Contribution of a deformable striking-ship structure to the structural crashworthiness of ship-ship collisions

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Abstract

Ship-ship collision frequently occurs in shipping industry. The risks of economic losses and marine pollution have been increased by to ship-ship collisions especially involved with large oil tankers or liquefied natural gas (LNG)-fueled ships. Various type of methods are available for the purpose of safety studies in association with structural crashworthiness involving crushing and fracture in ship-ship collisions. In the perspectives of multi-physics and multi-criteria involved, however, the nonlinear finite element method is
certainly one of the most powerful techniques to model the problems. In a ship-ship collision accident where the bow of a striking ship is collided with the side of struck ship, the kinetic energy must be absorbed by both striking and struck ship structures in terms of collision damages and corresponding strain energies. As the bow structure of the striking ship is usually much stiffer than the side structure of the struck ship. It does not allow for deformation and damage. Therefore, no contribution of energy absorption is made by the striking structure. As the energy absorption characteristics of the striking ship depends on the structural arrangement of bulbous bow and flare, however, the contribution of striking ship cannot be entirely neglected. The aims of the present study are to examine the effects of a deformable striking ship structure on the structural crashworthiness of ship-ship collisions using LS-DYNA nonlinear finite element method computations. As an illustrative example in the paper, the struck ship is a VLCC class double hull oil tanker, while the struck ships are two types: a VLCC class tanker and a SUEZMAX class tanker. The relationships between collision forces versus penetration together with their energy absorption capabilities are characterized in association with the contributions of the striking ship bow where the deformable striking ship structures are compared with the rigid striking ship structures. Developed Findings and insights from the present study are summarized.

*Keywords:* Ship-ship collision; deformable striking bow; oil tanker; structural crashworthiness; nonlinear finite element analysis.

**Introduction**

Accidental limit states (ALS) potentially brings about a catastrophe of serious loss of life, and property or environmental damage. The aim of ALS design is to ensure that
the structure is able to withstand specified accidental events such as collision, grounding, fire and explosion and to enable evacuation of personnel from the structure for a sufficient period under specific environmental conditions after accidents occur (Paik and Thayamballi 2003, 2007).

Limit state design and safety assessment relevant to collisions and grounding are generally based on the energy absorption capability of the structure until accidental limit state is reached. As the energy absorption capability can be calculated by integration of the area below the reaction force versus penetration curve of the structure, the improving structural crashworthiness of the ships must be fulfilled to obtain those curves in the accidental event.

As the amount of energy dissipation at the fore part of the striking ship is relatively lower than at the side part of the struck ship, conservative evaluations are relevant especially for safety designs in general, most ship collision simulations have been undertaken in the past where striking ships were modelled as a rigid body (Ammerman and Daidola 1996, Wisniewski and Kolakowski 2002, Haris and Amdahl 2011, Montewka et al. 2012, Sun et al. 2015, Zhang et al. 2016). On the other hand, some other studies have of course been conducted with the striking ships that were modelled as a deformable body (Hogström and Ringsberg 2012, Haris and Amdahl 2013, Storheim and Amdahl 2015), however it is observed that more efforts are recommended to examine the contribution of a realistic striking ships to the structural crashworthiness of ship-ship collisions.
The aim of this study is to investigate the effects of a deformable striking-ship structure on the structural crashworthiness in ship-ship collisions. The characteristics of the energy absorption capabilities of ship structures in collision or grounding were studied in the literature by many investigators using the non-linear finite element method (Amdahl 1983, Simonsen 1997, Zhang 1999, Tornqvist 2003, Urban 2003, Alsos 2008, Hong 2009, Ehlers et al. 2010, 2016, Storheim and Amdahl 2015). This study also uses the non-linear finite element method with the LS-DYNA code (Hallquist 2010).

**Collision Scenarios**

Among various type of ships, the oil tanker which can bring about a significant amount of pollution has been utilized as a target structure in the simulations and a host of researchers have fulfilled studies with oil tankers to reduce loss of financial properties and to prevent loss of lives and environmental damages (Zheng et al. 2007, Tavakoli et al. 2010, Kim et al. 2015, Faisal et al. 2016, Parunov et al. 2016, Youssef et al. 2014, 2017).

