stellar mass of centrals and \( \sigma_c = \sigma(\log M_c) \). The SMF for the whole redshift range has been computed by dividing by the “effective” comoving volume of the redMaPPer catalog: it takes into account the masking and depth variations over the footprint. The best–fit parameters for the two redshift bins and the whole sample are presented in Table 6.2. We also find that the mass function has a similar behavior when binning in halo mass [i.e. the conditional
luminosity function $\phi_{\text{cen}}(M_\star|M_{200c})$.

In order to estimate the systematic contribution to the SMF from the photometry and stellar model selection, we assume the errors on the stellar masses to be Gaussian and randomly draw 200 “noisy” stellar mass values $M_\star^{\text{noise}}$ for each galaxy. The Gaussian width is given by the error estimate from the BMA code, as this will reflect the stellar population model uncertainty, as well as the photometry errors. The 16th and 84th percentiles of the SMF from such resampling are shown in the grey region in Figure 6.6. As we could have expected, this resampling has the effect of broadening the distribution (shown by the black points) because the uncertainty on the stellar masses has the effect of scattering the galaxies within different bins. This effect is known as the Eddington bias. Given that we assume the resampled stellar mass distribution to be a Gaussian in the logarithm of the stellar mass (as done also in Caputi et al. 2011) convolved with the SMF which is also Gaussian, the result is that the measured SMF has the Gaussian widths added in quadrature. The width of the $\log(M_\star^i) - \log(M_\star^{\text{noise}})$ distribution is 0.05 and we consider this effect as a systematic error from the photometry on the width $\sigma_c$.

The systematic error on $M_\star,c$ is driven by the IMF choice (see Section 6.6). The results are reported in Table 6.2. The reduced $\chi^2$ are high because of the contribution coming from the low mass end ($\log M_\star \lesssim 10.8$): the SMF is not log-normal there. Assuming the abundance matching theory, where the central stellar mass function at fixed halo mass has a log-normal scatter in $M_\star$, then the convolution of those distributions would be Gaussian in $\log M_\star$ over the clusters halo mass range. We tested this using the Buzzard simulations (DeRose et al. 2018; Wechsler et al. 2018) made for DES Year 1 data: when the true centrals for halo masses $M_{200c} > 10^{13} M_\odot h^{-1}$ are selected, no deviation from Gaussianity is seen in the luminosity function (LF) in absolute magnitude space (see Figure 6.7). On the contrary, when redMaPPPer centrals are selected from the same simulation, the luminosity function deviates from a Gaussian at the faint end. Assuming that the mass–to–light ratio does not vary significantly for these galaxies,\(^1\) we believe that both the SMF and the LF faint ends are affected by the redMaPPPer centering. In fact, the distribution of centering probability $P_{\text{cen}}$ shifts towards lower values at those lower luminosities.

Yang et al. (2009) explored the conditional stellar mass function $\phi_{\text{cen}}(M_\star|M_{200c})$ in bins\(^1\)

\(^1\)This is a reasonable choice over the redshift range explored here. Centrals may accrete some mass from other early type galaxies or satellite dwarfs since redshift 1, as we see in this Chapter, but the bulk of their in-situ star formation has ended by then, and they not expected to significantly change their mass-to-light ratio. In addition, centrals selected by redMaPPPer are by construction tightly connected to the red sequence.
6.4. Stellar mass functions

Figure 6.6: Stellar mass function of central galaxies in redshift bins. Errorbars come from 200 bootstrap samples of stellar mass values for each galaxy. The dashed lines represent the best fits of these data and errors with a log–normal function. The grey region represents the 16th and 84th percentiles of the SMF from the resampling of the stellar masses to include SSP and photometric uncertainties. The red shaded region shows the part excluded in the fit.

of halo masses for SDSS groups and clusters. They find that the width of the log–normal distribution is $\sigma_c \sim 0.17$ in all mass bins, while the mean increases by $\sim 0.25$ dex between halo masses of $10^{13.5} M_\odot$ and $10^{15} M_\odot$, which is similar to what we find in the SHMR for centrals in Section 6.3. Our width is larger than theirs as one could expect, given that we consider all halo masses in that range. Their mean values ($\log M_{*c} \sim 11.1 - 11.4$) are systematically lower than what we find, even in the lowest redshift bin that should contain a similar cluster population. We believe this may be due to SDSS luminosities being often underestimated for bright galaxies. Furthermore, there are differences in the stellar mass computation which may introduce systematic biases, such as the IMF assumption (they use a Kroupa IMF) and the fact that a single the mass-to-light ratio is used for all galaxies. However, the $\sim 0.2$ dex difference observed between the results is compatible with a conservative error on stellar mass estimation.

6.4.2 Total stellar mass function

The stellar mass function for all galaxies in the clusters is computed from the stellar mass distribution of the galaxies in our members catalog, with their entries being weighed
Chapter 6. Cluster evolution results from DES Year 1 redMaPPer clusters

Figure 6.7: Luminosity function of central galaxies from Buzzard simulations. The light blue data points come from the catalog of true centrals, while the orange data points represent the centrals from the redMaPPer algorithm run on the simulated data. The deviation from Gaussianity for the redMaPPer distribution is seen at the faint end. The normalisation is arbitrary.

Figure 6.8: Stellar mass function of all cluster galaxies in redshift bins. Errorbars represent the Poisson noise and the systematic error from a resampling of the stellar masses added in quadrature. The dashed lines represent the best fits of these data and errors with a single Schechter function. The red shaded region shows the part excluded in the fit. The best fit from Vulcani et al. (2013) shown are from a sample of ESO Distant Cluster Survey clusters at $0.4 < z < 0.8$ for all galaxy morphological types. The dotted line is the best fit from Weigel et al. (2016) for SDSS clusters with halo masses $13.5 < \log M_h < 15$. Both distributions have been arbitrarily renormalised to match our results at $\log M_* = 11$ at the relevant redshifts for a visual comparison of the shape of the functions.
by their membership probability. The comoving volume is computed as in the previous section for different redshift bins, and we divide the distribution by the stellar mass bin width. A Schechter function of the form:

$$\phi(M) = \phi^* e^{-M/M^*} \left( \frac{M}{M^*} \right)^{\alpha},$$

(6.7)
is fit to the data, with $M$ being the stellar masses for clarity of notation, $\alpha$ the parameter that controls the low-mass end slope of the SMF, $\phi^*$ a normalisation factor and $M^*$ the characteristic stellar mass at which the slope of the SMF changes significantly. Errors on $\phi$ come from adding in quadrature the statistical error from Poisson noise and a systematic error from a resampling of the galaxy stellar mass as for the centrals. Best-fit values are listed in Table 6.2. We exclude from the fit the bins below $\log M_\star < 10.3$ to be further from the completeness limit. It is not straightforward to compare stellar mass function measurements from different galaxy and cluster samples that used different methods and observations. In particular, the amplitude of SMF will strongly depend on the selection function of the galaxy survey considered. In this work we therefore focus on a comparing the shape of the SMF with previous literature results, where the normalisation is completely arbitrary.

In Figure 6.8 we show our data points and best fit in different redshift bins and for the whole redshift range, along with the results from Vulcani et al. (2013) for all galaxy morphological types in clusters from the ESO Distant Cluster Survey clusters at $0.4 < z < 0.8$. We normalise their results so that they match ours at $\log M_\star = 11$ in the lowest redshift bin. They find that the SMF is roughly flat at those redshifts, with a low-mass slope just above -1 ($-0.915 \pm 0.026$), and less steep than the low-redshift sample (where $\alpha = -0.987 \pm 0.009$ at $0.04 < z < 0.07$). We also find that the slope is less steep in the highest redshift bin at $0.5 < z < 0.7$ ($z_{\text{mean}} \sim 0.6$), but still below -1 ($-1.108 \pm 0.034$). However, if we were to push the fit limit down to lower masses, our $\alpha$ would also rise above -1. This is in fact seen when we assume a Salpeter IMF and fit over the same mass range, as this has the effect of shifting the whole distribution towards higher masses. We conclude that the discrepancy is due to different ways of dealing with the sample incompleteness. At the high mass end Vulcani et al. (2013) have low-number statistics due to the few clusters analysed, so the SMF is not well constrained there.

We also plot the best fit from Weigel et al. (2016), who used the SDSS clusters catalogue
from Yang et al. (2007) in the halo mass range $13.5 < \log M_h < 15$. This sample partially overlaps with our lowest redshift bin ($0.1 < z < 0.3$), given that their cluster catalog goes out to redshift 0.2. We normalize their results so that they match ours at $\log M_* = 11$ in the highest redshift bin. Their low mass end slope is also below $-1 (-1.07 \pm 0.02)$, but slightly less steep than our lowest redshift bin. In Yang et al. (2009) they take carefully into account the cluster completeness for the same sample of Weigel et al. (2016), which may impact on the normalisation but also the shape of the SMF (e.g. if we consider a higher fraction of high mass clusters than another analysis, we may measure a higher $M_*$). They find that the satellites low-mass–end slope is steeper ($\alpha \sim -1.2$ to $-1.6$) than what found in Weigel et al. (2016) at our halo masses, and satellites are the dominant contribution at the low–mass end. Our best–fit $M_*$ is $\sim 0.5$ dex above the result from Weigel et al. (2016), causing the discrepancy seen at the high mass end. We cannot compare this value to the results from Yang et al. (2009), as they separate satellites from central galaxies in the conditional luminosity function, however we believe that the discrepancy is due to the cluster selection function: a qualitative analysis of the two samples shows that our volume–limited redMaPPer catalog has a fraction of clusters out to $\log M_{200c} \lesssim 14$ which is $5 - 10\%$ less than what is found in Yang et al. (2007) catalog. This might cause the difference in the characteristic mass of the SMF.

The main conclusion of our SMF analysis is that we find evidence for an evolution of the low–mass end slope over the redshift range $0.1 < z < 0.7$, and no or little evolution at the high–mass end. This implies that the population of low mass galaxies evolved significantly since redshift 0.7, while the mass build-up of the more massive galaxies has mostly been completed by then. Given the absence of evidence for redshift evolution seen in the previous subsection, the behaviour observed at the massive end includes the centrals.