In the present study, it is considered that the side structure of a VLCC class double-hull oil tanker is collided with the bow structure of either a VLCC class double-hull oil tanker or a SUEZMAX class double-hull oil tanker. Tables 1 and 2 indicate the principal dimensions of the both ships. Figure 1 shows the finite element models.
Figure 1. The VLCC class (left) and SUEZMAX class (right) double-hull oil tankers.

Table 1. Principal dimensions of the VLCC class double-hull oil tanker.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Dimension</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overall length (m)</td>
<td>318.2</td>
</tr>
<tr>
<td>Moulded breadth (m)</td>
<td>60</td>
</tr>
<tr>
<td>Moulded depth (m)</td>
<td>30</td>
</tr>
<tr>
<td>Moulded draught (m)</td>
<td>21.6</td>
</tr>
<tr>
<td>Dead weight (ton)</td>
<td>300,000</td>
</tr>
<tr>
<td>Transverse frame spacing (m)</td>
<td>5.69</td>
</tr>
</tbody>
</table>

Table 2. Principal dimensions of the SUEZMAX class double-hull oil tanker.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Dimension</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overall length (m)</td>
<td>272.0</td>
</tr>
<tr>
<td>Moulded breadth (m)</td>
<td>48.0</td>
</tr>
<tr>
<td>Moulded depth (m)</td>
<td>23.7</td>
</tr>
<tr>
<td>Moulded draught (m)</td>
<td>16.0</td>
</tr>
<tr>
<td>Dead weight (ton)</td>
<td>157,500</td>
</tr>
<tr>
<td>Transverse frame spacing (m)</td>
<td>4.8</td>
</tr>
</tbody>
</table>

For the present study, the colliding angle between the striking and struck ships as denoted in Figure 2 is varied at $\theta = 45, 90$ and 135 degrees. The speed of the striking ships is varied at $V_2 = 0.5, 3, 6$ and 10 knots, while the struck ship is standstill at $V_1 = 0$ knot. The location of collision is around midship (No. 3 cargo hold) of the struck ship. Also, it is assumed that both striking and struck ships at the time of collision are in the laden (fully loaded) condition. Table 3 indicates a summary for a total of 48 cases studied with varying the collision conditions considered in the present study.
Figure 2. Definition of the collision angle between the striking and struck ships.

Table 3. Case study identification numbers with varying the collision conditions.

<table>
<thead>
<tr>
<th>Case No.</th>
<th>Striking ship</th>
<th>Rigid or deformable</th>
<th>Collision angle $\theta$ (deg.)</th>
<th>Collision speed $V_2$ (knot)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1–12</td>
<td>VLCC</td>
<td>Rigid</td>
<td>90, 45, 135</td>
<td>0.5, 3, 6, 10</td>
</tr>
<tr>
<td>13–24</td>
<td>VLCC</td>
<td>Deformable</td>
<td>90, 45, 135</td>
<td>0.5, 3, 6, 10</td>
</tr>
<tr>
<td>25–36</td>
<td>SUEZMAX</td>
<td>Rigid</td>
<td>90, 45, 135</td>
<td>0.5, 3, 6, 10</td>
</tr>
<tr>
<td>37–48</td>
<td>SUEZMAX</td>
<td>Deformable</td>
<td>90, 45, 135</td>
<td>0.5, 3, 6, 10</td>
</tr>
</tbody>
</table>

Nonlinear Finite Element Method Modelling

3.1 Material Property Modelling

The striking and struck ship structures are made of both mild and high tensile steels. The mechanical properties of mild and high tensile steels (AH32 and AH36) are indicated in Table 4. In the present LS-DYNA simulations, the elastic-perfectly plastic material model is applied without considering the strain-hardening effect. The material option of “Mat.024-Elastic/Plastic Isotropic with piecewise linear plasticity” is adopted to consider the dynamic effects such as strain-rate sensitivity in

Table 4. Material properties of the striking and struck ship structures.