### 6.5 Mass growth and definition of centrals

#### 6.5.1 Central stellar mass growth

While semi-analytic models (De Lucia & Blaizot 2007) predict BCG stellar mass growth of the order of 4 between redshift 1 and 0, observations seem to be in contrast. Lidman et al. (2012) found an increase of $\sim 1.8$ between $z = 0.9$ and $z = 0.2$. We follow a similar method and correct the stellar mass of the central in order to take into account for the
6.5. Mass growth and definition of centrals

Figure 6.9: Central mass growth with redshift. The stellar masses are divided by the corresponding cluster halo mass at \( z = 0 \) for a comparison of different clusters. The data points represent the median stellar mass fractions in redshift bins.

Figure 6.10: Distribution of the offsets from the redMaPPer central for the most massive cluster galaxy (black points) and the brightest cluster galaxy (red triangles) when they do not coincide. Errorbars are given by the Poisson error.
correlation with the mass of the halo it belongs to. When we correct the BCG mass using the $M_{200c}$ estimate from the weak lensing calibration we find no evidence of stellar mass growth between redshift 0.7 and 0.1. It follows that the mild redshift evolution found in Section 6.3 for the SHMR of centrals is due to a different cluster selection function at different redshifts. Correcting by the halo mass that the cluster would have today brings to a different result. We use the mean accretion rate from Fakhouri et al. (2010) to extrapolate the mass of the clusters from the redshift at which they were observed to the current time. The results are shown in Figure 6.9. Between redshift 0.7 and 0.1 we find a growth of a factor $\sim 1.6$: as expected due to the significant mass accretion of halos from redshift 1, the central mass growth is higher when correcting for the halo mass as it would be today. On the other hand, the scatter in the mass fraction is considerably high, $\sim 30 - 50\%$ in each redshift bin. This result corresponds to a $\sim 0.2$ dex growth, which is consistent with $0.29 \pm 0.11$ dex between $z = 1$ and $z = 0$ found by Zhang et al. (2016) for the cluster sample with $\log(M_{200c}/M_\odot) > 13.85$ (the lowest mass systems are excluded due to uncertainties in the X-ray temperature–mass relation).

6.5.2 Definition of central, BCG and most massive galaxy

So far we have considered redMaPPer centrals in comparison with results from some studies of BCGs, as if they were the same objects. Discerning between these two components is not always trivial because galaxies in the core of the cluster are moving at speeds of $\sim 200$ km/s and also will undergo merging and stripping events.

We identify the BCG as the brightest galaxy in $i$-band absolute magnitude and the most massive cluster galaxy (MMCG) as the galaxy with the highest stellar mass. The latter should also roughly correspond to the BCG if we consider that most of the giant red galaxies close to the cluster core have similar mass-to-light ratios. In order to select the possible candidates, we use $N = \Sigma_i p_{\text{mem}}$ to estimate the number of galaxies $N$ in each cluster, where the sum goes over all the galaxies associated with the cluster. Only galaxies in the highest 40th percentile of the $p_{\text{mem}}$ distribution are considered, in order to avoid considering galaxies that are not associated with the cluster. We find that $\sim 24\%$ of clusters have a MMCG that is not the redMaPPer central, and $\sim 30\%$ have a BCG which is not the central. If the redMaPPer centre is given as a truth table, then the most massive galaxy traces better the central than the brightest. We can interpret this result in terms of abundance matching. If there were no scatter in the halo-galaxy abundance
6.6. Impact of the Initial Mass Function

The choice of the IMF is regarded as one of the main cause of systematics in stellar mass estimation (Coupon et al. 2015). The IMF describes the distribution in mass of the stars when they enter the main sequence. It is given as the number of stars that have been born with initial stellar masses between $M_*$ and $M_* + dM_*$: $\xi(M_*)dM_*$. Some of the most used IMFs are shown in Figure 6.11 and are defined as:

- Salpeter (1955): $\xi(M_*) = kM_*^{-2.35}$, where $k$ is a normalisation factor.

![Figure 6.11: Most commonly used Initial Mass Functions. Note that the Salpeter IMF diverges at the low-mass end.](image)

matching, then this statement would always be true: the galaxy with most stellar mass would also be the central as its sub-halo would be the most massive among all sub-halos. In reality, the existing scatter between stellar mass and sub-halo mass impacts on the one-to-one relation between those two quantities and the MMCG will not always be the central. Similarly, Hoshino et al. (2015) found that $20 - 30\%$ of SDSS redMaPPer centrals are not the brightest Luminous Red Galaxies (LRGs) in the cluster. The offset distribution of the MMCGs and BCGs compared to the redMaPPer centres are shown in Figure 6.10 for those clusters in which MMCG (or BCGs) and centres do not correspond.
Chapter 6. Cluster evolution results from DES Year 1 redMaPPer clusters

• Kroupa (2001): $\xi(M_*) = kM_*^{-\alpha}$, where

$$\alpha = \begin{cases} 
0.3 & \text{if } M_* < 0.08 \\
1.3 & \text{if } 0.08 < M_* < 0.5 \\
2.3 & \text{if } M_* > 0.5 
\end{cases} \quad (6.8)$$

• Chabrier (2003):

$$\xi(M_*) = \begin{cases} 
\frac{0.158}{\ln(10)M_*} e^{-\frac{\left(\log(M_*) - \log(0.08)\right)^2}{2 \times 0.69^2}} & M_* < 1 \\
kM_*^{-2.3} & M_* > 1 
\end{cases} \quad (6.9)$$

where $k$ is a normalization factor.