<table>
<thead>
<tr>
<th>Material property</th>
<th>Mild steel</th>
<th>High-tensile steel</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>AH32</td>
<td>AH36</td>
</tr>
<tr>
<td>Density, ρ (ton/m³)</td>
<td>7.85</td>
<td>7.85</td>
</tr>
<tr>
<td>Young’s modulus, E (MPa)</td>
<td>205,800</td>
<td>205,800</td>
</tr>
<tr>
<td>Poisson’s ratio</td>
<td>0.3</td>
<td>0.3</td>
</tr>
<tr>
<td>Yield stress, σ₁ (MPa)</td>
<td>235</td>
<td>315</td>
</tr>
<tr>
<td>Cowper-Symonds</td>
<td>C</td>
<td>40.4</td>
</tr>
<tr>
<td>coefficient</td>
<td></td>
<td>3200</td>
</tr>
<tr>
<td></td>
<td>q</td>
<td>5</td>
</tr>
<tr>
<td></td>
<td></td>
<td>5</td>
</tr>
</tbody>
</table>

3.2 Finite Element Size

As the structural crashworthiness in ship-ship collisions involves crushing and fracture, it is important to assign relevant mesh sizes in the finite element method modelling. In the present study, only plate-shell elements with an aspect ratio of almost unity were used but without beam elements. For the structural areas that are less affected by the collision, coarse meshes were used. The plating was modelled with an element size of 1 m. The stiffener webs were modelled by one element while stiffener flanges were modelled by one element for an angle type and two elements for a T-type girder.

On the other hand, the collided areas were modelled by fine meshes. Paik and Thayamballi (2003, 2007) and Paik (2007a, 2007b) suggested techniques to define relevant size of finite elements to compute the structural crashworthiness of thin-walled structures when a rectangular type of plate-shell elements is utilized. The element size can then be determined from Equation (1) to represent the crushing
behavior of thin walls as illustrated in Figure 3.

\[ s \leq \frac{H}{8} = 0.1228b^{2/3}t^{1/3} \]  

where \( s \) is the element size, \( H \) is the half-fold length which may be taken as \( H = 0.983b^{2/3}t^{1/3} \) (Wierzbiki and Abramowicz 1983), \( b \) is the plate breadth between support members (e.g., stiffeners, frames, stringers), and \( t \) is the plate thickness.

Figure 3. Definition of the half-fold-length of a thin-walled structure crushed under predominantly axial compression and cut at its midsection (Paik and Thayamballi 2007).

In the present study, the above-mentioned Paik-Thayamballi method yields an element size of between 104 - 244 mm, depending on the breadth and thickness of plate at different areas for the element size as indicated in Table 5. To reconfirm this value, a convergence study was performed by varying the element size. Figure 4 shows the results of the convergence study in terms of penetration and absorbed energy of the struck ship structures. The collision between a striking VLCC tanker and a struck VLCC tanker was considered with a collision angle of 90 deg. at a collision speed of 2 knots. The collision also between a striking SUEZMAX tanker
and a struck VLCC tanker was also analysed for the convergence study. As a result, it was realized that the trend is quite similar. It is concluded from the convergence studies that the prediction of the mesh size by the Paik-Thayamballi method is good enough and the element size was finally taken as 200 mm in the present study.

![Graph](image)

**Figure 4.** The convergence study to determine the element size

<table>
<thead>
<tr>
<th>Area</th>
<th>Breadth of plate (b) (mm)</th>
<th>Plate thickness (t) (mm)</th>
<th>A half-fold length (H) (mm)</th>
<th>Element size (s) (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frame space</td>
<td>5690</td>
<td>18.5</td>
<td>828.61</td>
<td>103.68</td>
</tr>
<tr>
<td>Deck height</td>
<td>6600</td>
<td>24</td>
<td>997.67</td>
<td>124.84</td>
</tr>
<tr>
<td>Hull depth (except double bottom)</td>
<td>20608</td>
<td>18.5</td>
<td>1954.2</td>
<td>244.52</td>
</tr>
</tbody>
</table>

**3.3 Dynamic Yield Strength**

The dynamic yield strength of material is determined from the Cowper-Symonds equation (2).
where $\sigma_y$ and $\sigma_{yd}$ are the static and dynamic yield stresses, respectively, $\dot{\varepsilon}$ is the strain rate, and C and q are the Cowper-Symonds coefficients. The coefficients in Equation (2) are taken as indicated in Table 4, where it is noted that they differ for mild and high tensile steels (Paik 2007a, 2007b).