The Kroupa (2001) and Chabrier (2003) IMFs are representative of the IMF in the Solar neighbourhood, and the Salpeter (1955) one is considered a dwarf–rich or bottom–heavy IMF, as it deviates from the others at $M_* < 1M_\odot$.

Most works report their results assuming a Chabrier IMF, but several studies (e.g. Barnabè et al. 2013, Martin-Navarro et al. 2015, Smith et al. 2015) have shown that the IMF of massive elliptical galaxies is better described by a more bottom-heavy function. If that is the case, SHMR may be biased (Kravtsov et al. 2018) at all halo masses, as a result of the stellar mass estimates being biased for most of the red sequence galaxies. So far we have assumed a Chabrier IMF for a more straightforward comparison with other literature results. Here we reproduce the same analyses assuming a Salpeter IMF in the SSP models used to fit the stellar mass. This represents the extreme case of an IMF diverging at the low mass end: the difference between the SHMR obtained by assuming a Chabrier and a Salpeter IMF will give us an estimate of the systematic uncertainty due to the uncertainty on the IMF. In Table 6.1 we report the results for the SHMR when assuming a Salpeter IMF, and in Table 6.2 for the SMFs. This different IMF has the effect of biasing the galaxy and the cluster stellar masses, resulting in a change in the intercept of the linear relation between halo mass and stellar mass, and in the mean of the centrals SMF log–normal fit. Table 6.1 shows that the pivot Log($\tilde{M}_*$) is 0.23–0.27 dex higher in the case of a Salpeter IMF. Kravtsov et al. (2018) find that the effect of a more bottom-heavy IMF steepens the SHMR, as they study this effect by introducing a mass-to-light ratio which depends on the velocity dispersion in galaxies (and therefore on their total mass). In our work we are assuming the same IMF for all galaxies, as our SED fitting of photometric optical
6.7 Intra-cluster light

In Section 6.3.2 we mentioned that the ICL can contribute up to $\sim 40\%$ of the total cluster stellar mass. This statement is based on ICL measurements from the DES data. Through averaging $\sim 300$ galaxy clusters from the DES Y1 redMaPPer catalog, in Zhang et al. (2018) we report the detection of diffuse intra-cluster light at a surface brightness limit of 30 mag/arcsecond$^2$ to 1 Mpc in DES $r-$band. The analysis is further verified by averaging the images of random points and point-like sources. After estimating the light from cluster galaxies, we infer that the diffused intra-cluster light associated with the cluster central galaxies extend to 200 kpc and beyond. This diffuse light constitutes a significant component of the central galaxy light: light contained beyond 32 kpc makes up $\sim 42\%$ of the total light within 200 kpc. In Figure 6.12 we show the derived ICL data would not be able to distinguish between different IMFs, and most of the cluster stellar mass is contributed by the old elliptical galaxies. This measurement gives us the most conservative upper limit to the SHMR and SMF. Our result is remarkably consistent with Leauthaud et al. (2012a), who find a 0.25 dex shift in the $f_\star - M_{\text{halo}}$ relation due to changing IMF from a Chabrier to a Salpeter.

Figure 6.12: This figure shows the derived ICL profiles (upper panel) and the uncertainties of the measurements (lower panel). Cluster galaxy residue (red point) is subtracted from the raw ICL measurements (blue line) to derive pure ICL profile (red line). Uncertainties of the ICL profiles are displayed as the shaded regions (upper panel) and also shown in the lower panel against radii. The ICL profiles are measured with high S/N to 1 Mpc, despite the subtraction of cluster galaxy residue introduces significant noise into the profile. Plot by Yuanyuan Zhang.
Chapter 6. Cluster evolution results from DES Year 1 redMaPPer clusters

Figure 6.13: Colour Profile of pure ICL. Errors are computed with the Jackknife method. The horizontal lines are the mean redMaPPer colours (K-corrected to $z = 0.25$) from the redMaPPer cluster members at $0.2 < z < 0.3$ and their central galaxies. The shaded region around the members’ colour mean represents 1 standard deviation of the sample.

Profiles (upper panel) and the uncertainties of the measurements (lower panel). Cluster galaxy residue (red point), excluding the central galaxy, is subtracted from the raw ICL measurements (blue line) to derive a “pure” ICL profile (red line). The pure ICL profile therefore contains the contribution of the central galaxy and the diffuse stellar matter, given that there is no clear separation between the two components. Uncertainties of the ICL profiles are displayed as the shaded regions (upper panel) and also shown in the lower panel against radii, where the errors are computed through a jackknife resampling of 40 regions. The ICL profiles are measured with high S/N to 1 Mpc, despite the subtraction of cluster galaxy residue introducing significant noise into the profile.

We further derive the ICL colour profile of $g - r$, utilizing our measurements of ICL profiles in the $g$-band. The result is shown in Fig. 6.13. We find that the mean colour of pure ICL becomes bluer at larger radii. A $\chi^2$ minimisation gives a gradient $\nabla(g - r) \equiv \frac{d(g-r)}{d \log(r)} = -0.203 \pm 0.011$ within the inner 90 kpc, showing a negative colour gradient at a 18$\sigma$ level. If we only consider the range $10 < r < 90$ kpc, therefore excluding the central part of the CG we find $\nabla(g - r) = -0.152 \pm 0.027$. The result is consistent with previous works (e.g. DeMaio et al. 2018) on ICL colour gradient in individual clusters, although there exist clusters that does not display this trend. Note that the “spikes” in Figure 6.13 are a consequence of our measurements. In fact, these are present in the pure ICL profile
6.7. *Intra-cluster light*

Figure 6.14: Left: Cumulative stellar mass profile contribution of different cluster components for DES clusters at $0.2 < z < 0.3$. Right: Fraction of stellar mass that resides in the central plus the pure ICL as a function of radius. These measurements are too sensitive to the noise in the galaxies profile subtracted from the raw ICL profile beyond 100 kpc, we thus can only base our analysis below that value.

from Figure 6.12, and come from the galaxies profile which is subtracted from the “raw” ICL measurement. The spikes show up at the galaxies’ positions. The $g$–band profiles are even fainter and noisier than those in $r$–band, and thus are more visible in the colour profile.

In Figure 6.13, we also show the colours of cluster central and satellite galaxies for comparison to ICL. Those are the mean colours from \texttt{MODEL\_MAG} magnitudes, K-corrected to $z = 0.25$ as done for the ICL. While in the inner $\lesssim 10$ kpc the ICL is as red as most central galaxies, outside this range it appears to be consistent with the cluster satellite galaxies. This result, together with ICL getting bluer at larger radii, indicate that in the inner tens of kpc the central galaxy blends in the ICL profile, and in the outer regions the ICL build–up channel is likely dwarf disruption and tidal stripping. In fact, the former mechanism is expected to create a colour gradient as the disrupted dwarfs lived at different radii depending on their mass (and therefore on their colour). On the other hand, tidal stripping will be stronger closer to the cluster centre and will be able to strip the redder, inner parts of the cluster galaxies. Major mergers are not likely to be the main ICL formation mechanism, as this would give rise to more uniform colour profiles (e.g. Eigenthaler & Zeilinger 2013).

From the $g$ and $r$ profiles we can also derive stellar mass profiles. We use the relation between colour and mass-to-light ratio in $r$–band derived in Bell et al. (2003):

$$\log(M_*/L_r) = 1.097(g - r) - 0.306.$$ 

This equation has been derived for $g$ and $r$ SDSS...
Chapter 6. Cluster evolution results from DES Year 1 redMaPPer clusters

filters, but the difference in the magnitudes brought by the use of DES filters is negligible compared to the typical errors in the stellar mass. These values have been corrected by 0.1 dex to provide estimates consistent with a Chabrier IMF, while Bell et al. (2003) used a corrected Salpeter IMF. The $M/L$-colour relation is used at all considered radii to derive a stellar mass surface brightness profile $\Sigma_* = M/L_r \times \Sigma_{L, r}(R)$. Luminosities are estimated from the absolute magnitudes $M_r$ derived from the apparent magnitude $r$ as $M_r = r - k_{rr} - EC(z) - DM$ where $k_{rr}$, $EC(z)$ and $DM$ are the K-correction, the evolutionary correction and the distance modulus respectively. Similarly it is done for $g$ band. The evolutionary correction used is from Bell et al. (2003): $EC(g, r) \sim (-1.6, -1.3)z$, and the conversion from magnitudes to luminosities in $L_\odot$ units is performed using the absolute magnitudes of the Sun $M_g, \odot = 5.15$ and $M_r, \odot = 4.67$. Here we show results for the $r-$band as it is less noisy than the $g$ band. In Figure 6.14 we show the cumulative stellar mass profiles obtained in this way, and compare to the stellar mass results computed as described in Chapter 2 and Chapter 5 with the BMA method. From the Y1 redMaPPer sample, we only select the same clusters used for the ICL detection for this comparison.

The profile of the central galaxy plus the pure ICL is shown in red, with the shaded region being the error. Jackknife errors on the measured fluxes have been propagated to the stellar mass with the error propagation chain. This measurement is too sensitive to the noise in the galaxies profile subtracted from the raw ICL profile beyond 100 kpc, and we therefore restrict the analysis to this radius. This profile is comparable to the mean stellar mass value of centrals (dashed line) in the range $8 \text{kpc} \lesssim r \lesssim 30 \text{kpc}$, showing that our stellar mass estimates from the MOF photometry are able to recover the diffuse ICL component within this range on average. The brown line represents the profile from member galaxies in our cluster catalog with masses computed through the BMA method. Clearly in this case the mass of the central is considered at 0 kpc from the centre instead of being an extended component, explaining the discrepancy at low radii. We also show the mean value of the total (i.e. from all members) mass within 200 kpc. It is interesting to understand what fraction of the total stellar mass is in the ICL component. This is shown in the right-hand panel of Figure 6.14, where the total stellar mass comes from the ICL measurement plus the members from our cluster catalog (excluding the central, already included in the ICL measurement), and is shown in blue in the left-hand panel. While the size of a typical galaxy, taken as the radius within which most of the light ($\sim 90\%$) is emitted, is roughly 32 kpc, the extended halo around the cluster centrals constitutes a
significant contribution (\(\sim 40\%\)) to the total stellar mass of clusters out to 100 kpc and possibly beyond. Note that the ICL stellar mass fraction only drops by 10\% between 30 and 100 kpc, showing the importance of the aperture considered when computing SHMR and SMF for centrals.