### 3.4 Dynamic Fracture Strain

In the present study, the dynamic fracture strain of material used is determined from the method developed by the authors (Ko et al. 2017). Figure 5 describes the method to determine the dynamic fracture strain $\varepsilon_{yd}$ where the static fracture strain $\varepsilon_{fc}$ is determined as a function of the static fracture strain $\varepsilon_{f}$ of material determined from the tensile coupon test. The dynamic fracture strain to be used for nonlinear finite element method computations is then determined as an inverse of the Cowper-Symonds equation as indicated in Equation (3) (Paik and Thayamballi 2003, Paik 2007a, 2007b).

$$\varepsilon_{yd} = \left[ 1 + \left( \frac{\dot{\varepsilon} \cdot \sqrt{q}}{C} \right) \right] \varepsilon_{fc}$$  \hspace{1cm} (2)$$

where $\varepsilon_{fc}$ and $\varepsilon_{yd}$ are the static and dynamic fracture strains to be used for nonlinear finite element method computations, respectively, $\dot{\varepsilon}$ is the strain rate, and C and q are the Cowper-Symonds coefficients which are taken as indicated in Table 4.
**Figure 5.** Procedure to determine the dynamic fracture strain to be used for nonlinear finite element method computations (Ko et al. 2017).

Using Equation (3), Ko et al. (2017) suggested to determine the strain rate \( \dot{\varepsilon} \) as a function of the collision speed as follows:

\[
\dot{\varepsilon} = 1.528 V^2 - 0.686 
\]  

(4)

where \( V \) is the collision speed in knot of the striking ship.

In the present study, 0.43 and 0.32 of static fracture strain obtained from experiments are used. Table 6 indicates a summary of dynamic fracture strains determined from the above-mentioned method. The plate thickness also affects the fracture strains, therefore, the dynamic fracture strains must differ for different plates with different thicknesses. However, it is interesting to note that the dynamic fracture strain is close to 0.1 which is well adopted in the industry practice, but it is seen that the method of Ko et al. (2017) gives a reasonable guidance to determine the dynamic fracture strains in general scenarios.
Table 6. The dynamic fracture strains used for the nonlinear finite element method computations.

<table>
<thead>
<tr>
<th>Collision speed $V_c$ (knot)</th>
<th>Strain rate $\dot{\varepsilon}$ (1/sec)</th>
<th>Steel grade</th>
<th>Static fracture strain $\varepsilon_{s}$</th>
<th>Critical fracture strain $\varepsilon_{c}$</th>
<th>Dynamic fracture strain $\varepsilon_{d}$</th>
<th>Dynamic yield stress $\sigma_{yd}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>0.079</td>
<td>Mild steel</td>
<td>0.43</td>
<td>0.129</td>
<td>0.100</td>
<td>302.416</td>
</tr>
<tr>
<td></td>
<td></td>
<td>High tensile steel</td>
<td>0.32</td>
<td>0.096</td>
<td>0.086</td>
<td>352.692</td>
</tr>
<tr>
<td>3</td>
<td>3.901</td>
<td>Mild steel</td>
<td>0.43</td>
<td>0.129</td>
<td>0.079</td>
<td>382.240</td>
</tr>
<tr>
<td></td>
<td></td>
<td>High tensile steel</td>
<td>0.32</td>
<td>0.096</td>
<td>0.076</td>
<td>397.322</td>
</tr>
<tr>
<td>6</td>
<td>8.488</td>
<td>Mild steel</td>
<td>0.43</td>
<td>0.129</td>
<td>0.074</td>
<td>407.010</td>
</tr>
<tr>
<td></td>
<td></td>
<td>High tensile steel</td>
<td>0.32</td>
<td>0.096</td>
<td>0.074</td>
<td>411.170</td>
</tr>
<tr>
<td>10</td>
<td>14.604</td>
<td>Mild steel</td>
<td>0.43</td>
<td>0.129</td>
<td>0.071</td>
<td>426.728</td>
</tr>
<tr>
<td></td>
<td></td>
<td>High tensile steel</td>
<td>0.32</td>
<td>0.096</td>
<td>0.072</td>
<td>422.195</td>
</tr>
</tbody>
</table>