6.8 Conclusions

In this Chapter we have performed several cluster evolution analyses for \(\sim 76,000\) DES Y1 redMaPPer clusters using DES Y3 photometry. These studies had not previously been carried out with samples of comparable size (usually 1 – 3 orders of magnitude smaller). Our main results can be summarised as follows:

- A power law fits well the stellar-to-halo mass relation over the halo mass range studied (\(10^{13.5} \lesssim M_{200c}/M_{\odot} \lesssim 10^{14.6}\)) for centrals and the whole galaxy population in a volume–limited sample of DES Year 1 redMaPPer clusters. A Bayesian linear regression method allows to take into account errors on stellar mass, halo mass and redshift, while introducing an intrinsic scatter to the relation. We find that the total stellar mass scales almost linearly with halo mass in logarithmic scale as: \(M_{\star}^{\text{tot}} \propto M_{200c}^{0.89}\) with an intrinsic scatter at fixed halo mass of \(0.2492 \pm 0.0010\). The slope found is steeper than several previous observational works, showing that the star formation efficiency is not as suppressed as previously thought at higher halo masses. Moreover, we find that \(\sim 7\%\) of cluster baryons are transformed into stars. These measurements will be useful to define the inputs of galaxy formation and evolution simulations.

- We provide measurements of the SMF for centrals, which is found to be log–normal at masses \(\log(M_{\star}/M_{\odot}) \gtrsim 10.8\). In particular, the value of the width \(\sigma_c\) is \(0.246 \pm 0.002\)stat \(\pm 0.05\)syst and can be used to constrain abundance matching models. On the other hand, the SMF of the whole galaxy population in clusters is fit to a single Schechter function, with a low-mass end slope of \(\alpha = -1.119 \pm 0.025\) for a Chabrier IMF. We find evidence this slope is evolving over the redshift range \(0.1 < z < 0.7\), while there is no or little evolution at the high–mass end. This implies that the population of low mass galaxies evolved since redshift 0.7, while the mass build-up of the more massive galaxies has mostly been completed by then.
A measurement of the diffuse intracluster light has been possible for \( \sim 300 \) DES clusters at redshift \( 0.2 < z < 0.3 \) using \( g \) and \( r \) fluxes. We find that the mean colour of pure ICL becomes bluer at larger radii. A \( \chi^2 \) minimisation gives a gradient 
\[
\nabla(g - r) \equiv \frac{d(g-r)}{d \log(r)} = -0.203 \pm 0.011 \text{ within the inner 90 kpc, showing a negative colour gradient at a } 18\sigma \text{ level. While in the inner } \lesssim 10 \text{ kpc the ICL is as red as most central galaxies, outside this range it appears to be consistent with the cluster satellite galaxies. This result, together with ICL getting bluer at larger radii, indicate that in the inner tens of kpc the CG blends in the ICL profile, and in the outer regions the ICL build–up channel is likely dwarf disruption and tidal stripping. We also find that the central plus ICL components contribute to } \sim 40\% \text{ of the total stellar mass of clusters within 100 kpc at } 0.2 < z < 0.3.
\]

In the last three Chapters, we have shown how stellar masses (combined with X-ray and/or weak lensing measurements) can be used to define a physically motivated cluster mass proxy for cosmology, while simultaneously obtaining measurements useful to understand structure formation and evolution. In the future, we plan on providing the same mass proxy and cluster evolution measurements for a much larger sample of clusters from DES Y3 data, spanning redshifts out to \( z \sim 1 \). We also plan on adding colour probabilities information to SHMR and SMF analyses, to estimate the relative contribution and evolution of red sequence and blue cloud.
Chapter 7

Conclusions and future work

“My real love has always been the sleep that rescued me by allowing me to dream.”

Luigi Pirandello

In this thesis, I have explored the properties of tens of millions of galaxies that have been observed by the Dark Energy Survey to study gravitational wave sources and dark matter in galaxy clusters. All of the analyses performed are easily transferrable to larger future datasets, which will include the final DES data and a larger number of LIGO events in the near future, and LSST data in the longer term.

In Chapter 2, I have presented the methods used to derive redshifts, stellar masses, and other properties of galaxies from photometric surveys. In particular, I have shown how a Bayesian Model Averaging method has been developed and applied in my work for galaxies in clusters studies. This method naturally takes into account the uncertainties due to the model selection, and working with a code that I developed has provided me with the flexibility needed to perform the varied analyses presented in the following chapters. The outputs of these methods have been used for two different science cases, both of which have important implications for cosmology: an understanding of galaxies and their evolution is a fundamental step towards unlocking the dark sector of the Universe.
Chapter 7. Conclusions and future work

7.1 Gravitational waves

The discovery of the first gravitational wave signal from a binary neutron star coalescence, GW170817, and its associated electromagnetic counterpart has been a milestone in the history of astronomy. The identification of the galaxy that hosted this event (and a careful characterisation of its redshift) has allowed new constraints to be placed on the Hubble constant, although currently not as stringent as those from more traditional methods.

7.1.1 Conclusions from this thesis

In this thesis, I have shown that an analysis of the host galaxy can also provide useful information on the formation mechanisms and evolution of binary neutron stars, which are still poorly understood. By applying these concepts to the host galaxy of GW170817, NGC 4993, I have described the extensive morphological and spectral analyses performed. The results show that NGC 4993 is an early–type galaxy, with $i$-band Sérsic index $n = 4.0$ and low asymmetry ($A = 0.04 \pm 0.01$), which is unusual for sGRB hosts. However, shell structures, dust lanes and photometric properties are consistent with a disturbed galaxy that has likely undergone a recent galaxy merger. Neither spatially–resolved broadband SED, spectral fitting nor pixel colour–magnitude analyses show evidence for recent star formation. The best–fit SFH has been used to estimate the BNS merger rate in this type of galaxy when a pure star formation scenario is assumed for BNS formation: $R_{\text{NSM}}^{\text{gal}} = 5.7^{+0.57}_{-3.3} \times 10^{-6}\text{yr}^{-1}$. This type of calculation has been extended to all observable early type galaxies in the volume which is observable by LIGO, obtaining $0.038^{+0.004}_{-0.022}$ events in total for the LIGO observing seasons O1 and O2. In the pure SF scenario, most of the contribution to the expected number of observable events comes from late–type, star forming galaxies, summing up to $\sim 0.5$ events from all galaxy types. These numbers, together with the observation of GW170817 in NGC 4993, suggest that pure star formation may not be the only formation mechanism of BNSs. I have suggested that dynamical interactions may have affected the formation or evolution of the system. If such interactions arose during the galaxy merger, the subsequent time elapsed can constrain the delay time of the BNS coalescence. By using velocity dispersion estimates and the position of the shells, I find that the galaxy merger occurred $t_{\text{mer}} \lesssim 200$ Myr prior to the BNS coalescence.

Other authors have followed our line of thought and reached similar conclusions. Bel-
czynski et al. (2018) probe different formation mechanisms of double compact objects and find that these are unlikely to happen in this type of galaxy, suggesting that the observation of this event in NGC 4993 is either statistically unlikely, or that formation mechanisms need to be revised. Ebrová & Bílek (2018) have described in more analytical detail the shells of NGC 4993 from HST data, finding that the galaxy merger happened around \( \sim 400 \) Myr ago. If this is a more accurate estimate of the time since the galaxy merger than our value, then it should be used as an estimate of time delay from a dynamically driven formation model. However, this does not affect our conclusions.

In Chapter 3, I have also presented the role of galaxy catalogs within electromagnetic follow up programs of GW sources. I have implemented a host galaxy search within the DES GW pipeline, which is useful to both match potential candidates to their host and to reject SNe, which are the most likely contaminants of kilonovae. In both cases, it is crucial for the galaxies to have an estimated photo-z.

### 7.1.2 Future work

A host galaxy search is currently being performed within the DES–GW team in the context of the BBH event GW170814. Even though an EM counterpart is not (theoretically) expected from such an event, it is still important to reject hundreds of SNe from the list of potential BBH transients, and match the remaining ones (or flag them as hostless). An analysis of potential host galaxies is also interesting, even if no counterpart is found. The LIGO 90\% probability region happens to be fully covered by DES Y3 data, and given the redshift range estimated from the GW signal \((0.07 < z < 0.14)\), we can select a DES galaxy sample: there are \( \sim 6,000 \) galaxies, and this sample is complete at these redshifts above \( M_* \sim 10^8 M_\odot \). In the context of dynamically driven compact binary formation as suggested for GW170817, groups of galaxies are of interest because the galaxy mergers are more frequent there. In this spirit, I have decided to explore those objects, and in Figure 7.1 I show the distribution of redMaPPer groups and clusters at \( z < 0.25 \) that overlap the LIGO 90\% probability area. The analysis of these galaxies and clusters is part of my on-going research.

The next LIGO observing season (O3; October 2018 – September 2019), is expected to bring a 10–fold increase in number of detections: \( \sim 8 \) BNS events and \( \sim 100 \) BBH signals (computed from Chen et al. 2017). I am involved in DECam and Gemini proposals to follow up LIGO O3 events, and obtaining photometry and spectra of the transients
and host galaxies is part of the plan. If we are successful, I plan on extending the work presented here to future BNS events. If BBH events do no show any counterparts, the same analysis can still be carried out in a statistical way. I plan on implementing an observational methodology for cross-correlating galaxy catalogs with BBH GW events, given probability sky maps for each event. My method would incorporate full photometric redshift PDF information and a flexible prior on host galaxy properties. The host galaxy dependance will reveal information on BBH formation and nature (as suggested in e.g. Raccanelli et al. 2016). From such analysis, there is also room for measurements of the Hubble constant: the GW event provides a distance measurement, and our galaxy catalogs will have computed photometric or spectroscopic redshifts. Measurements in this direction are extremely valuable means towards understanding the existing tensions between $H_0$ estimates from SNe and CMB experiments.
7.2 Clusters

7.2.1 Conclusions from this thesis

Stellar mass is regarded the most robust galaxy property that can be estimated from SED fitting. However, the typical uncertainty on photo-z’s can pose significant challenges for deriving this property if the galaxies’ redshifts need to be assumed. Recent cluster finders, such as redMaPPer, are able to provide much excellent photo-z estimates, so that this problem can be overcome. In Chapter 4, I have presented an analysis on stellar mass estimation with early DES data for the galaxy cluster RXC J2248.7–4431. The opportunity for a consistency test is provided by the overlap with HST data, and we find that DES is able to estimate stellar masses within 25% of HST values when the cluster redshift is assumed. Using the weak lensing measurements from Melchior et al. (2016), I have studied total stellar mass and stellar mass fraction profiles of this cluster out to the very large radii that DES is able to probe, thanks to the DECam wide field of view. Within $r_{200c}$ the stellar mass fraction is $\sim 0.7\%$, which is compatible with other results from the literature. This means that in this cluster only $\sim 4\%$ of the baryons are locked into stars. In the future, I plan on providing an estimate of the density in stars $\Omega_*$ from the stellar masses I have computed from DES galaxies.