3.5 Contact Problem Modelling

Thin-walled structural components contact each other during crushing. Therefore, the structural crashworthiness analysis needs to model contact problems properly. Typically, two types of contact are considered, general contact and self-contact. The former is affected by surfaces between different structural components, while the latter can arise from structural components themselves due to folding or crushing. It is obvious that the effect of overlapping of contacted surfaces can be of significance. In the present study, the contacts between the striking and struck vessels are applied as in LS-DYNA “Automatic Surface to Surface” for general contact and “Automatic Single Surface” for self-contact. The effects of self-contact phenomenon are often omitted for saving computational times in simulations. In the present LS-DYNA computations, however, both general contact and self-contact are taken into account.

3.6 Friction Effect Modelling

During collision, the effect of friction can not be neglected if there is a relative
velocity between the striking and struck bodies. The influence of friction may be of significance for a collision where the contact occurs at the side of the struck ship like a racking type (Paik and Thayamaballi 2007). In the present study, however, a friction constant of 0.3 is assumed for all collision scenarios. This is a simple assumption. However, it should be noted that the characteristics of friction may change even in the same collision scenario as the penetration proceeds. In this regard, further studies are recommended.

3.7 Surrounding Water Effect Modelling

the vessels are moving on the ocean at the time of collision accidents, and thus striking and struck vessels are not fixed in any direction where they naturally move even after collisions. For this reason, the external ship dynamics should be considered, and it is defined with respect to hydrodynamics and the ship motions. The ship hydrodynamics denote the surrounding water effect in terms of added masses, and the ship motions are calculated by carrying rigid-body motion analysis out. In addition, the effect of sea water (e.g., added mass) against vessel’s motions cannot be neglected as a part of kinetic energy is consumed for the movement of the ships involved.

For the present nonlinear finite element method computations, free body boundary condition is applied by using LS-DYNA/MCOL program which can simulate a ship motion taking into account the effect of the added mass during collision (Kuroiwa et al. 1995, Kuroiwa 1996, Kitamura 2000, Ferry et al. 2002, Le Source et al. 2003). In
this modelling, the effect of surrounding water is taken into account in terms of hydrodynamic forces associated with the deceleration of the ships where a virtual mass of the striking and struck ships in surge, sway and yaw motions is added to the actual ship mass. The motions of pitch, roll and heave may be neglected because of relatively lower effects to the computation results than the surge, sway, and yaw directions.

Upon using the LS-DYNA/MCOL solver for ship-ship collisions, the resultant forces and moments imposed on the struck ship structure are calculated at each time step during the simulation, and by using these values the new position of the struck ship is then updated without additional boundary conditions as shown in Figure 6. In the present computations, \( c_{11} = 0.05 \), \( c_{22} = 0.85 \), and \( c_{33} = 0.21 \) in Equation (5) are taken for the movements of the struck ship at each direction (Pedersen and Zhang 1998).

\[
a_{11} = c_{11}m, \quad a_{22} = c_{22}m, \quad a_{33} = c_{33}I_2
\]  

(5)

where \( a_{11} \), \( a_{22} \) and \( a_{33} \) are the added masses in the direction of surge, sway and yaw motions, respectively, \( c_{11} \), \( c_{22} \) and \( c_{33} \) are the coefficients of added masses for each motion, \( m \) is the mass of struck vessel, and \( I_2 \) is the mass moment of inertia of struck vessel.
**Results and Discussions**

In the present study, LS-DYNA computations have been performed for total 48 cases addressed in Table 3. Various results are obtained including deformations, stresses, and resultant forces of both striking and struck ship structures. The relationships between resultant forces versus time, and between penetration versus time are firstly identified from the numerical computations. Using these relations, resultant forces versus penetration curves are then obtained, where resultants forces and penetration are taken at the identical time each other. The relationships between absorbed energy versus penetration can then be obtained by integrating the areas below the corresponding curves.