I have presented the follow up of the work on the stellar mass fraction in clusters in Chapter 6. Using $\sim 76,000$ clusters from the DES Y1 redMaPPer sample, I show that $f_* \sim 7\%$ and that the stellar mass fraction is roughly constant over the mass range $13.5 < \log(M_{200c}/M_\odot) < 14.5$. This indicates that the suppression of star formation efficiency at larger halo masses is not as strong as previously thought, and it is the contribution of satellites that makes this efficiency only a mild function of halo mass. The total cluster mass estimates are derived from weak lensing studies performed by DES collaborators.

I have also presented measurements of the stellar–to–halo mass relation for central galaxies, satellites and total cluster content for the same Y1 cluster sample. For the total content of clusters: $M_\star^{\text{tot}} \propto M_{200c}^{0.89}$ with an intrinsic scatter at fixed halo mass of $0.2492 \pm 0.0010$ (1σ uncertainty). Central galaxies show a shallower slope (in logarithmic scale) in their relation with total mass ($\sim 0.4$). It is the satellites that contribute to the steepening of the total SHMR, as most of the stellar content resides there for increasing halo mass. The results presented are mostly in agreement with previous works, but they have been measured on a sample which is 1–3 orders of magnitude larger than other
literature results.

Chapter 6 also includes measurements of the stellar mass function in clusters. I have fit this with a log-normal distribution for the centrals, and a Schechter function for the overall galaxy population. The measured low mass end slope is $\alpha = -1.119 \pm 0.025$ ($1\sigma$ uncertainty), with evidence of evolution over $0.1 < z < 0.7$. The high mass end shows no signs of evolution, implying that the mass build up of massive galaxies has ended by $z \sim 0.7$, as opposed to low mass galaxies that continue to evolve. I have contributed to the work on ICL detection lead by DES collaborator Yuanyuan Zhang. In particular, I have focused on colour and stellar mass measurements of this component. I have shown that the ICL becomes bluer toward larger cluster radii and that this is a consequence of different contributions to the diffuse light. In the core of the cluster, the central galaxy blends into the ICL, while towards larger radii dwarf disruption and tidal stripping are the most likely formation mechanisms of ICL. Moreover, ICL is an important component for cluster mass estimation: it can contribute up to $\sim 40\%$ of the total stellar mass within 100 kpc. I have also explored the effect of the assumed IMF on the results reported, which can be substantial: it can bias cluster stellar mass by up to $\sim 0.27$ dex.

Estimating the total mass for DES clusters is necessary for cluster cosmology. The tight correlation found in the SHMR shows that cluster stellar mass is a good proxy for total mass. Chapter 5 has shown that our stellar mass based proxy $\mu_*$ is a promising mass observable. By comparing it with X-ray temperatures, I have found that the scatter at fixed $\mu_*$ is $\sigma_{\log T_X|\mu_*} \sim 0.15$ and $\sim 0.14$ for the XMM and Chandra samples respectively. I found that these values are competitive compared to results from the widely used redMaPPer richness. This mass proxy has also been calibrated with weak lensing analyses from SDSS data in work lead by DES collaborator Maria Pereira.

### 7.2.2 Future work

Our $\mu_*$ team is currently implementing the methodology developed in this thesis and in external work into the Voronoi-Tessellation cluster finder, and we will provide VT DES cluster catalogs with $\mu_*$ measurements in the near future. This catalog will represent an interesting alternative to redMaPPer clusters: we have seen that the intrinsic width of the red sequence increases with redshift, so that red sequence–based cluster finders may face more difficulties in identifying clusters at higher $z$. Moreover, we will be able to provide measurements for both red sequence and blue cloud galaxies.
While it is true that DES is mostly designed to observe galaxies and clusters out to redshift $\sim 1$, we have shown in Chapter 6 that the red sequence intrinsic width increases to $\sim 0.1$ dex already around redshift 0.6 for all colours. We predict that this scatter will be even larger for the full Y3 cluster sample, reaching out to $z \sim 1$, so that identifying clusters with alternative methods may bring a substantially different sample. Furthermore, there is some ongoing effort within DES to match DECam photometry to other infrared surveys, such as WISE and VHS, which are expected to help cluster finding at $z > 1$.

In this golden era of large astronomical surveys, I am stunned by the overwhelming amount of new data that we have the opportunity to utilise for an incredibly wide range of astrophysical studies. While we pave our way towards a gravitational wave precision cosmology program to complement the classical cosmological probes, significant mysteries remain on the astrophysics of the systems studied, dark matter, dark energy and colliding black holes. I look forward, as a scientist or a spectator, to new exciting discoveries about the dark components of the Universe to be unveiled.
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“Of course it is happening inside your head, Harry, but why on earth should that mean it is not real?”

J. K. Rowling, The Deathly Hallows