Maximum penetration is one of primary concerns as the bow structure of striking ship penetrates the side structure of struck ship. In the present study, a reference penetration was measured for the maximum sideways penetration of struck ship’s cargo hold number 3 or for the maximum deformation of striking ship’s bulbous bow tip along the ship’s longitudinal direction. According to Paik and Pedersen (1995),
resultant forces on the struck and striking vessels should be on equilibrium. Hence, the amount of damage is to be calculated in facet of the penetration for colliding and collided structures as well as absorbed energy as a result of collision accident can be calculated by integral of resultant force. For this reason, table 7 indicates a summary of maximum penetration together with the corresponding maximum resultant forces and absorbed energy until all the kinetic energy is entirely consumed.

**Table 7. Maximum structural consequence.**

<table>
<thead>
<tr>
<th>Case</th>
<th>Collision angle θ (deg.)</th>
<th>Collision speed V2 (knot)</th>
<th>Max. penetration (m)</th>
<th>Max. absorbed energy (MJ)</th>
<th>Max. resultant force (MN)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>90</td>
<td>0.5</td>
<td>0.192</td>
<td>2.596</td>
<td>8.288</td>
</tr>
<tr>
<td>2</td>
<td>90</td>
<td>3</td>
<td>3.735</td>
<td>61.009</td>
<td>30.694</td>
</tr>
<tr>
<td>3</td>
<td>90</td>
<td>6</td>
<td>8.710</td>
<td>220.528</td>
<td>36.389</td>
</tr>
<tr>
<td>4</td>
<td>90</td>
<td>10</td>
<td>20.920</td>
<td>484.870</td>
<td>45.280</td>
</tr>
<tr>
<td>5</td>
<td>45</td>
<td>0.5</td>
<td>0.081</td>
<td>0.309</td>
<td>3.739</td>
</tr>
<tr>
<td>6</td>
<td>45</td>
<td>3</td>
<td>1.232</td>
<td>19.907</td>
<td>23.068</td>
</tr>
<tr>
<td>7</td>
<td>45</td>
<td>6</td>
<td>2.763</td>
<td>102.343</td>
<td>40.857</td>
</tr>
<tr>
<td>8</td>
<td>45</td>
<td>10</td>
<td>3.660</td>
<td>322.774</td>
<td>61.007</td>
</tr>
<tr>
<td>9</td>
<td>135</td>
<td>0.5</td>
<td>0.062</td>
<td>0.266</td>
<td>3.698</td>
</tr>
<tr>
<td>10</td>
<td>135</td>
<td>3</td>
<td>1.464</td>
<td>18.741</td>
<td>21.626</td>
</tr>
<tr>
<td>11</td>
<td>135</td>
<td>6</td>
<td>2.368</td>
<td>167.532</td>
<td>39.441</td>
</tr>
<tr>
<td>12</td>
<td>135</td>
<td>10</td>
<td>17.190</td>
<td>644.734</td>
<td>56.082</td>
</tr>
<tr>
<td>13</td>
<td>90</td>
<td>0.5</td>
<td>0.182</td>
<td>2.406</td>
<td>8.068</td>
</tr>
<tr>
<td>14</td>
<td>90</td>
<td>3</td>
<td>3.005</td>
<td>32.859</td>
<td>25.464</td>
</tr>
<tr>
<td>15</td>
<td>90</td>
<td>6</td>
<td>4.760</td>
<td>131.688</td>
<td>47.039</td>
</tr>
<tr>
<td>16</td>
<td>90</td>
<td>10</td>
<td>7.100</td>
<td>342.360</td>
<td>61.860</td>
</tr>
<tr>
<td>17</td>
<td>45</td>
<td>0.5</td>
<td>0.101</td>
<td>0.239</td>
<td>1.759</td>
</tr>
<tr>
<td>18</td>
<td>45</td>
<td>3</td>
<td>0.142</td>
<td>8.247</td>
<td>29.728</td>
</tr>
<tr>
<td>19</td>
<td>45</td>
<td>6</td>
<td>0.513</td>
<td>44.183</td>
<td>47.207</td>
</tr>
<tr>
<td>20</td>
<td>45</td>
<td>10</td>
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Figures 7 and 8 show deformed shapes of the VLCC tanker structures struck by the VLCC and the SUEZMAX tanker structures with a deformable and rigid bow, where collision angles are varied while the collision speed was fixed at 10 knots. The deformations of side structures were measured at around the tip of the striking bow. It is evident that the damage extent and the amount of side structures struck by a rigid striking bow are much larger than those struck by a deformable striking bow.
(a) Deformable bow at a collision angle of 45 deg.  
(b) Rigid bow at a collision angle of 45 deg.

(c) Deformable bow at a collision angle of 90 deg.  
(d) Rigid bow at a collision angle of 90 deg.

(e) Deformable bow at a collision angle of 135 deg.  
(f) Rigid bow at a collision angle of 135 deg.

**Figure 7.** Deformed shapes of struck VLCC tanker at around the tip of striking VLCC bow with a collision speed of 10 knots.
Figure 8. Deformed shapes of struck VLCC tanker at around the tip of striking SUEXMAX bow with a collision speed of 10 knots.

Figures 9 and 10 show the relationships between resultant forces and absorbed energies versus penetration in conjunction with Figures 7 and 8. It is found that at a collision angle of 90 deg., the differences between the deformable and rigid bows are
relatively small in terms of the rupture or perforation of outer and inner shell plate panels. This means that the industry practice in the treatment of striking ship bow as a rigid body may still be useful as far as the rupture of outer and inner shell plate panels are concerned. However, the differences between the deformable and rigid bows are of significance in terms of the structural crashworthiness associated with the maximum penetration and the total volume of damages which are related to the speed and amount of oil spills. This is because the remaining kinetic energy after the rupture of inner shell plate panels is further consumed by damaging not only the struck-ship side structures but also the striking-ship bow structures. Considering that the deformable bow model is more realistic and accurate, it is recommended that the rigid striking bow model applied in the current industry practice should not be used.

(a) Collision angle of 45 deg.  
(b) Collision angle of 45 deg.
Figure 9. The relationships between resultant forces or absorbed energies versus penetration for the VLCC tanker struck by the VLCC tanker at a collision speed of 10 knots.
Figure 10. The relationships between resultant forces or absorbed energies versus penetration for the VLCC tanker struck by the SUEZMAX tanker at a collision speed of 10 knots.

The stiffness of bulbous bow is generally higher than the side structure of the struck vessel. Thus, the influence of a deformable bulbous bow should be considered (Ehlers and Tabri 2012). The behavior of penetration or resultant forces with time for the striking VLCC or SUEZMAX tanker at each collision angle were illustrated in Appendix A to compare the results between striking and struck vessels. Figure 11
shows some example of the behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy. As shown in Figure 11 (a), the rigid bow penetration lengths between SUEZMAX and VLCC are significantly different except the case at collision speed of 10 knots contrast to Figure 11 (c) which shows that those are nearly equal. That is because it stems from the shape of vessel fore part. Even though the fore part of the SUEZMAX is sharper than VLCC, the rigid bow penetration lengths appears almost the same at the collision angle of 90 degree because of the difference in initial kinetic energy, which is influenced by the displacement of the vessel. In addition, relatively low difference of the absorbed energy between collision angles of 45 and 90 degree also can be seen in Figure 11. It seems that the shape of vessel fore part can affect to the damage pattern and extent.

The behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy and maximum resultant forces with varying angle or speed of collision are shown in Appendix B and C. It is found from these results that the effects of the deformable striking ship bow are of significance as the collision speed increases. Also, the maximum penetration occurs at the collision angle of 90 deg. It is again obvious from these computations that the deformable striking ship bow structures absorb some part of the initial kinetic energy of the collision as they penetrate into the struck ship structures in contrast to the industry practice applied with a rigid body.
Figure 1. Some example of the behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy

Concluding Remarks

The aim of the present paper has been to examine the effects of a deformable striking ship bow in ship-ship collisions. An extensive study of nonlinear finite element method computations has been undertaken for given collision scenarios in association.
with the structural crashworthiness. The angle of collision was varied at 45, 90, and 135 deg. The speed of collision was also varied at 0.5, 3, 6 and 10 knots. The collision location was fixed at the center of the number 3 cargo hold of the struck VLCC tanker. Also, both striking and struck ships were considered as a full load condition that can affect the collision location in elevation. A total of 48 scenarios were analyzed by the LS-DYNA nonlinear finite element method. In the industry practice, the striking ship bow is often modeled as a rigid body, but the present study modeled the striking ship bow as a deformable body with the realistic properties of geometry and materials. For a comparison purpose, the rigid body model of the striking ship bow was also considered. Based on the present study, important insights and conclusions can be drawn as follows:

1. The rigid bow model of the striking ship results in a greater penetration than the deformable bow model of the striking ship as the striking ship bow structures absorb some part of the initial kinetic energy in the latter model.
2. The penetration is the largest at the collision angle of 90 deg. as would be expected.
3. The difference of the structural crashworthiness between the deformable and rigid bow models becomes larger as the collision speed increases.
4. The shape of the striking ship bow affects the structural damage patterns and the resulting penetration. As the shape of the striking SUEZMAX tanker bow is sharper than that of the striking VLCC tanker bow, the maximum
penetration of the former is larger than the latter without regard to the fact that the initial kinetic energy of the VLCC tanker is greater than that of the SUEZMAX tanker. Because the displacement of the VLCC is larger than that of the SUEZMAX.

(5) At a collision angle of 90 deg., the difference between the deformable striking-ship bow model and the rigid striking-ship bow model is relatively small until the outer and inner shell plate panels rupture. However, the behavior with the deformable striking-ship bow model is totally different from that with the rigid striking-ship bow model after the rupture of the outer and inner shell plate panels or at other collision angles in terms of the maximum penetration and the total volume of structural damages which are related to the speed and amount of oil spills.

(6) In general, the effects of the deformable striking ship bow are significant in terms of penetration, absorbed energy amount and resultant forces. It should not be neglected in the analysis of structural crashworthiness in ship-ship collisions. Significance becomes greater as the collision speed becomes faster.

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Appendix A. Results of Collision Consequence Analysis

(a) The behavior of penetration with time

(b) The behavior of resultant forces with time

Figure A (1). The effects of the deformable and rigid striking VLCC tanker at a collision angle of 45 deg.
Figure A (2). The effects of the deformable and rigid striking VLCC tanker at a collision angle of 90 deg.
Figure A (3). The effects of the deformable and rigid striking VLCC tanker at a collision angle of 135 deg.
Figure A (4). The effects of the deformable and rigid striking SUEZMAX tanker at a collision angle of 45 deg.
Figure A (5). The effects of the deformable and rigid striking SUEZMAX tanker at a collision angle of 90 deg.
Figure A (6). The effects of the deformable and rigid striking SUEZMAX tanker at a collision angle of 135 deg.
Appendix B. Maximum Results of Collision Consequence Analysis at Each Collision Angle

**Figure B (1).** The behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy and maximum resultant force at a collision angle of 45 deg.
Figure B (2). The behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy and maximum resultant force at a collision angle of 90 deg.
Figure B (3). The behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy and maximum resultant force at a collision angle of 135 deg.
Appendix C. Maximum Results of Collision Consequence Analysis at Each Collision Velocity

Figure C (1). The behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy and maximum resultant force at a collision speed of 0.5 knots.
Figure C (2). The behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy and maximum resultant force at a collision speed of 3 knots.
Figure C (3). The behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy and maximum resultant force at a collision speed of 6 knots.
Figure C (4). The behaviors of the deformable and rigid striking ship bow on the maximum penetration, maximum absorbed energy and maximum resultant force at a collision speed of 10 knots.